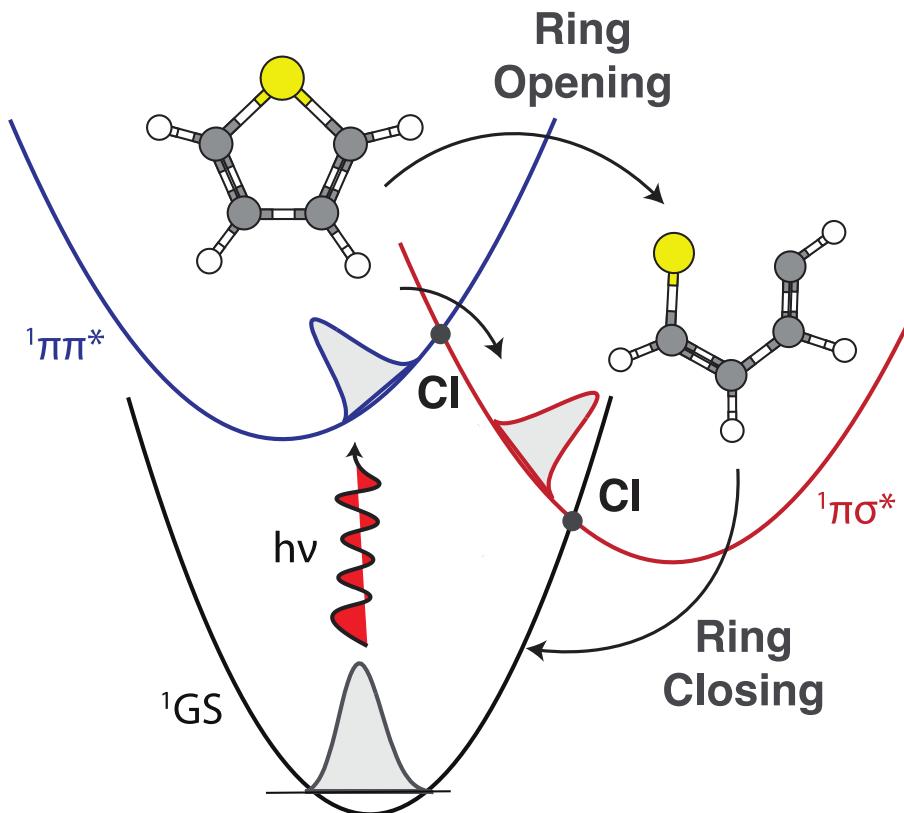
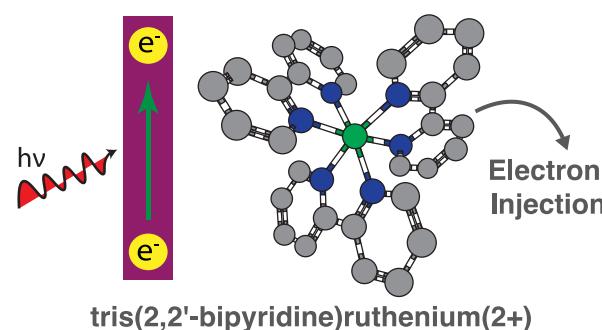
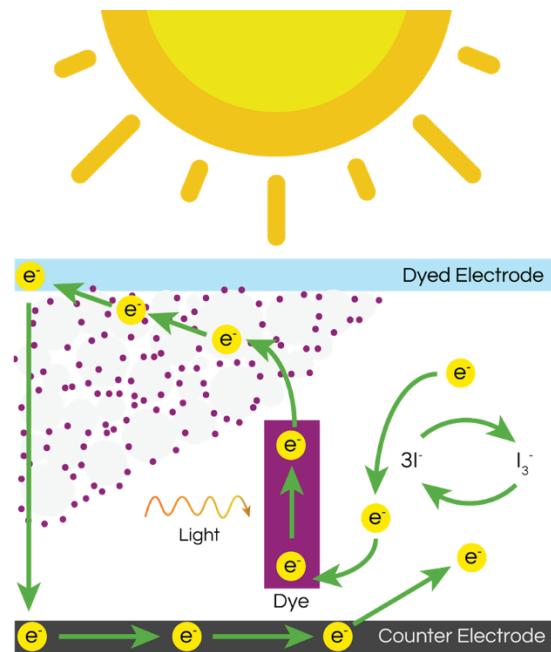


Addressing Challenges and Artifacts on Excited State Potential Energy Surfaces: Insights from Quantum Chemistry and Quasi-Classical Dynamics



Justin J. Talbot
VISTA Seminar
Clemson University
February 26, 2025

Solar Energy Catalysis



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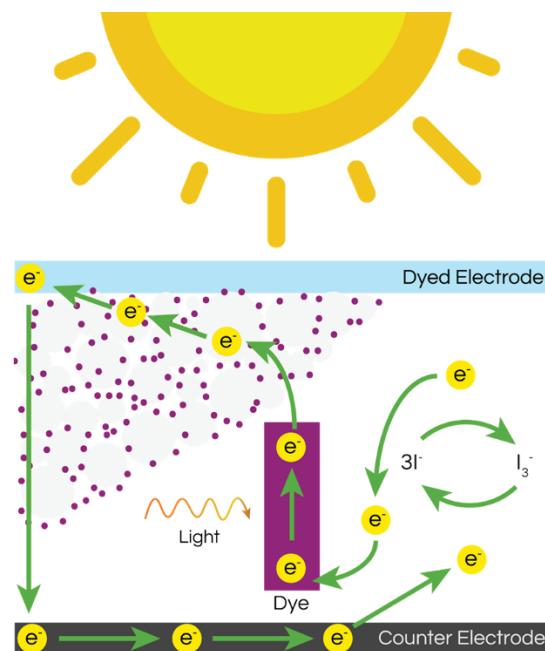
Cheshire, T. P., Houle, F.A., *J. Phys. Chem. A.*, **2021**, 125, 20, 4365-4372

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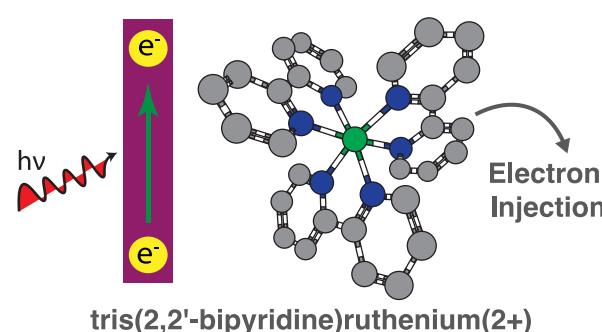
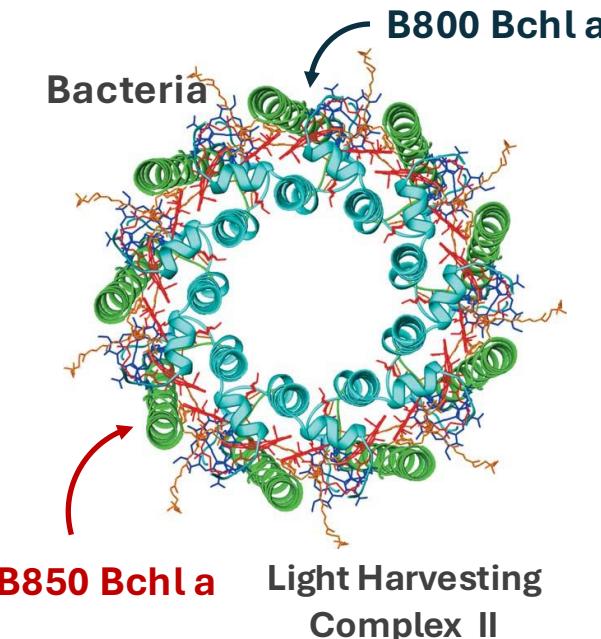
Castro, P. J.; Maeda, S.; Morokuma, K., *Int. J. Quantum. Chem.*, **2021**, 121(14), e26663

Cogdell, R.J., Gardiner, A.T., Roszak, A. W., Law, C. J. Southall, J., Isaacs, N.W. *Photosynth. Res.*, **2004**, 81(3), 207-214.

Solar Energy Catalysis



Biological Systems



Energy Transfer Time:

$B800 \rightarrow B800$	$\sim 0.5\text{ps}$
$B800 \rightarrow B850$	$\sim 0.9\text{ps}$
$B850 \rightarrow B850$	$\sim 50 - 150\text{fs}$

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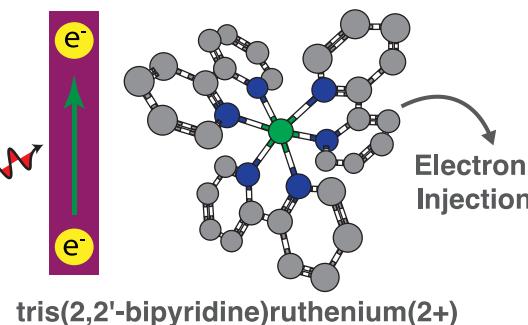
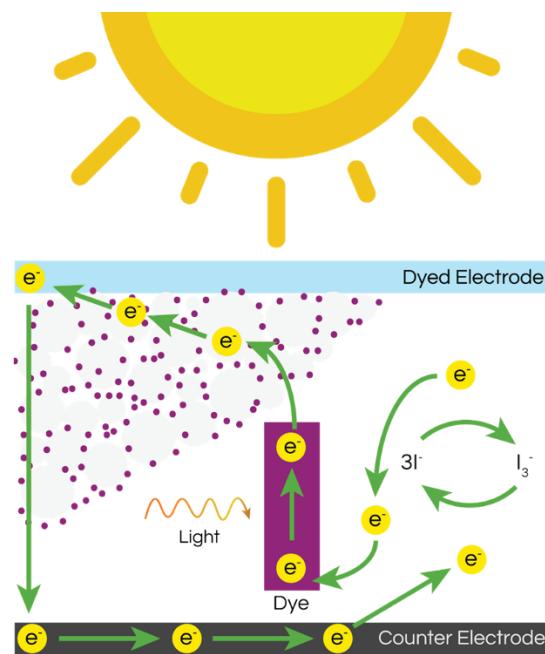
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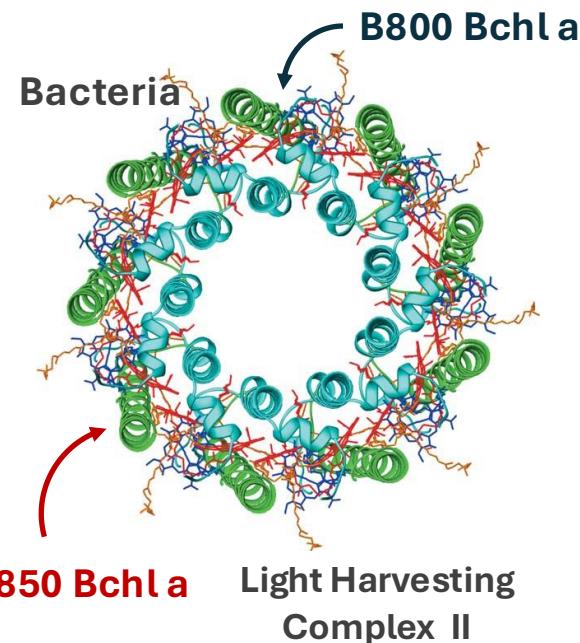
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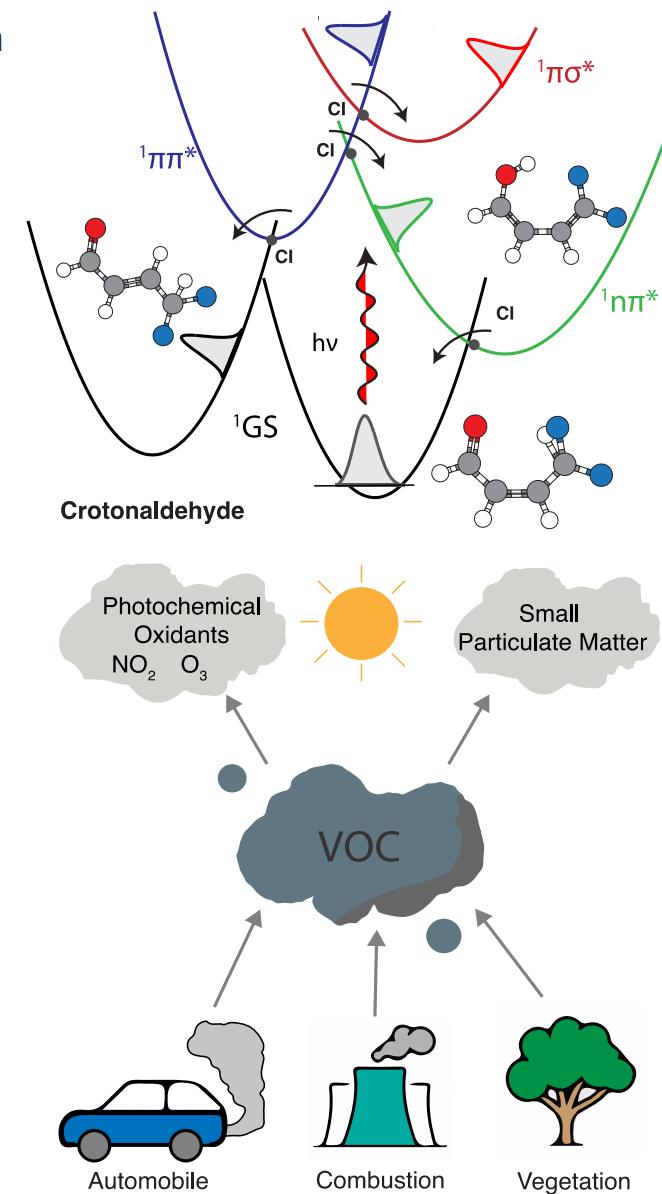
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Atmospheric Chemistry



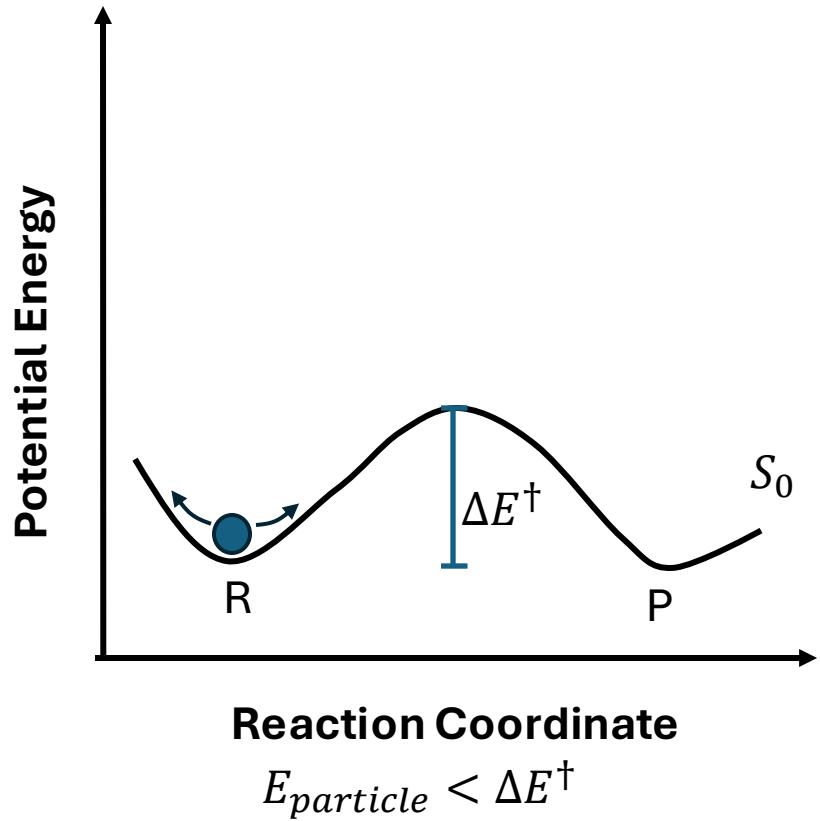
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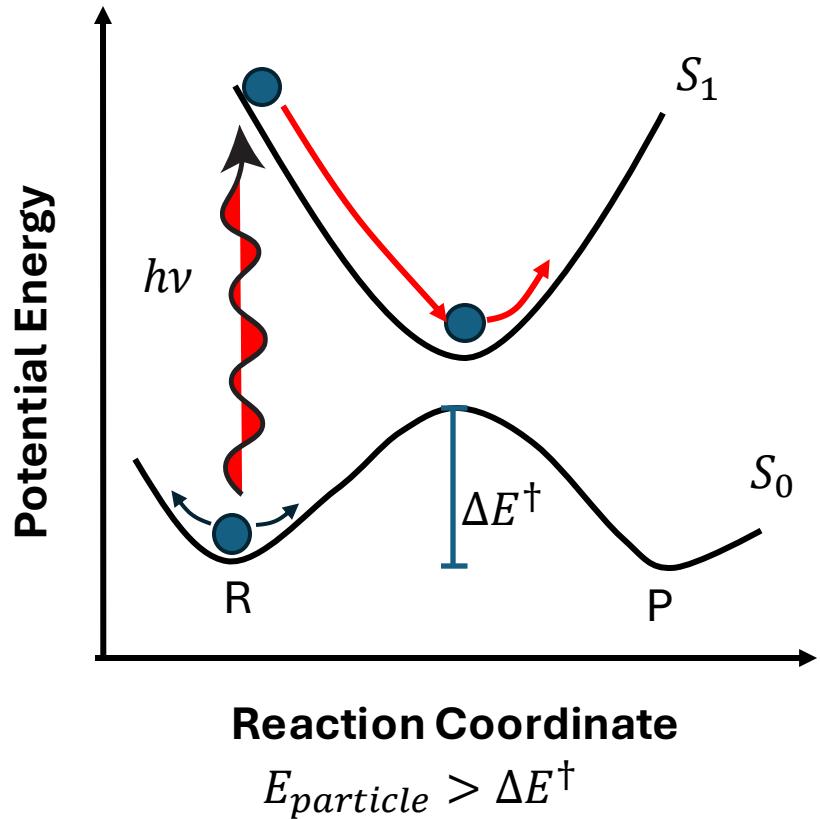


Yarkony, D.R., *J. Chem. Phys.*, **1990**, 92, 2457

Talbot, J.J.* et al., *J. Chem. Phys. Commun.*, **2023**, 159, 171102

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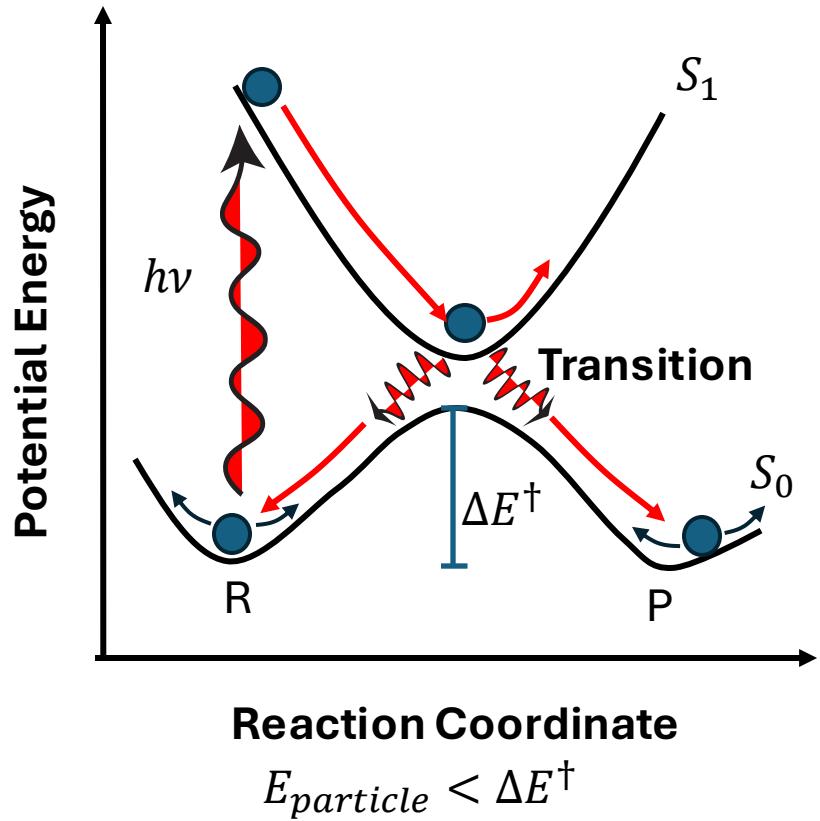


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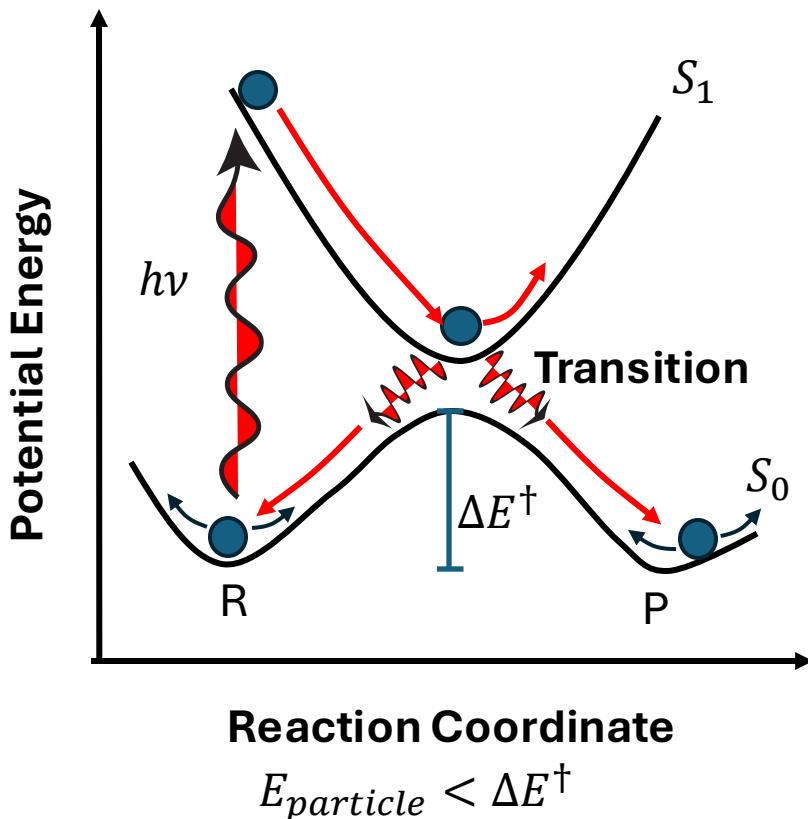
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What are the electronic and nuclear rearrangements that drive electron-nuclear coupling?



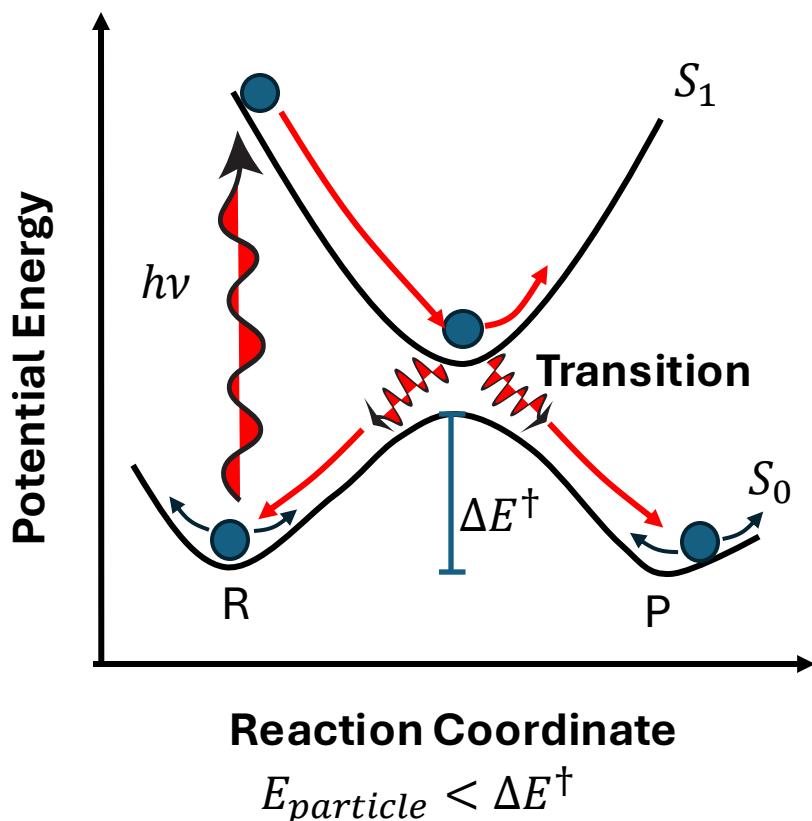
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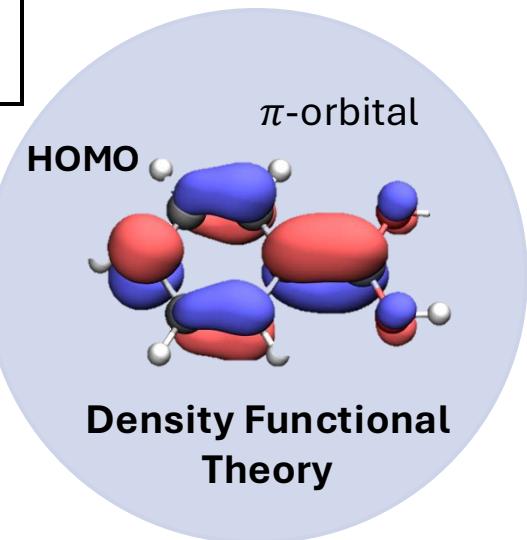
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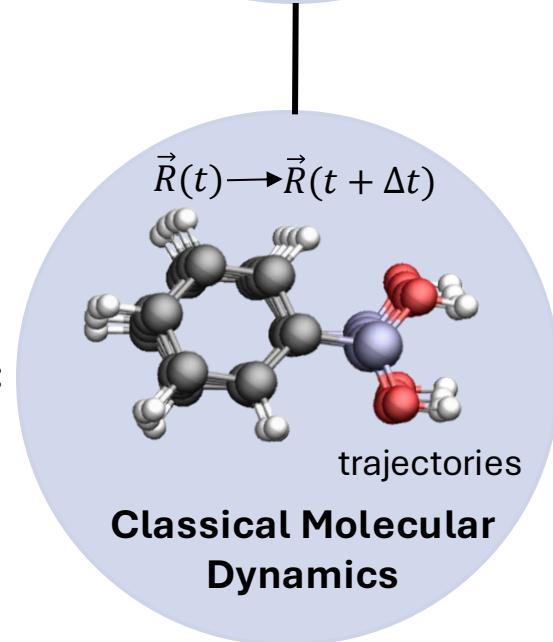
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Electronic
Rearrangements:



Nuclear
Rearrangements:



Predicting properties of excited electronic states of polyatomic molecules requires a combined electronic-nuclear approach.

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Molecular Hamiltonian

$$\begin{aligned}\hat{H}_{mol} &= \frac{\hat{\mathbf{P}}^2}{2M} + \hat{T}_e(\vec{\mathbf{r}}) + \hat{V}_{NN}(\vec{\mathbf{R}}) + \hat{V}_{eN}(\vec{\mathbf{r}}, \vec{\mathbf{R}}) + \hat{V}_{ee}(\vec{\mathbf{r}}) \\ &= \frac{\hat{\mathbf{P}}^2}{2M} + \hat{T}_e(\vec{\mathbf{r}}) + \hat{U}(\vec{\mathbf{r}}, \vec{\mathbf{R}})\end{aligned}$$

Predicting properties of excited electronic states of polyatomic molecules requires a combined electronic-nuclear approach.

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Assume time-scale separability between the nuclear degrees of freedom ($\vec{\mathbf{R}}$) and the electronic degrees of freedom ($\vec{\mathbf{r}}$) which allows \hat{H}_{mol} to be separated into two parts.

$$\hat{H}_{elec} = \hat{T}_e(\vec{\mathbf{r}}) + \hat{U}(\vec{\mathbf{r}}, \vec{\mathbf{R}}) \quad \hat{H}_{elec}\phi_I(\vec{\mathbf{r}}; \vec{\mathbf{R}}) = V_I(\vec{\mathbf{R}})\phi_I(\vec{\mathbf{r}}; \vec{\mathbf{R}})$$

$$\hat{H}_{Nuc} = \frac{\hat{\mathbf{P}}^2}{2M} + \hat{V}_I(\vec{\mathbf{R}}) \quad \hat{H}_{Nuc}\chi_I(\vec{\mathbf{R}}) = E_I\chi_I(\vec{\mathbf{R}})$$

Propagate the electronic degrees of freedom (TDSE)

$$i\hbar \dot{C}_K + i\hbar \sum_J C_J \langle \phi_K | \dot{\phi}_J \rangle = C_K V_K(\vec{\mathbf{R}})$$

Tully, *J. Chem. Phys.*, **1990**, 93, 1061.

Meyer, H.D., Miller, W. H., *J. Chem. Phys.*, **1979**, 70, 7, 3214-3223.

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Assume that the nuclear motion can be described a trajectory $\vec{\mathbf{R}}(t)$

$$i\hbar \dot{C}_K = C_K V_K(\vec{\mathbf{R}}) - i\hbar \sum_J C_J \dot{\vec{\mathbf{R}}} d_{kJ}(\vec{\mathbf{R}})$$

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$$i\hbar \dot{C}_K = C_K V_K(\vec{R}) - i\hbar \sum_J C_J \dot{\vec{R}} d_{kJ}(\vec{R})$$

Meyer-Miller dynamics require that the electronic coefficients evolve according to Hamilton's equations

$$C_K = \frac{1}{\sqrt{2}} [x_K + ip_K] \quad \longleftarrow \quad \text{canonically-conjugate electronic positions \& momenta}$$

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Putting this together the Meyer-Miller Hamiltonian is

$$H(x, p, \mathbf{R}, \mathbf{P}) = \frac{\mathbf{1}}{2M} \left(\vec{\mathbf{P}} + \sum_{JK}^F x_J p_K \mathbf{d}_{JK}(\vec{\mathbf{R}}) \right)^2 + \sum_K^F \left(\frac{1}{2} p_K^2 + \frac{1}{2} x_K^2 - \gamma_K \right) V_K(\mathbf{R})$$

n_K Ehrenfest $\gamma_K = 0$

Notes provided to me by Bill Miller.

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Cotton, S. J., Miller, W. H., *J. Chem. Phys A.*, **2013**, 117, 32 7190-7194.

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\nearrow
 $n_K \text{ Ehrenfest } \gamma_K = 0$

Propagate the dynamics classically by applying Hamilton's equations to the Hamiltonian

$$\dot{x}_I = \frac{\partial H}{\partial p_I} \quad \dot{p}_I = -\frac{\partial H}{\partial x_I} \quad \dot{\mathbf{R}} = \frac{\partial H}{\partial \vec{\mathbf{P}}} \quad \dot{\vec{\mathbf{P}}} = -\frac{\partial H}{\partial \mathbf{R}}$$

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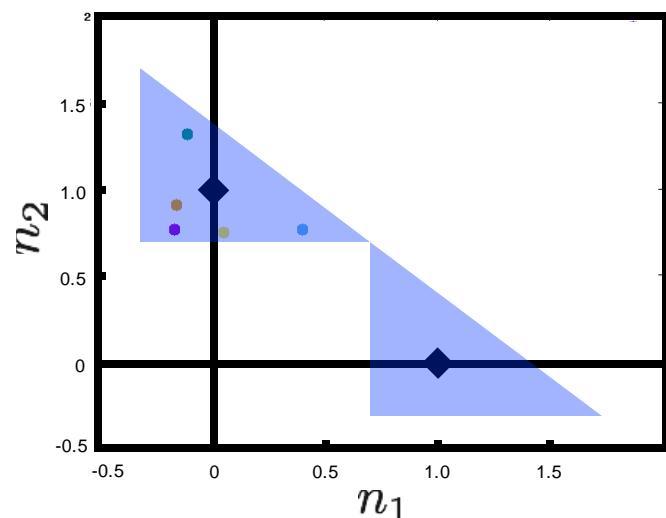
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Symmetric Quasi-classical Approach (SQC)

Quantize the action variables by binning according to windowing functions



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The Tamm-Dancoff Approximation (TDDFT)

$$\mathbf{A} \mathbf{X}^I = \omega_I \mathbf{X}^I$$

$$|\phi_I\rangle = \sum_{ia} X_{ai}^I |\Phi_i^a\rangle$$

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Hellmann-Feynman Derivative Coupling

$$\hat{\mathbf{d}}_{IJ}(\vec{\mathbf{R}}) = \langle \phi_I | \phi_J^{[\mathbb{R}]} \rangle = \frac{\langle \phi_I | \hat{H}_{elec}^{[\mathbb{R}]} | \phi_J \rangle}{\omega_J - \omega_I} = \frac{1}{\omega_J - \omega_I} \sum_{ijab} X_{ai}^I A_{ai,bj}^{[\mathbb{R}]} X_{bj}^J$$

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$$\sum_{ijab} X_{ai}^I A_{ai,bj}^{[R]} X_{bj}^J = \mathbf{P}_\Delta^{IJ'} \cdot \mathbf{H}^{[R]} + \boldsymbol{\Gamma}^{IJ'} \cdot \boldsymbol{\Pi}^{[R]} + \mathbf{W}^{IJ'} \cdot \mathbf{S}^{[R]} + \mathbf{P}_\Delta^{IJ'} \cdot \mathbf{F}_{xc}^{[R]} + \mathbf{T}^{I\dagger} \cdot \boldsymbol{\Omega}^{[R]} \cdot \mathbf{T}^J$$

Relaxed 1PDM

$$\mathbf{P}_\Delta^{IJ'}$$

$$F(F+1)/2$$

Relaxed 2PDM

$$\boldsymbol{\Gamma}^{IJ'}$$

$$F(F+1)/2$$

Relaxed EWDM

$$\mathbf{W}'$$

$$F(F+1)/2$$

Transition DM

$$\mathbf{T}^I$$

$$F$$

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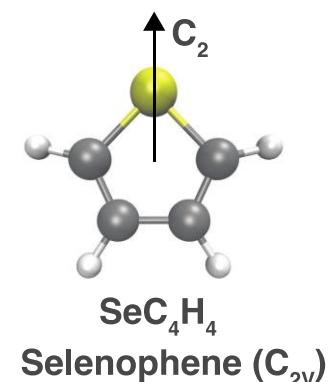
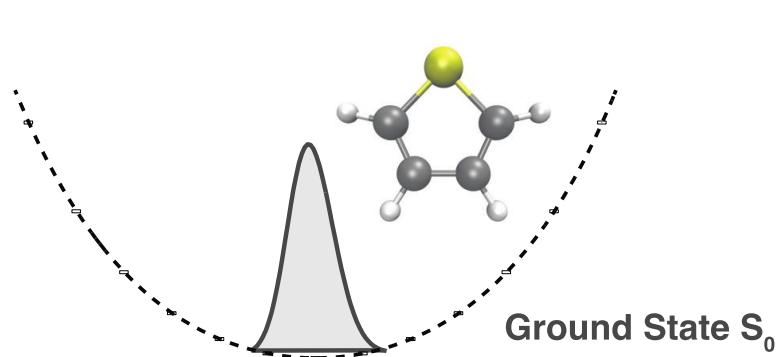
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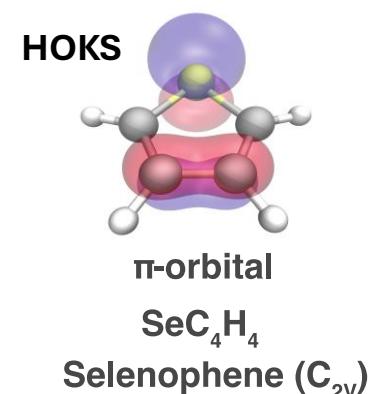
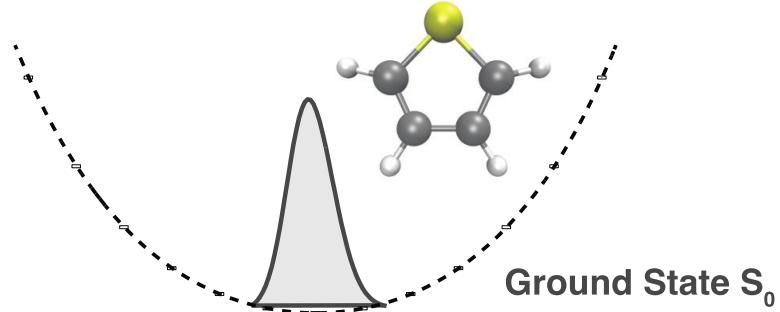
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Parallelize contractions!

Selenophene (SeC_4H_4)

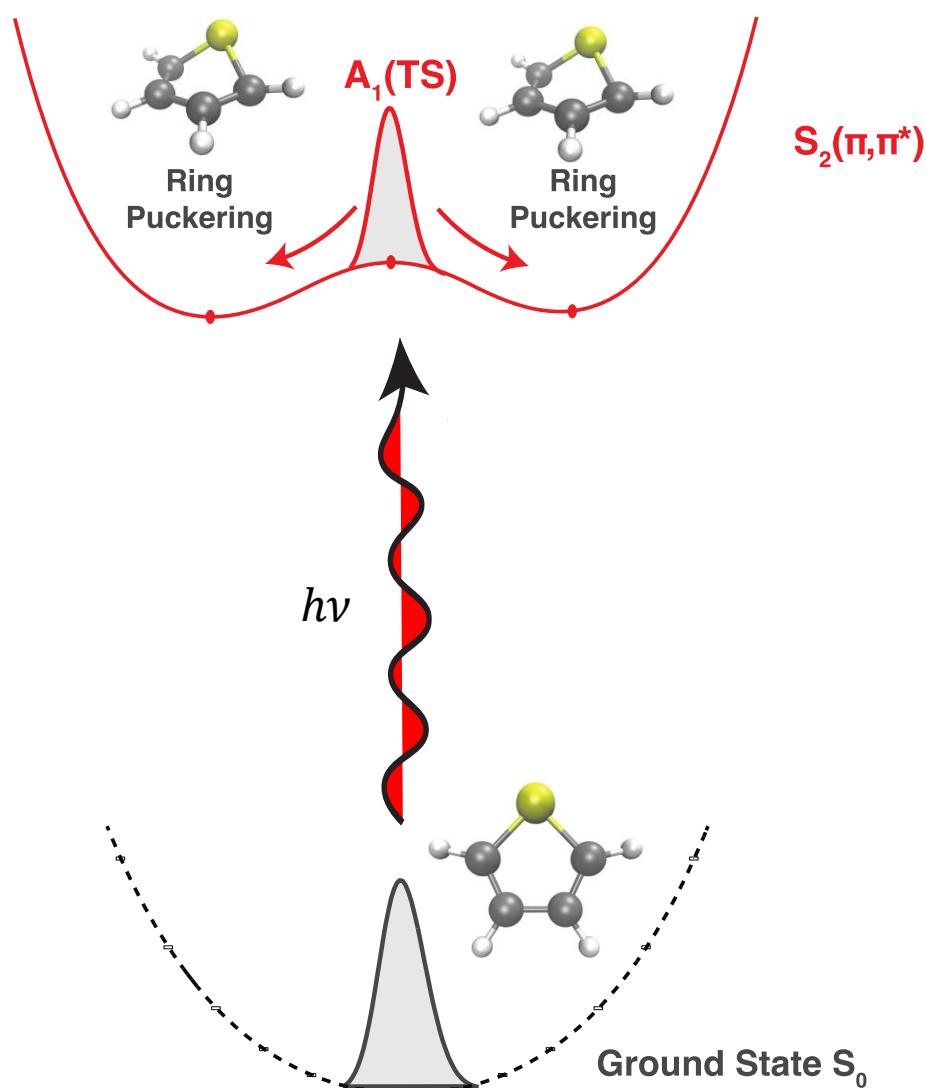


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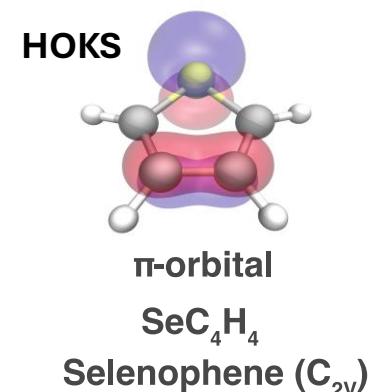
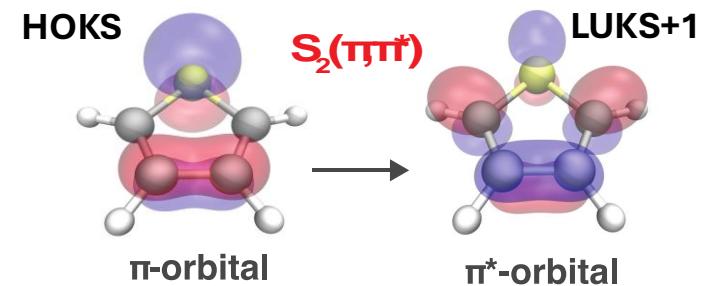


Selenophene (SeC_4H_4)

Nuclear Rearrangement

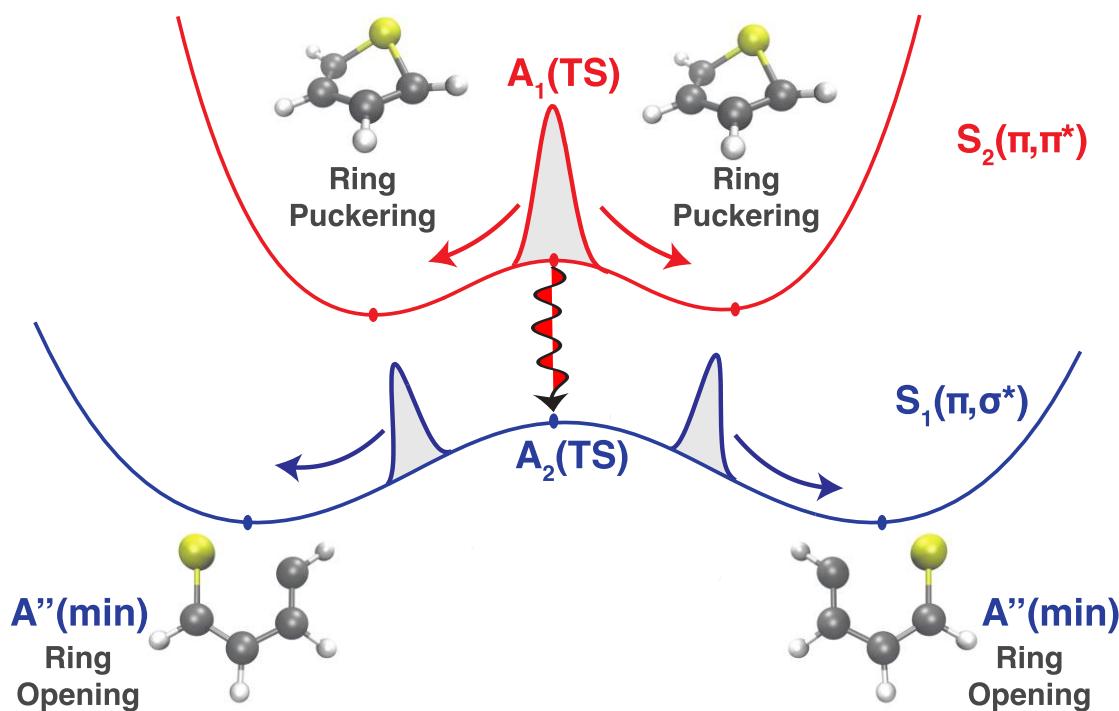


Electronic Rearrangement

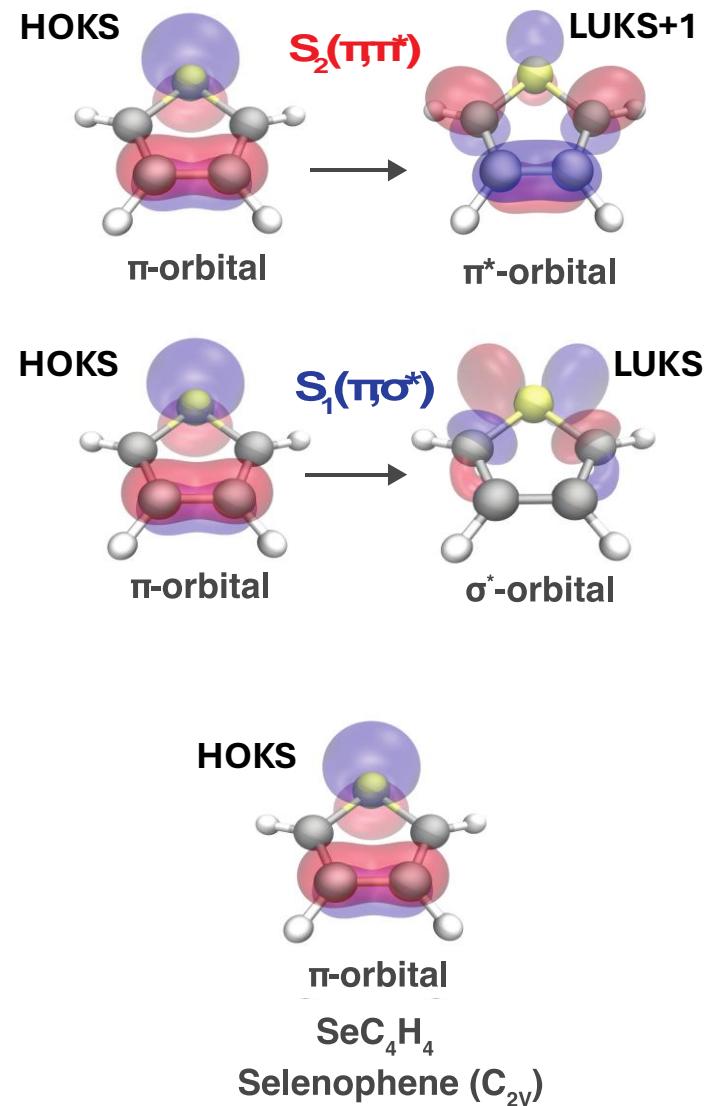


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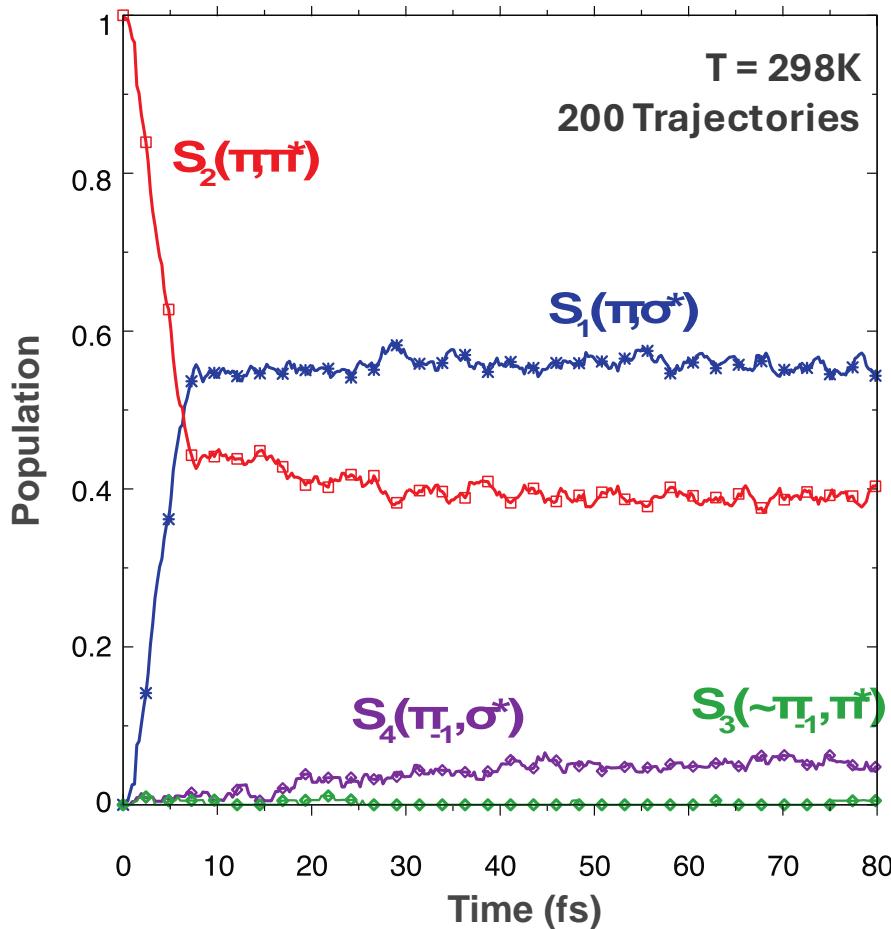
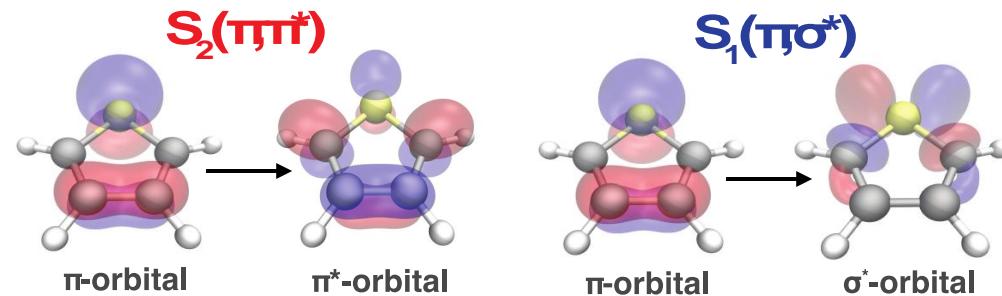
Nuclear Rearrangement



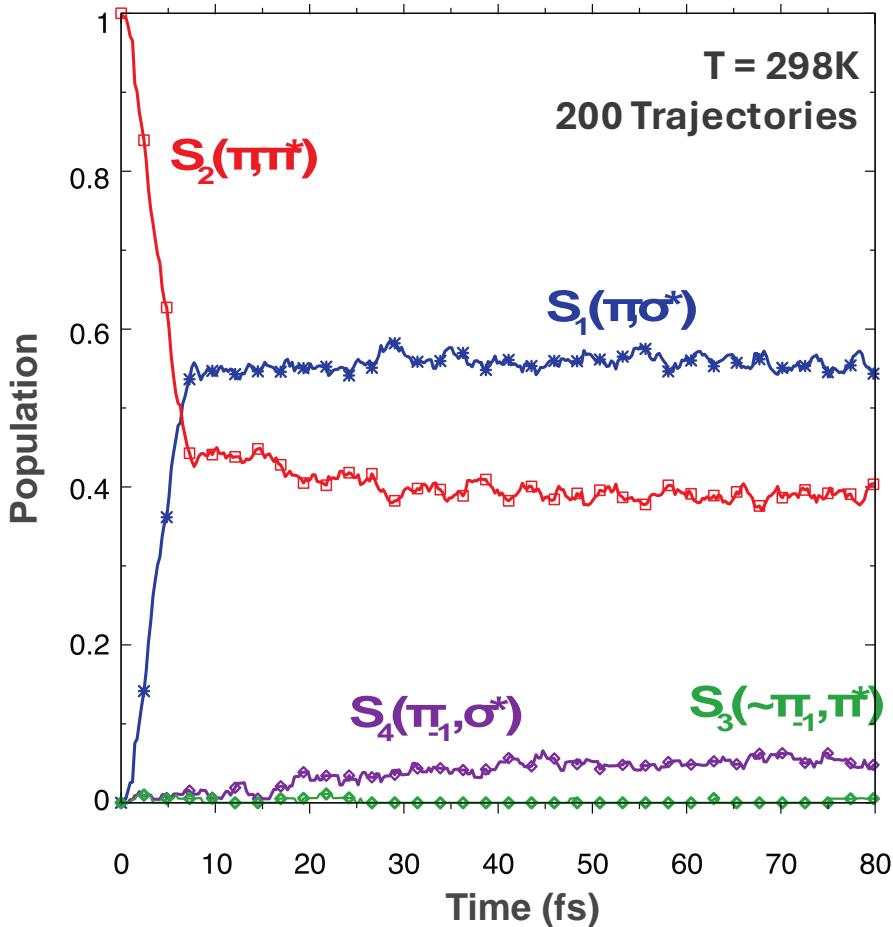
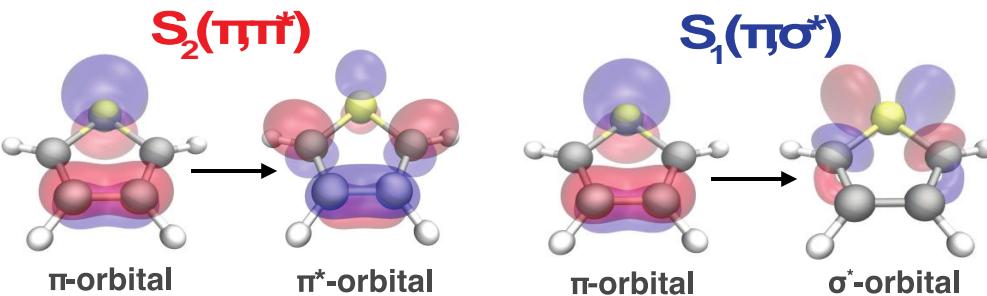
Electronic Rearrangement



Selenophene (SeC_4H_4)



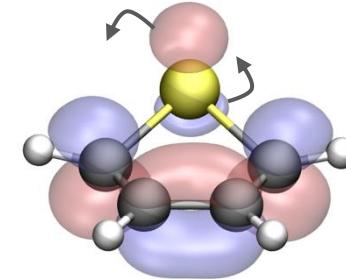
Selenophene (SeC_4H_4)



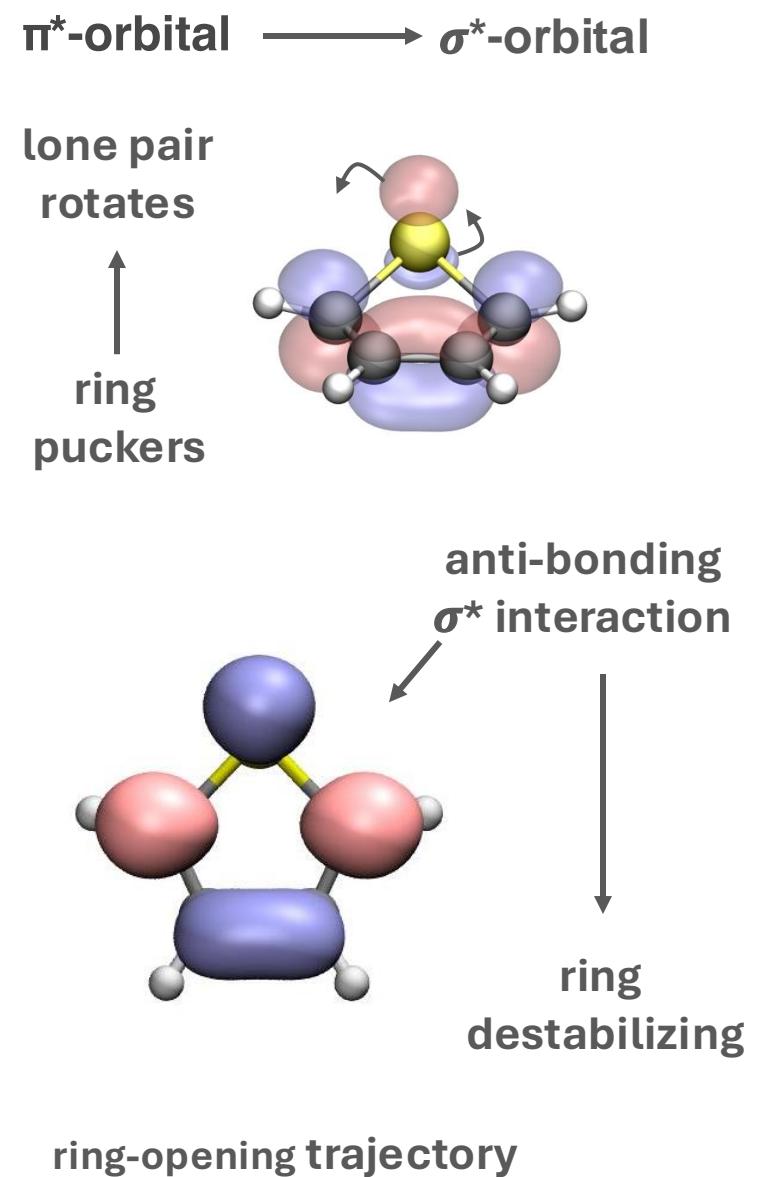
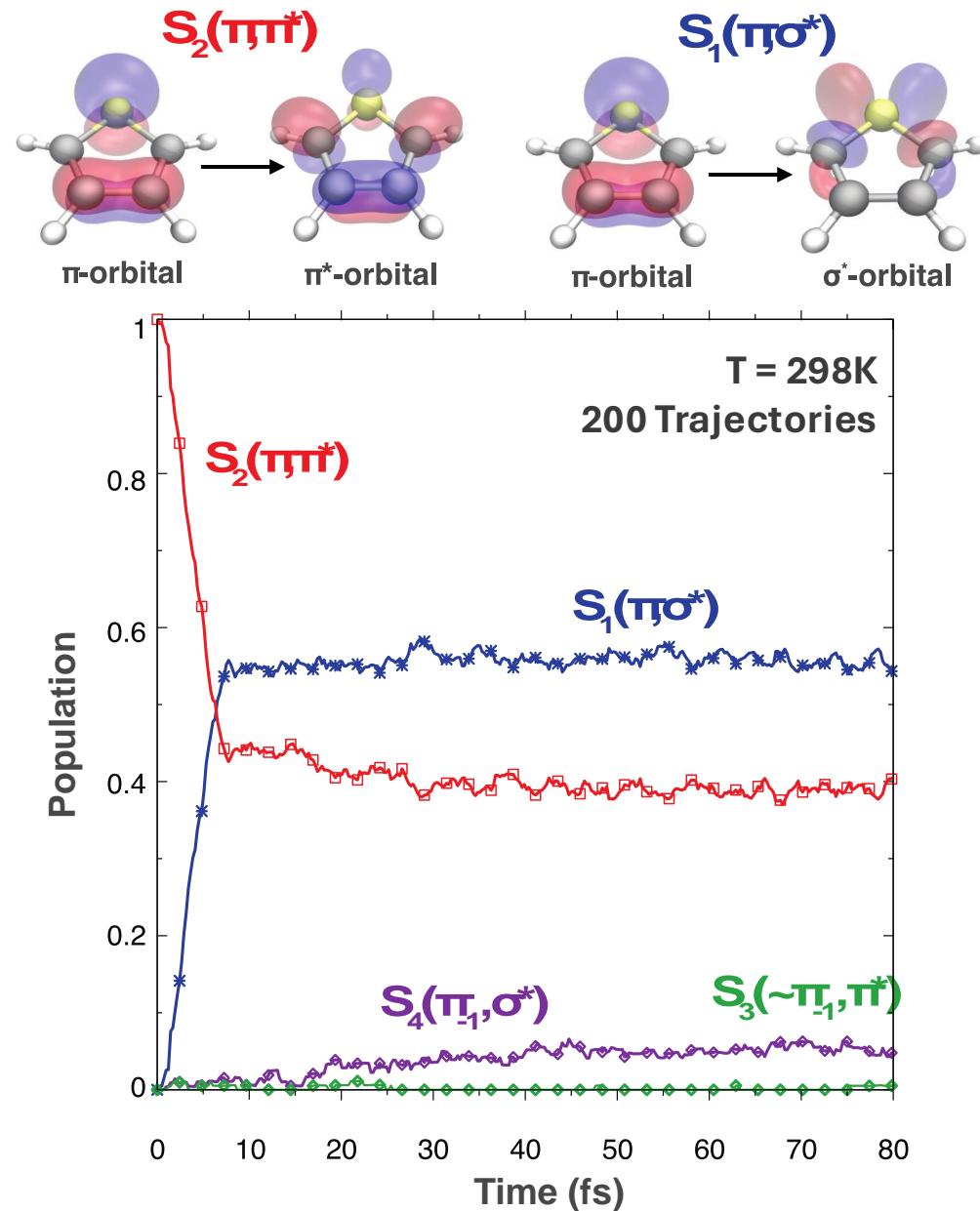
$\pi^*\text{-orbital} \longrightarrow \sigma^*\text{-orbital}$

lone pair
rotates

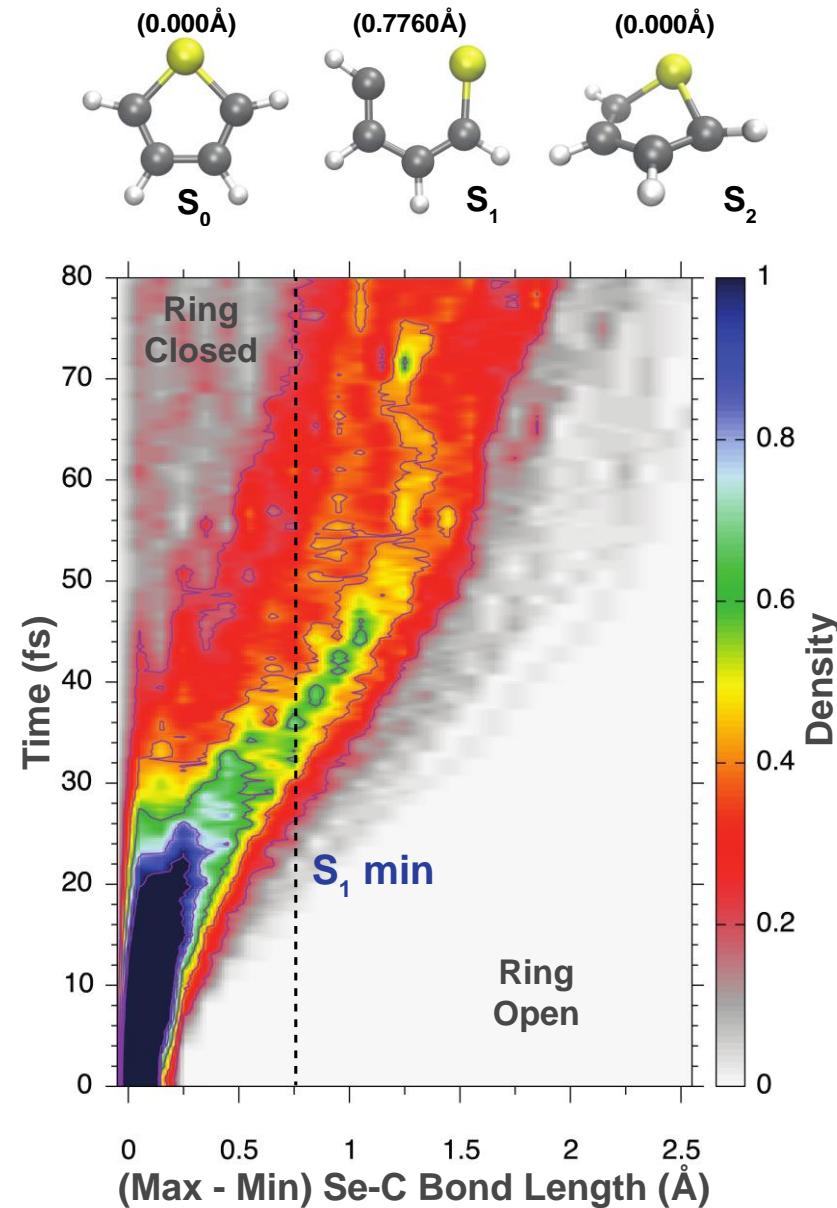
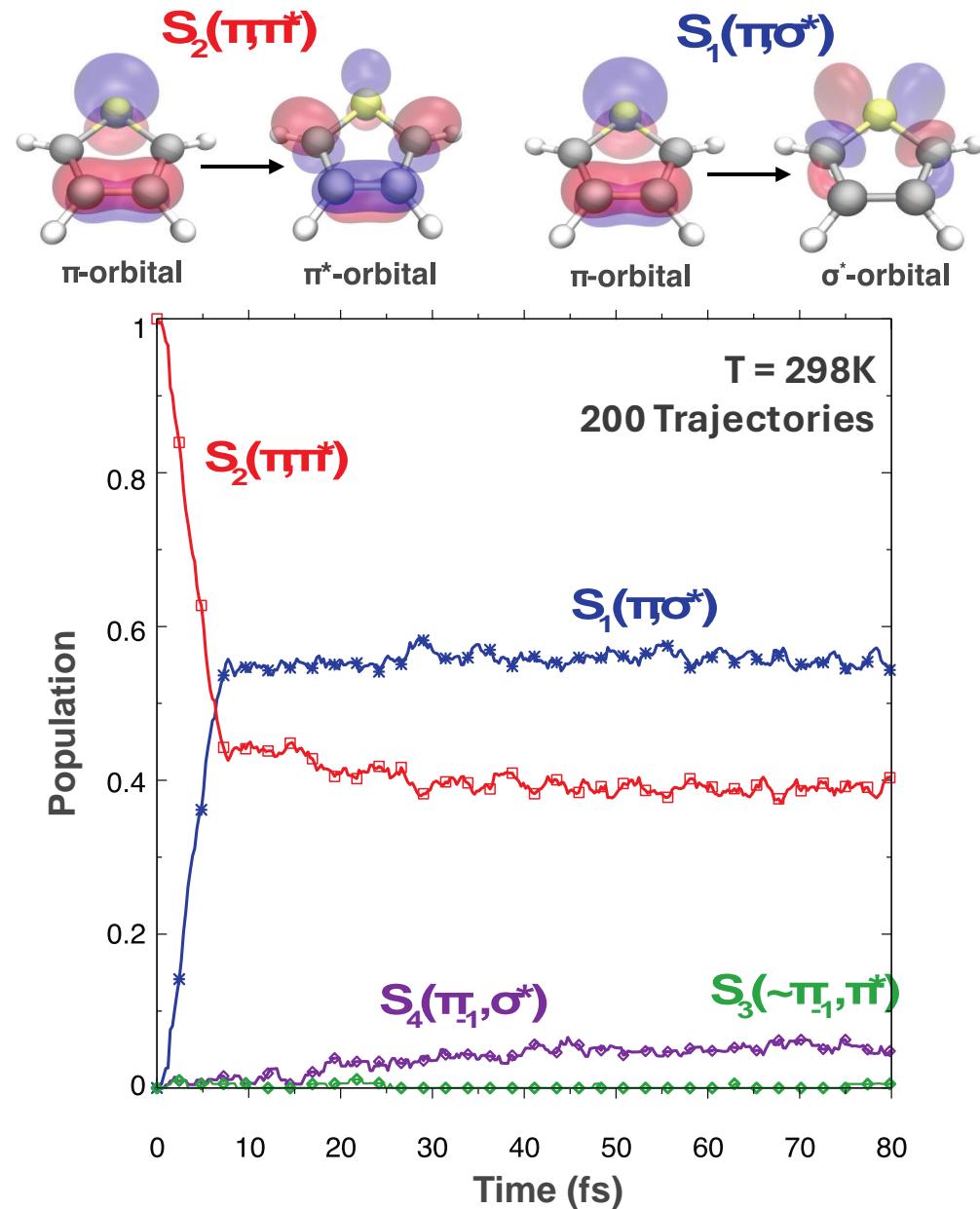
↑
ring
puckers



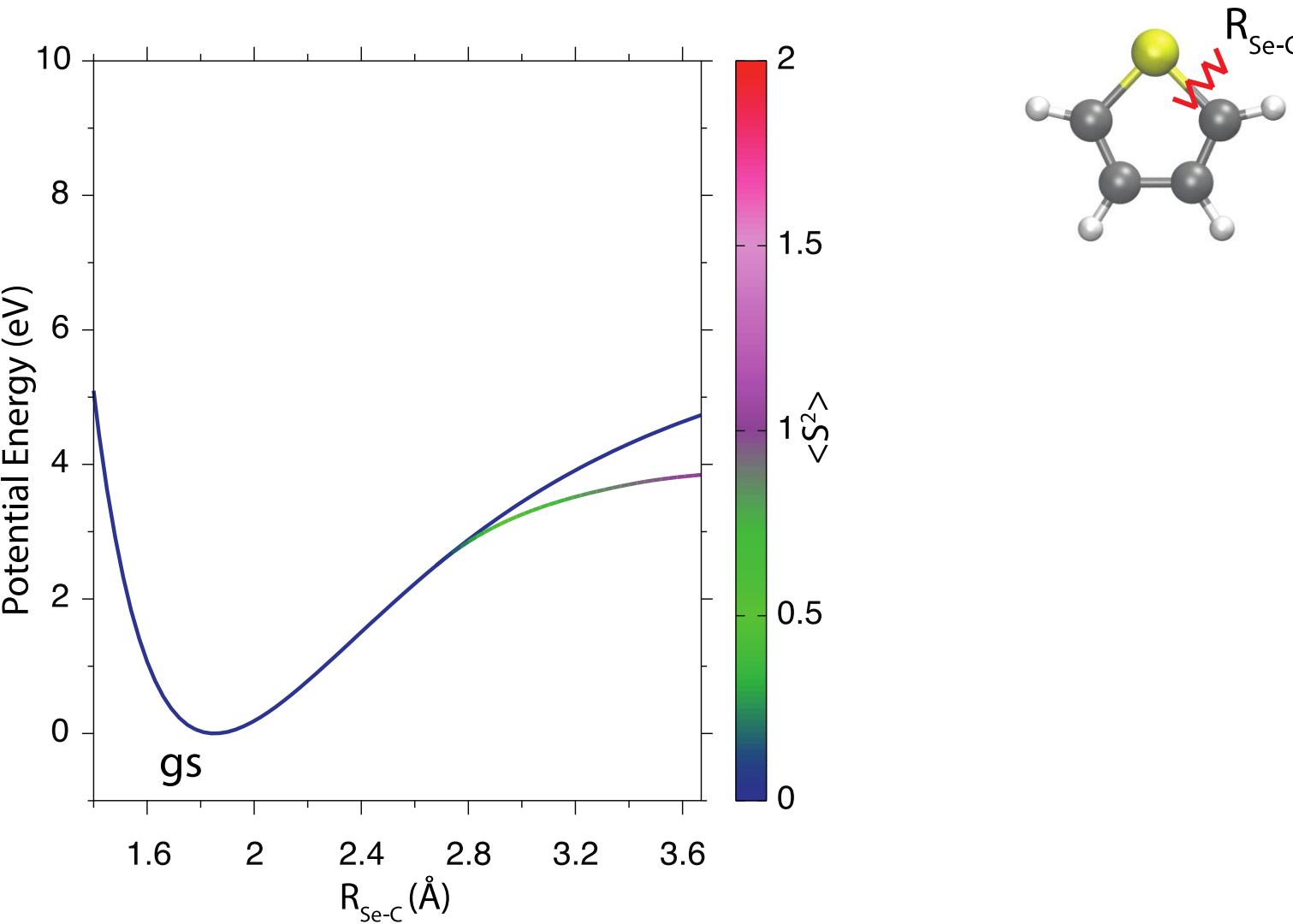
Selenophene (SeC_4H_4)



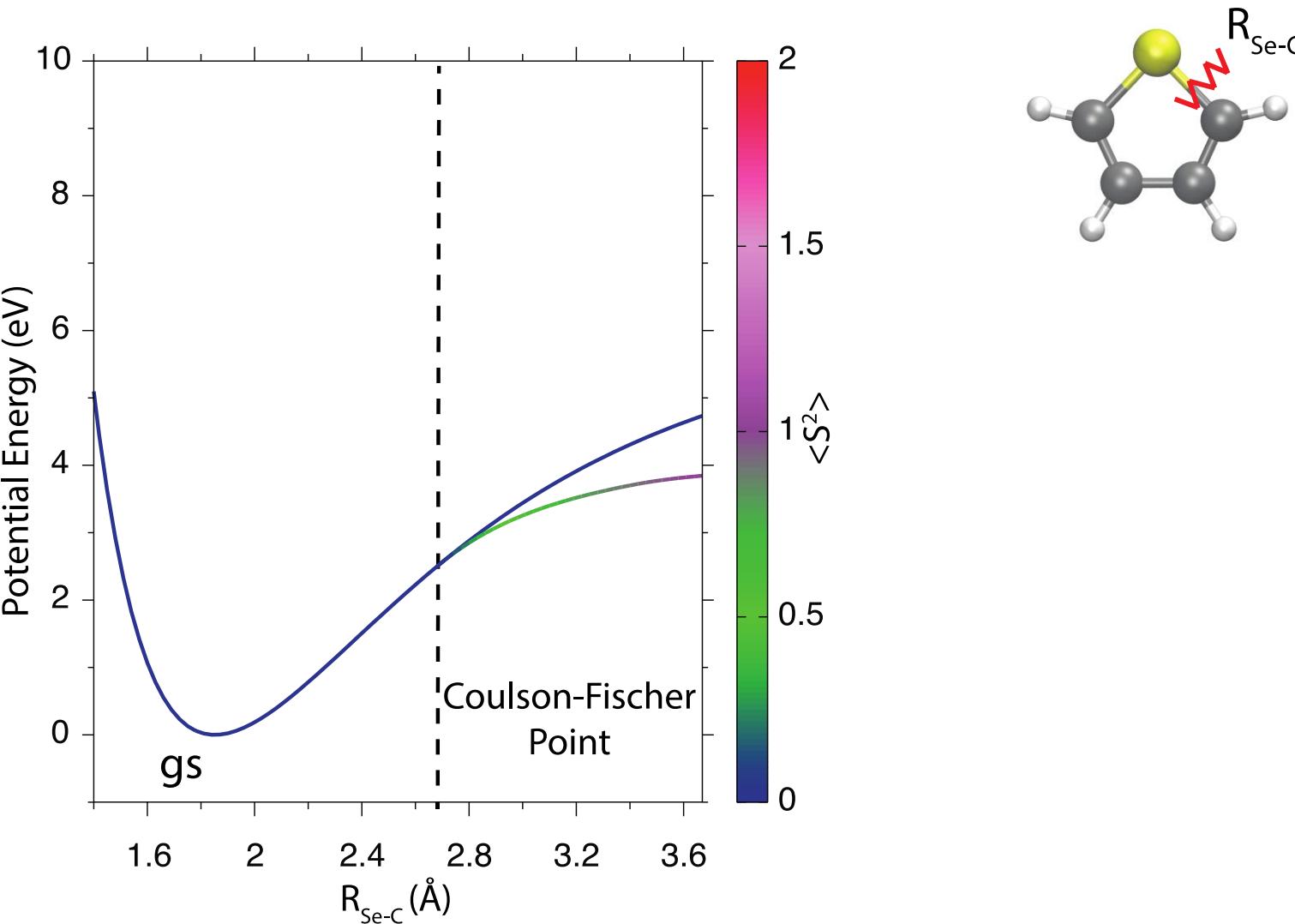
Selenophene (SeC_4H_4)



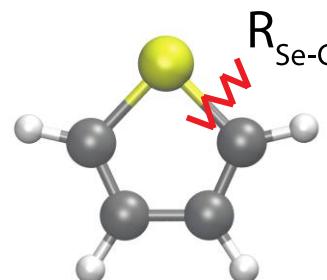
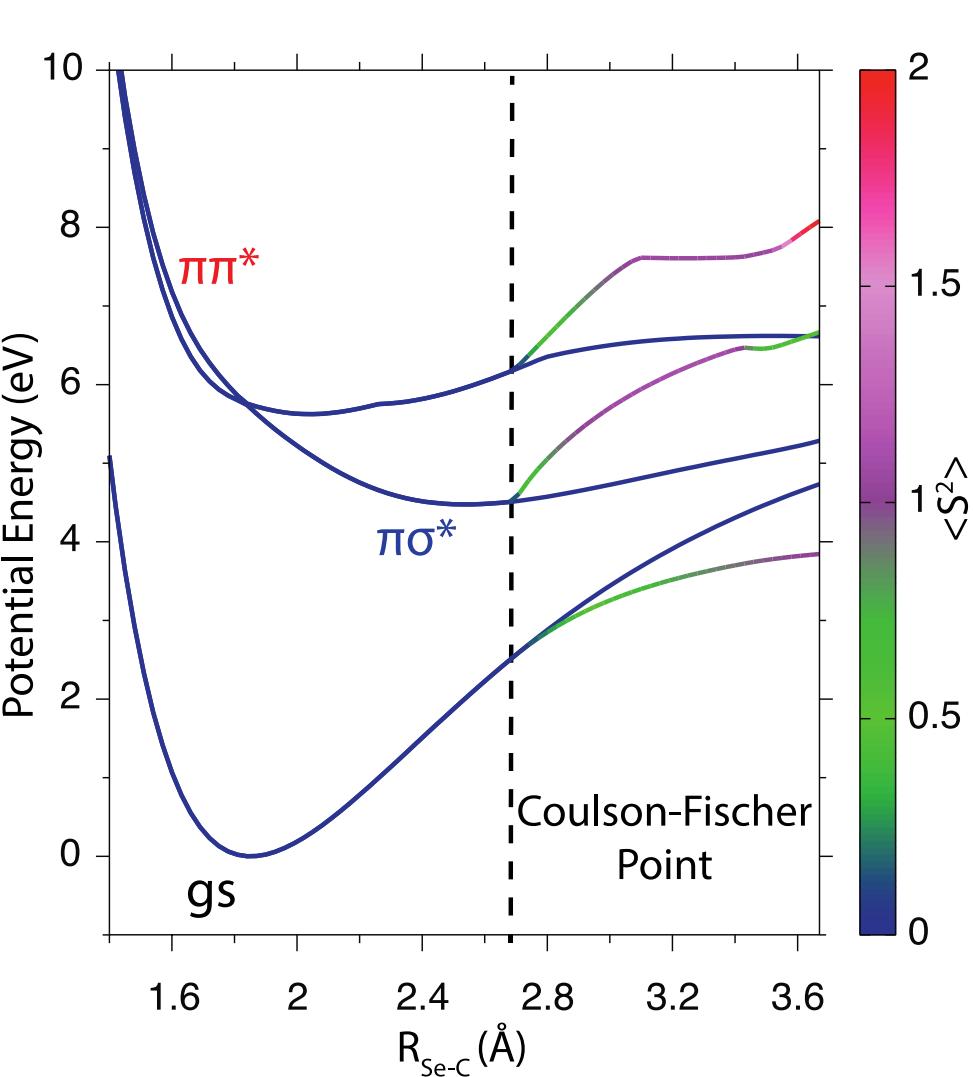
Realistic predictions of bond-breaking requires electronic structure theories that include static correlation.



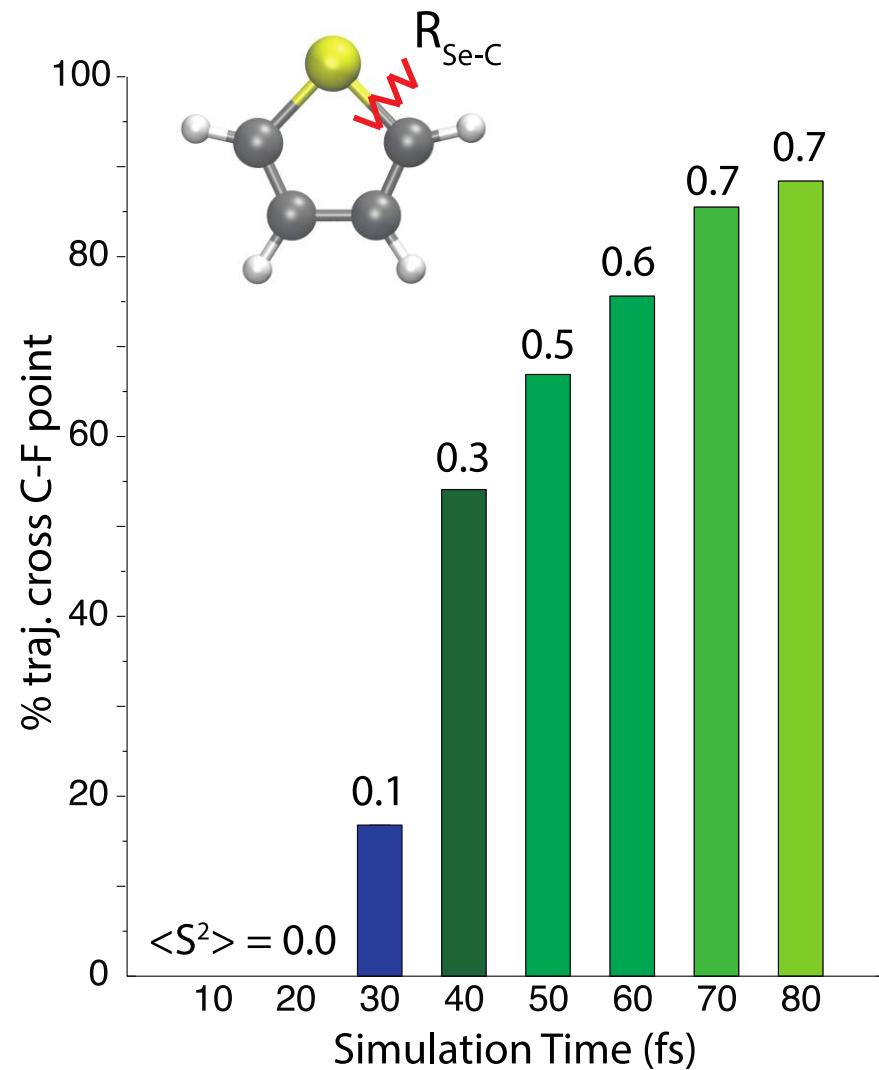
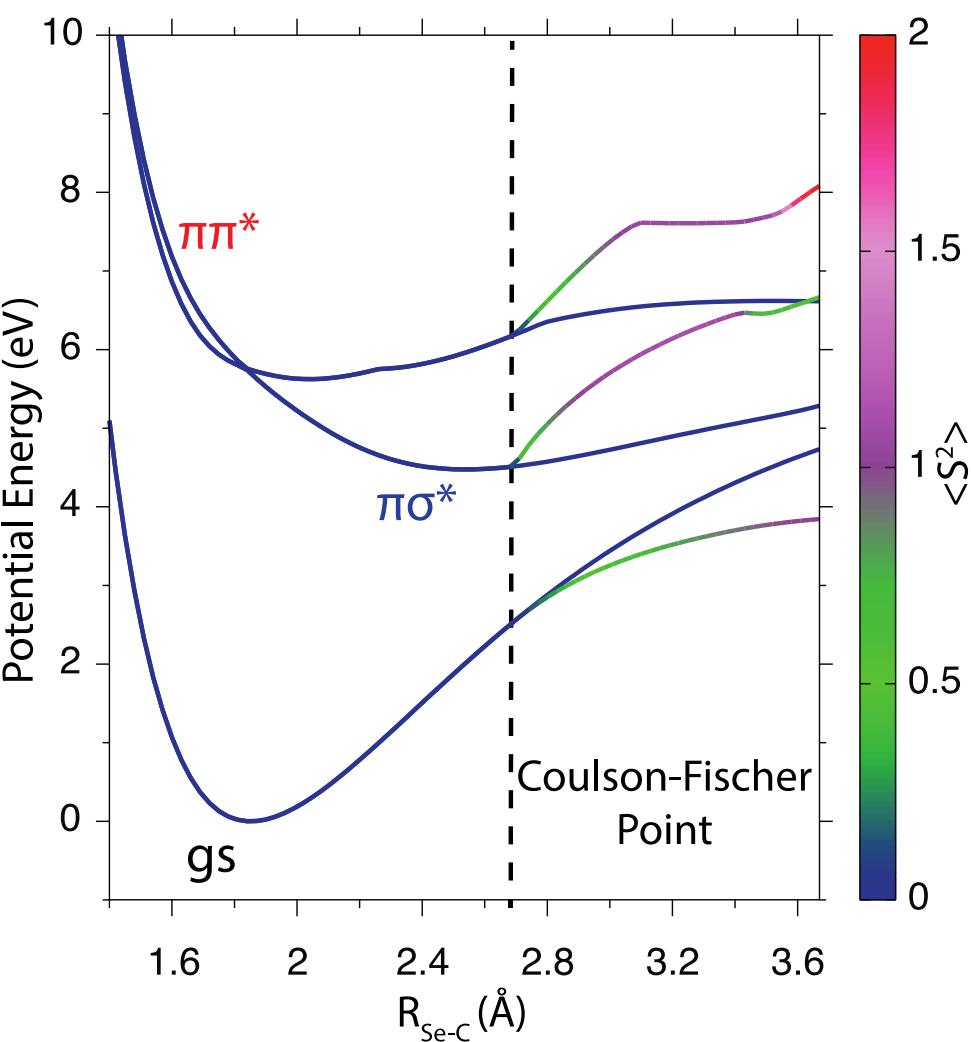
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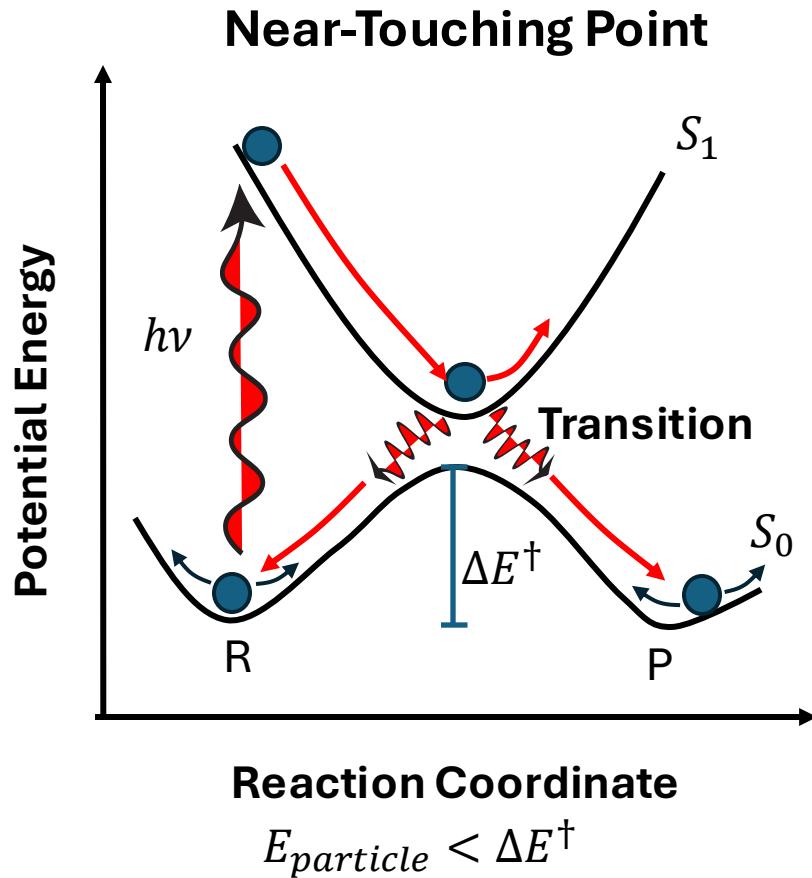
Realistic predictions of bond-breaking requires electronic structure theories that include static correlation.



Realistic predictions of bond-breaking requires electronic structure theories that include static correlation.



Fantastical excited state minimum energy configurations
can appear stable near conical intersections.



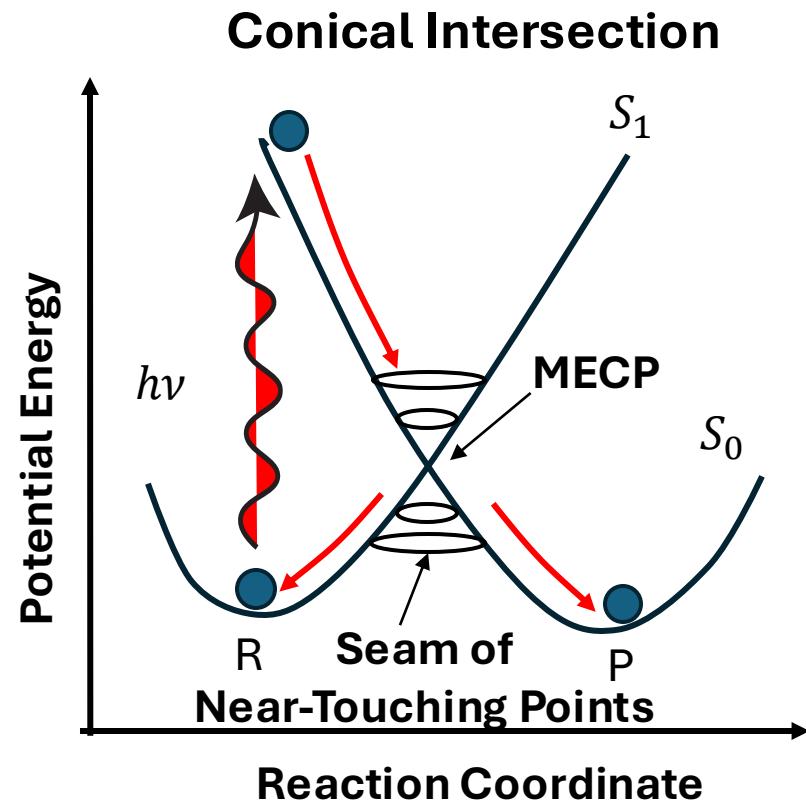
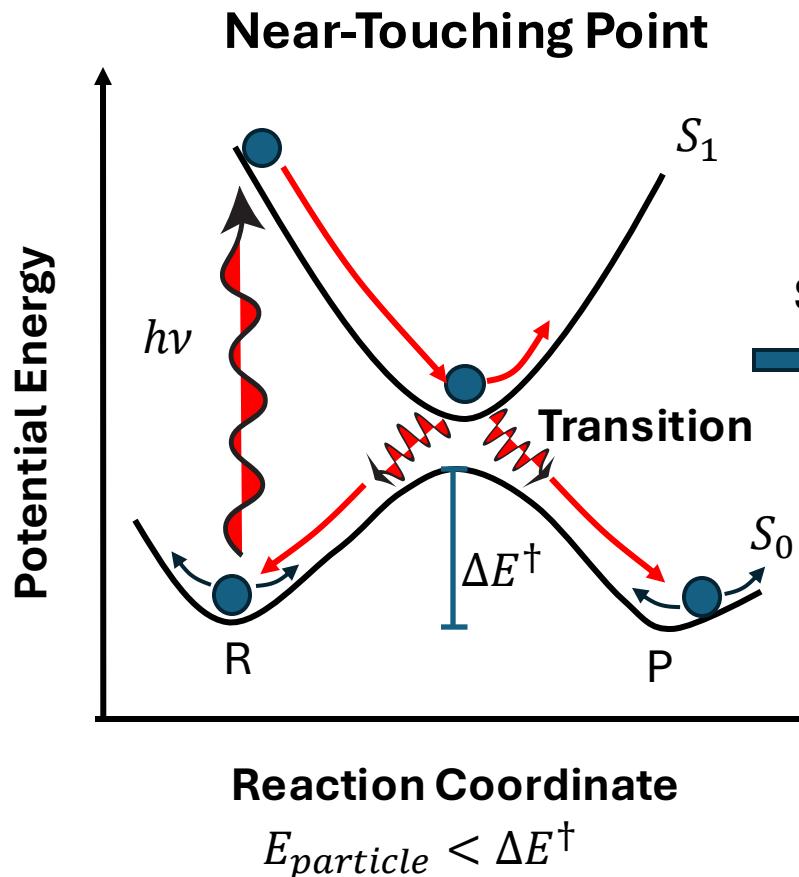
Yarkony, D.R., *J. Chem. Phys.*, **1990**, 92, 2457

Talbot, J.J.* et al., *J. Chem. Phys. Commun.*, **2023**, 159, 171102

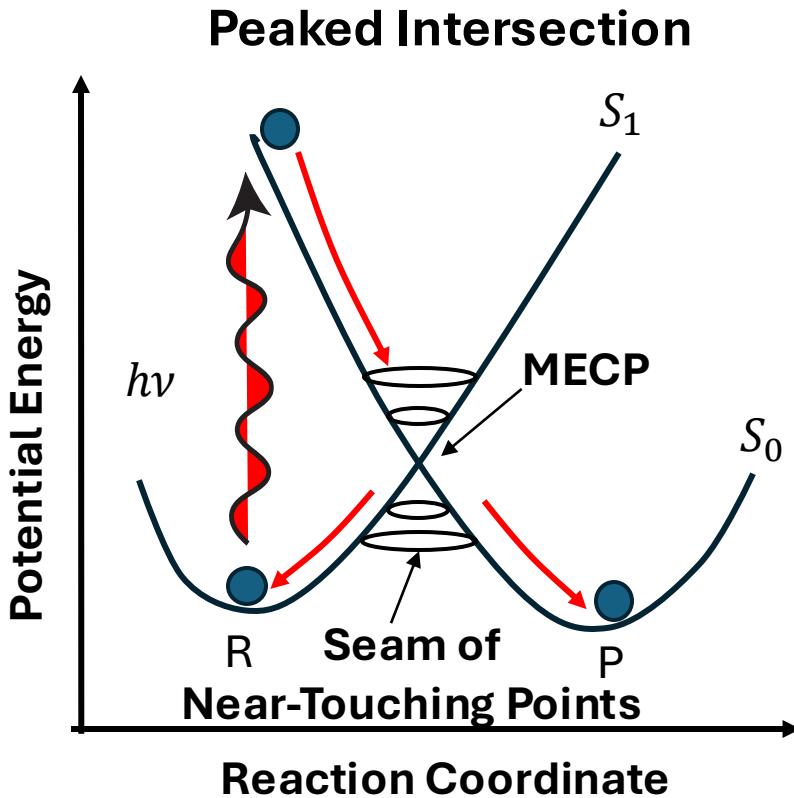
Talbot, J.J.* Head-Gordon, M., Cotton, S. J., *Mol. Phys.*, **2022**, 121, 7-8

Talbot, J.J.* et al., *Phys. Chem. Chem. Phys.*, **2022**, 24, 4820-4831

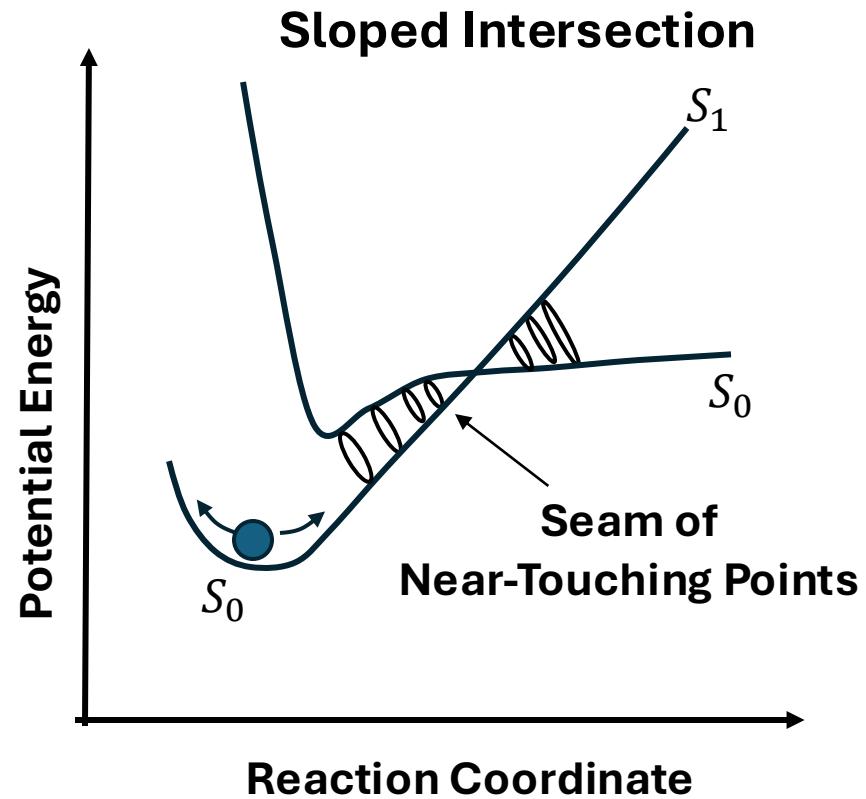
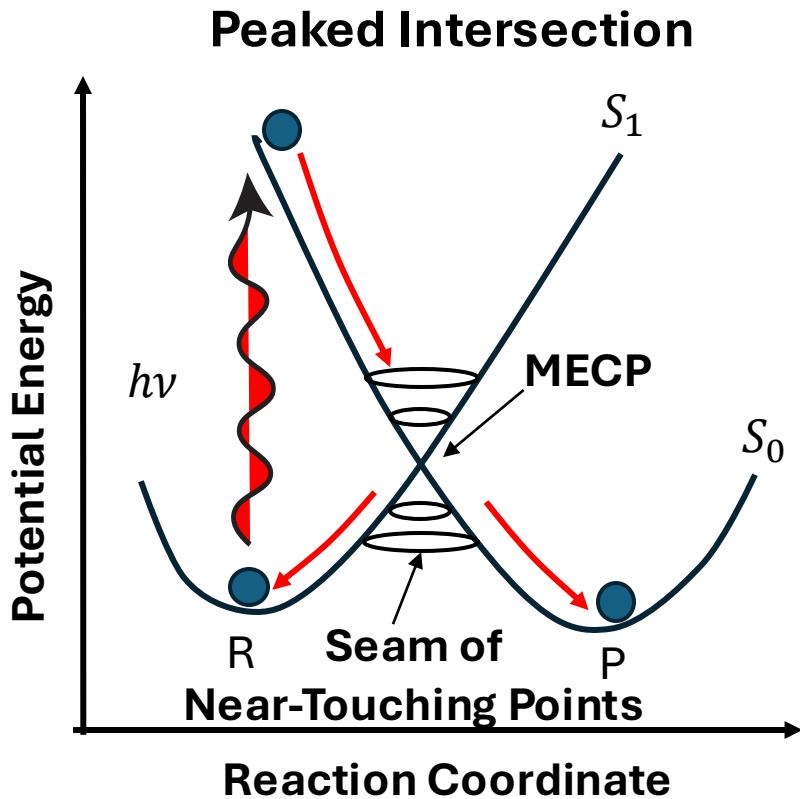
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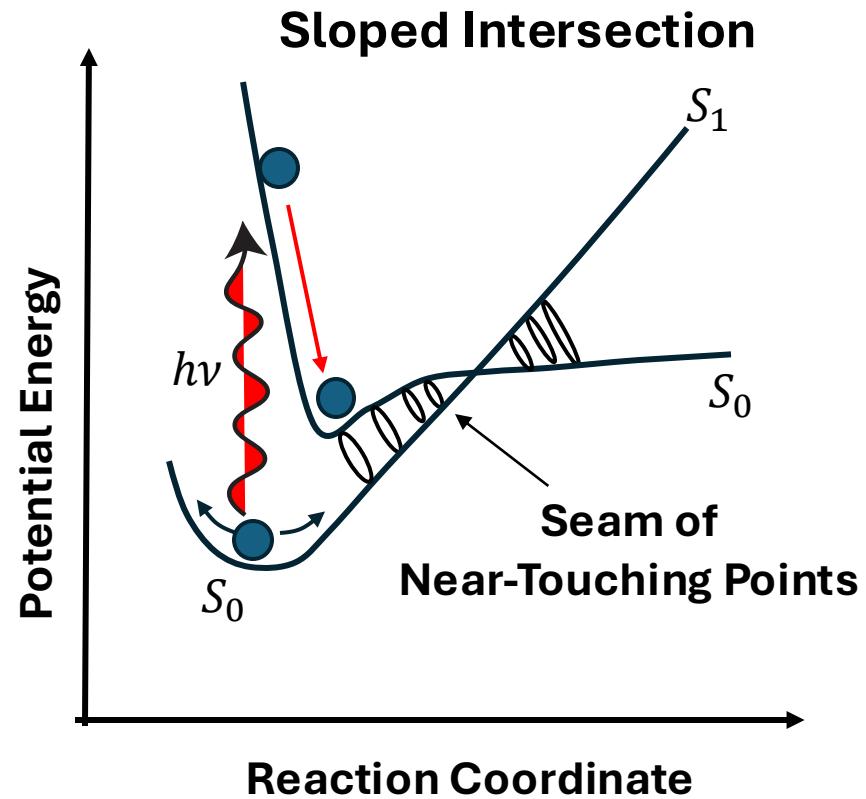
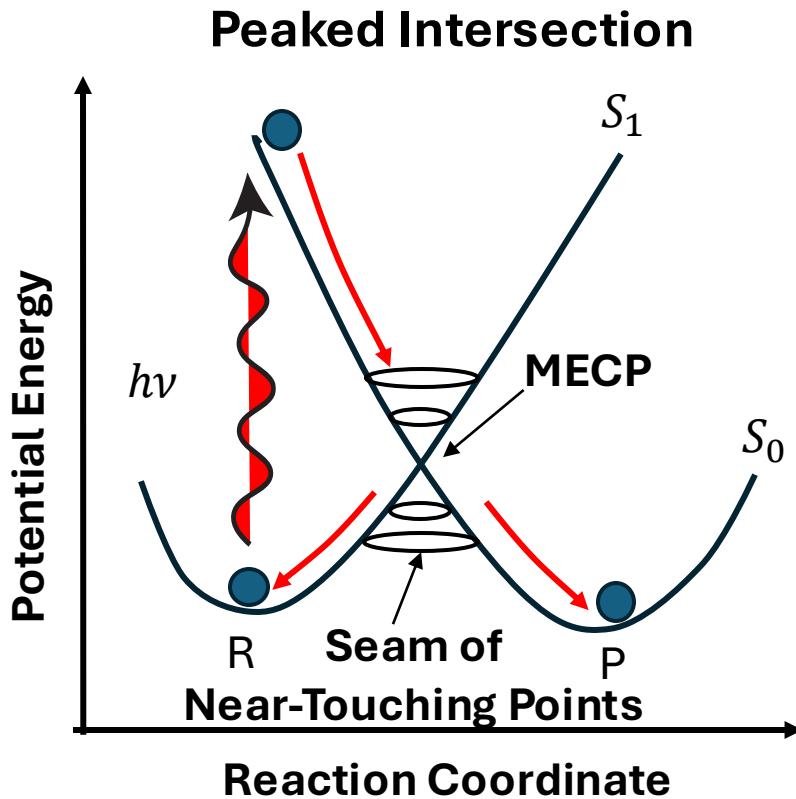
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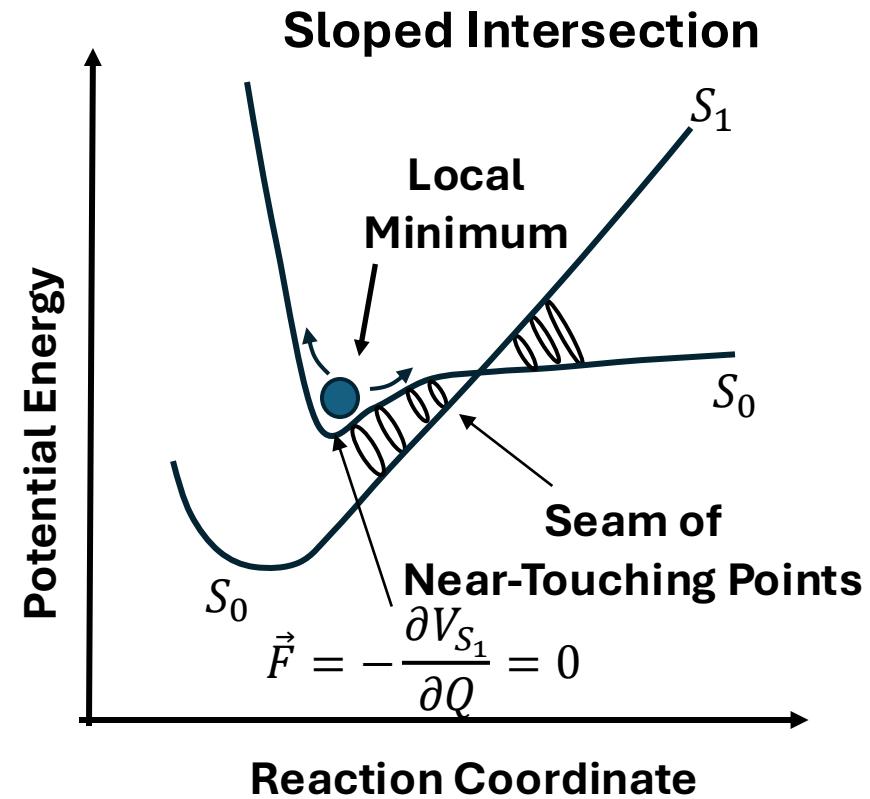
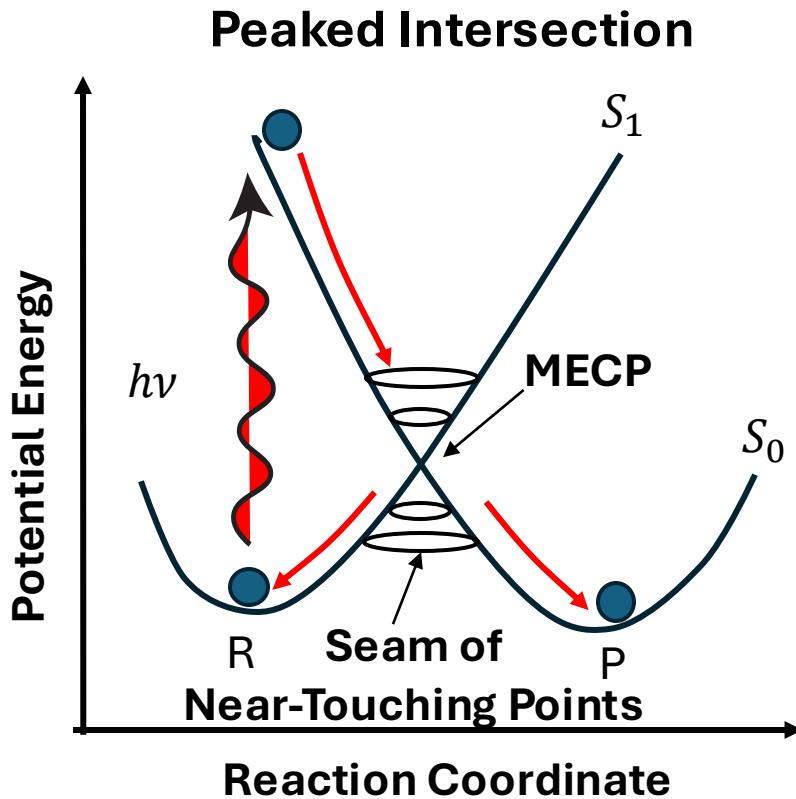
Fantastical excited state minimum energy configurations
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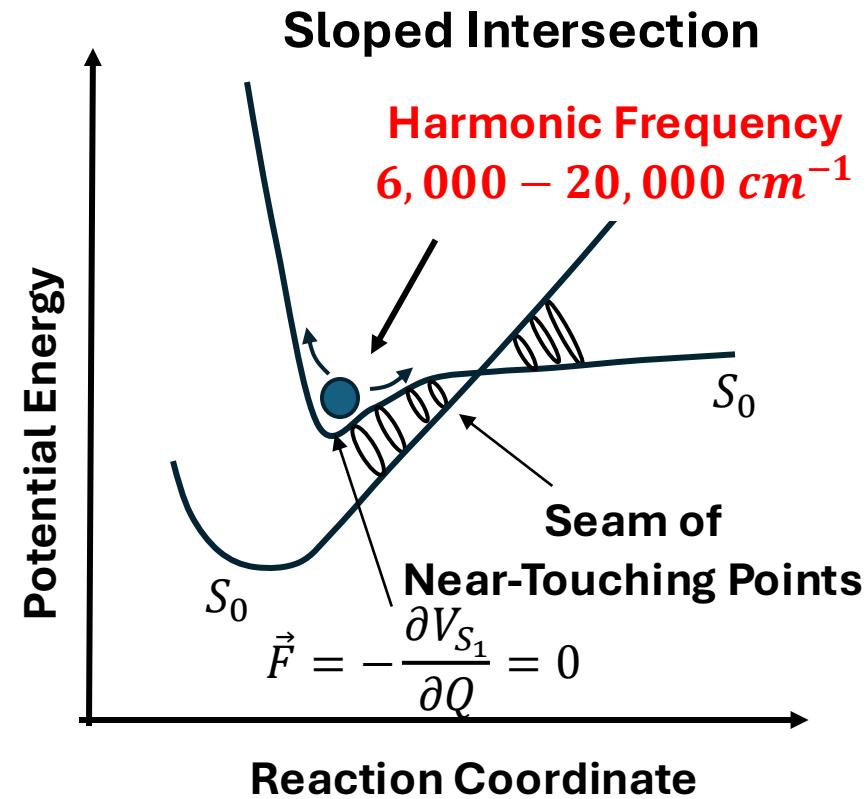
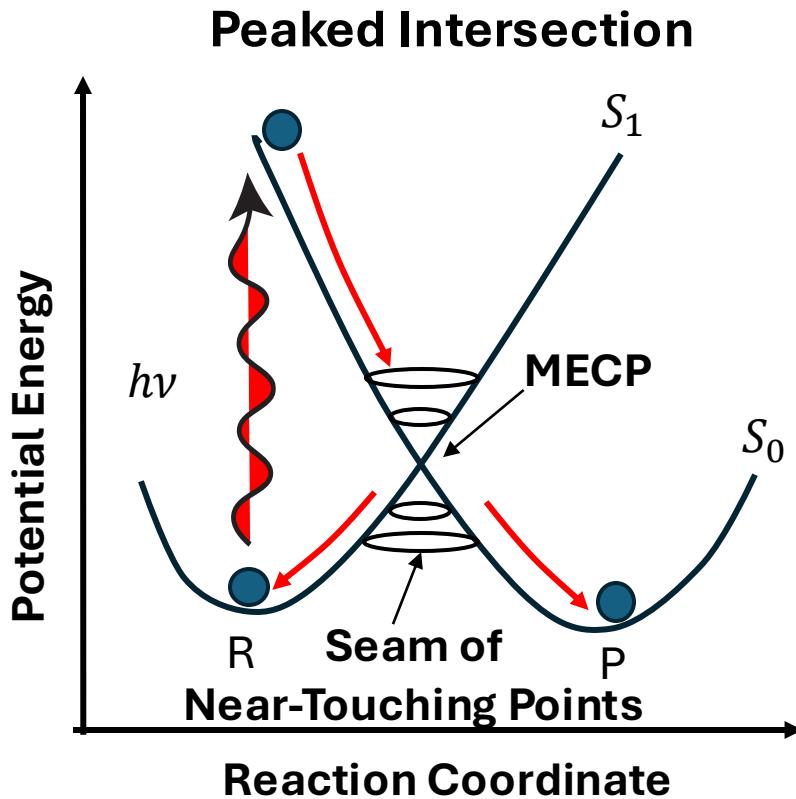
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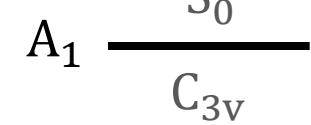
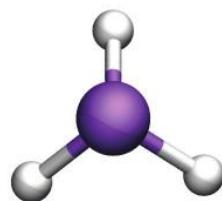
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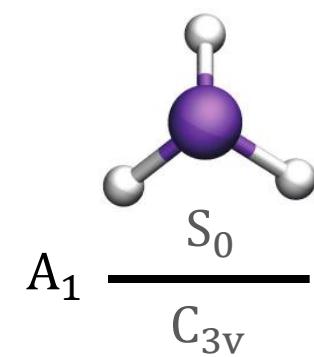
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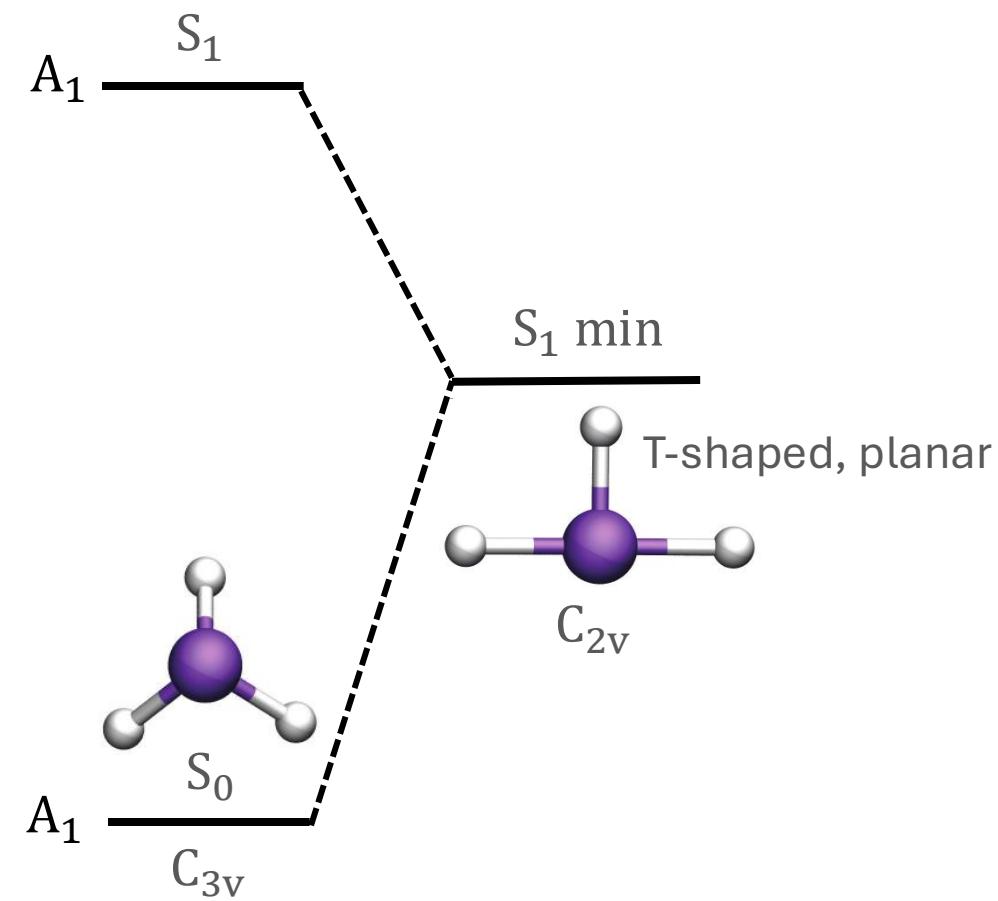
Phosphine (PH_3)



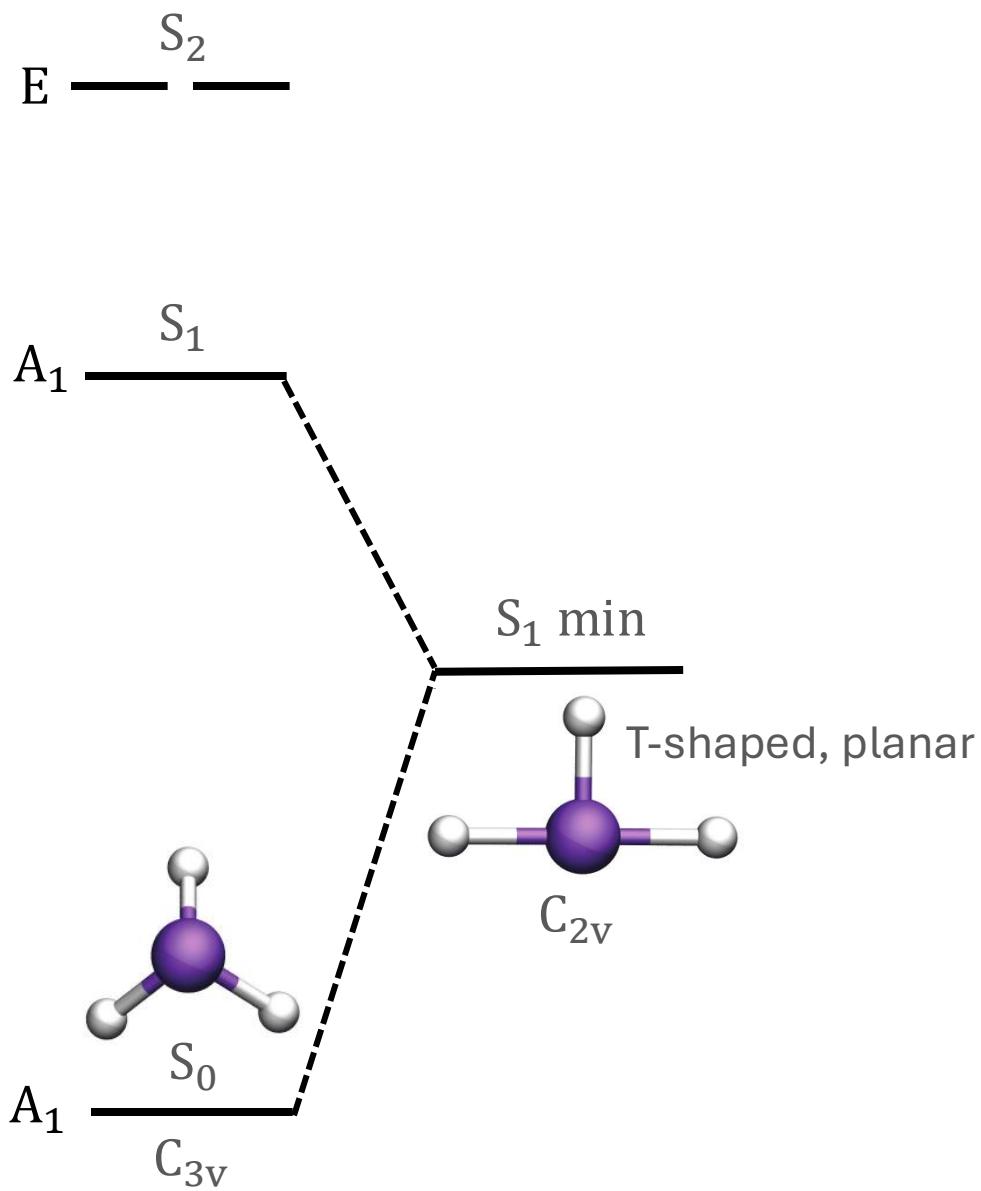
Phosphine (PH_3)



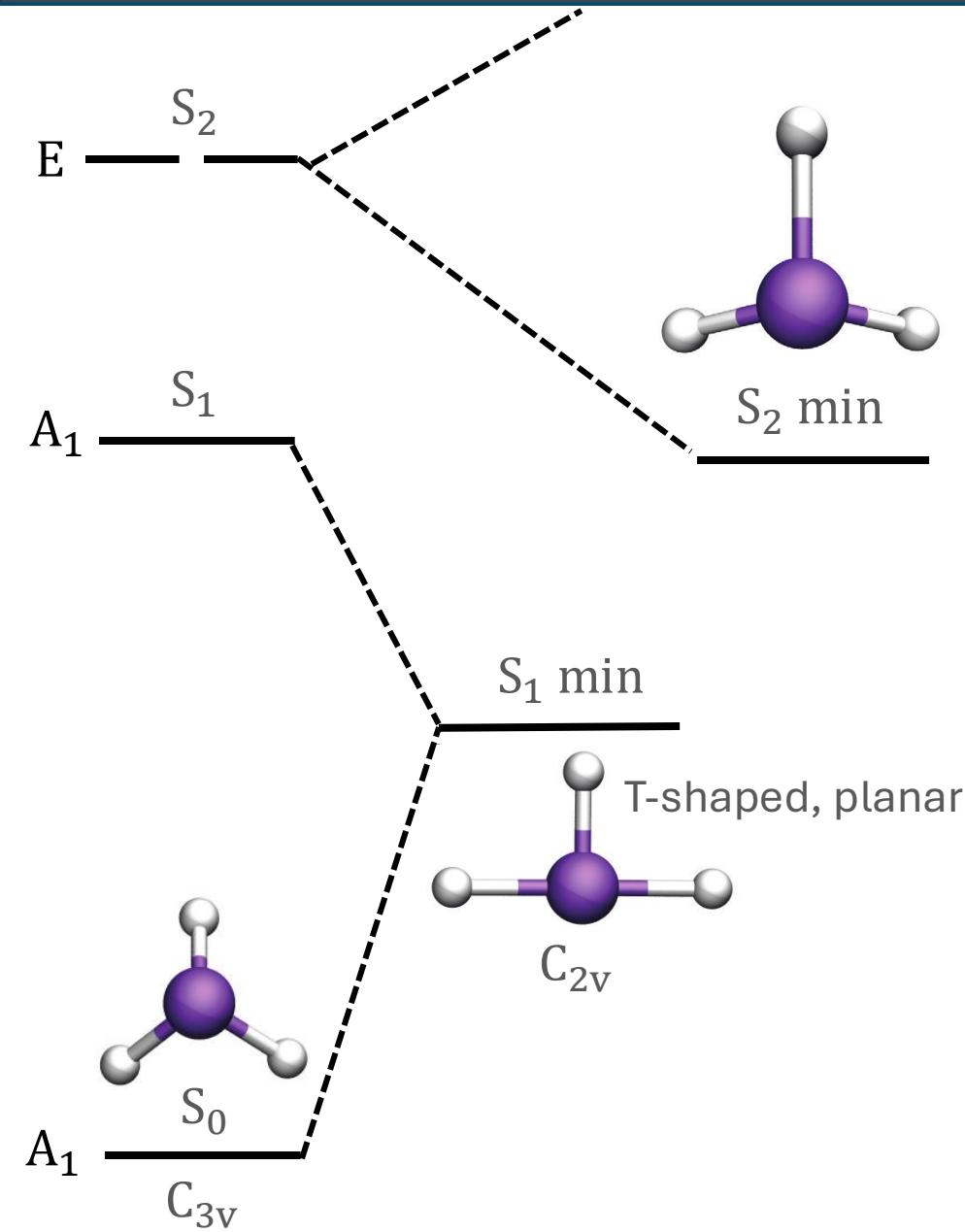
Phosphine (PH_3)



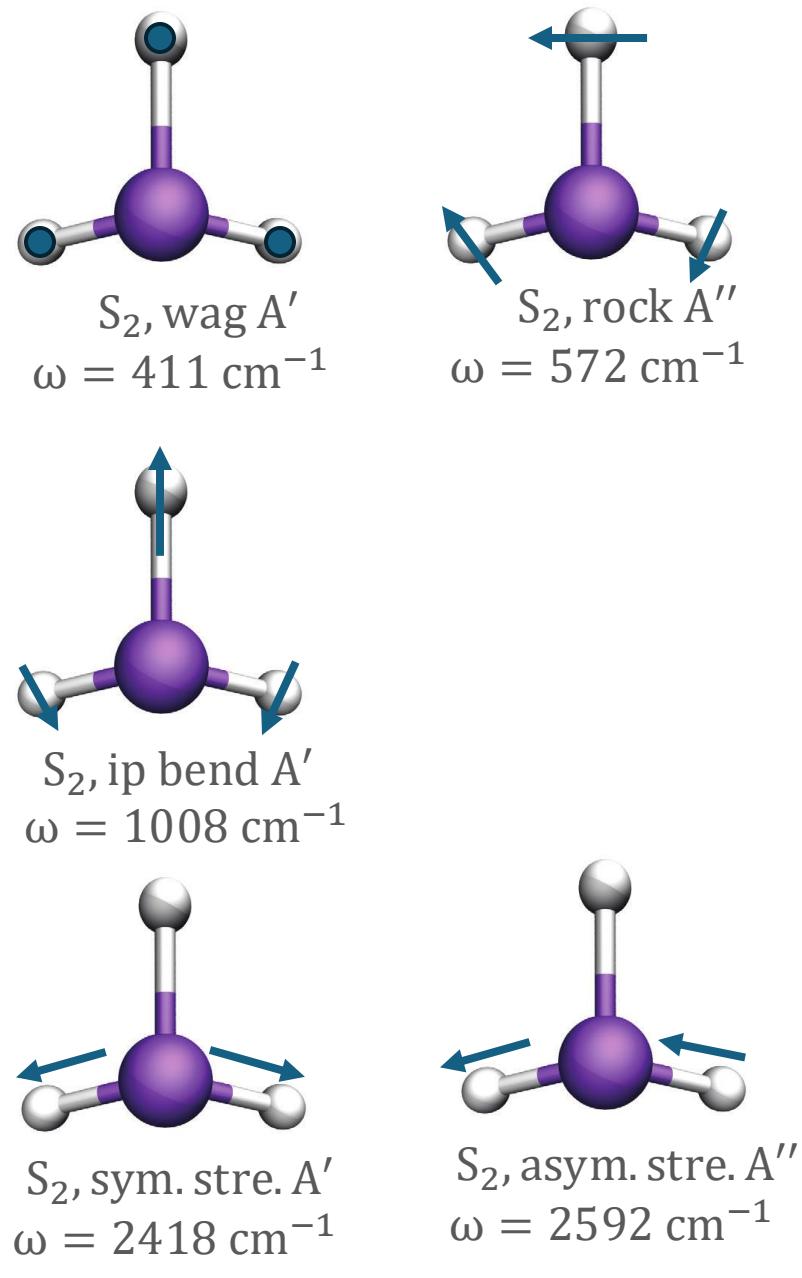
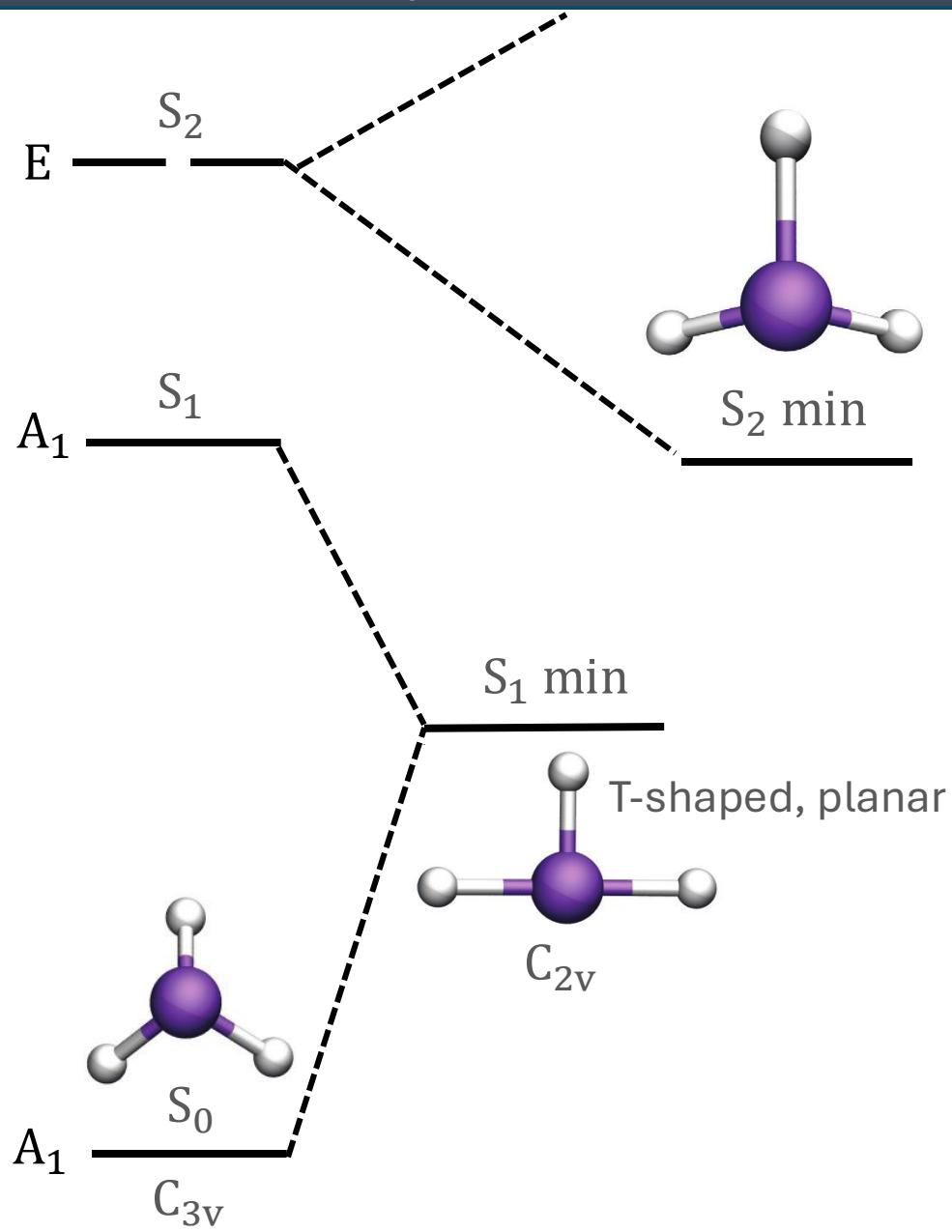
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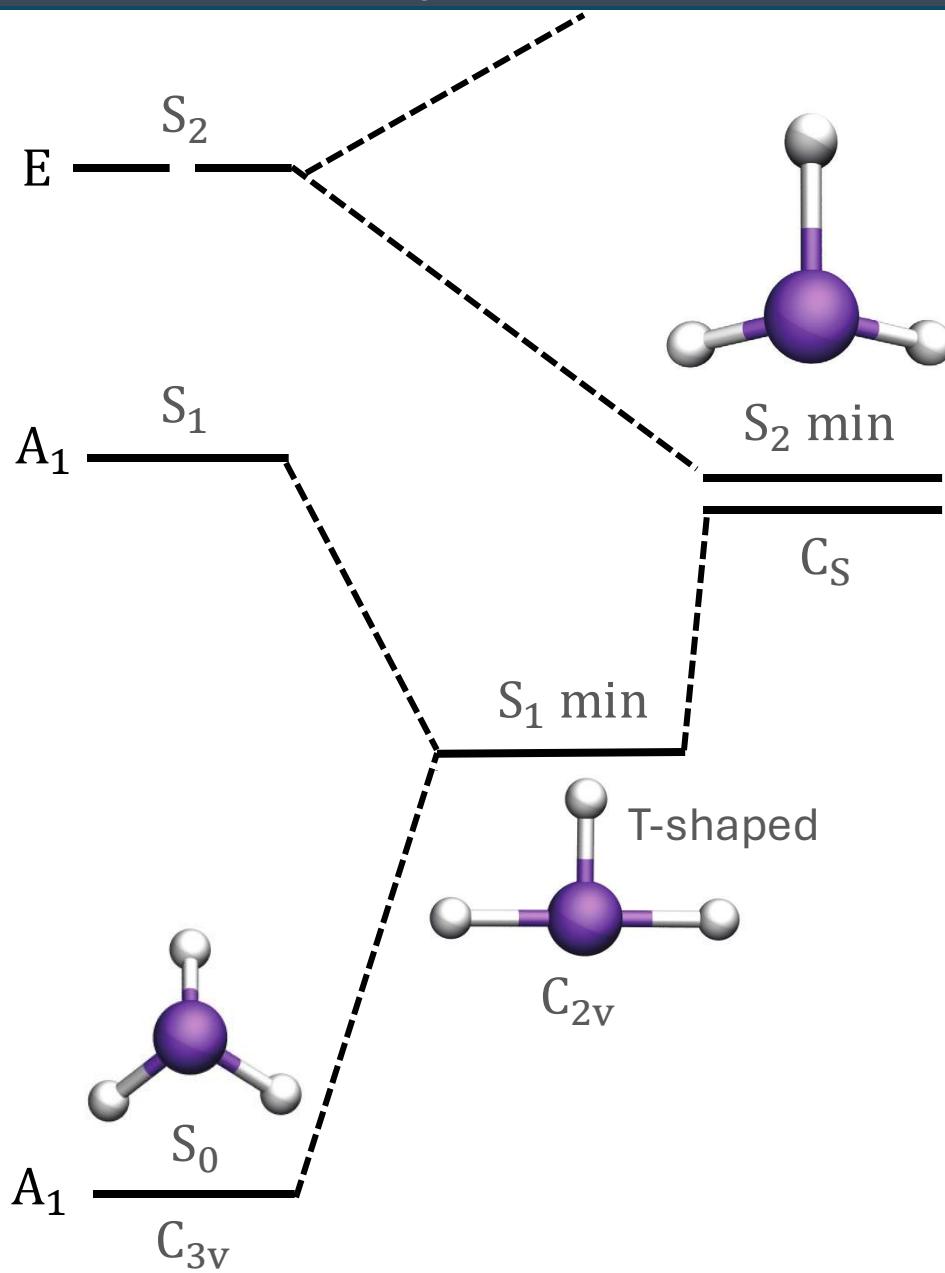
Phosphine (PH_3)



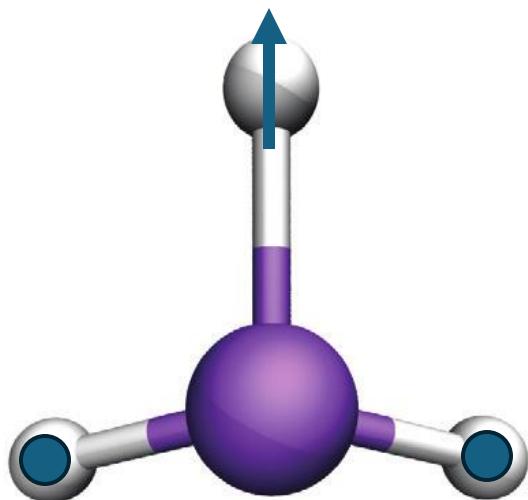
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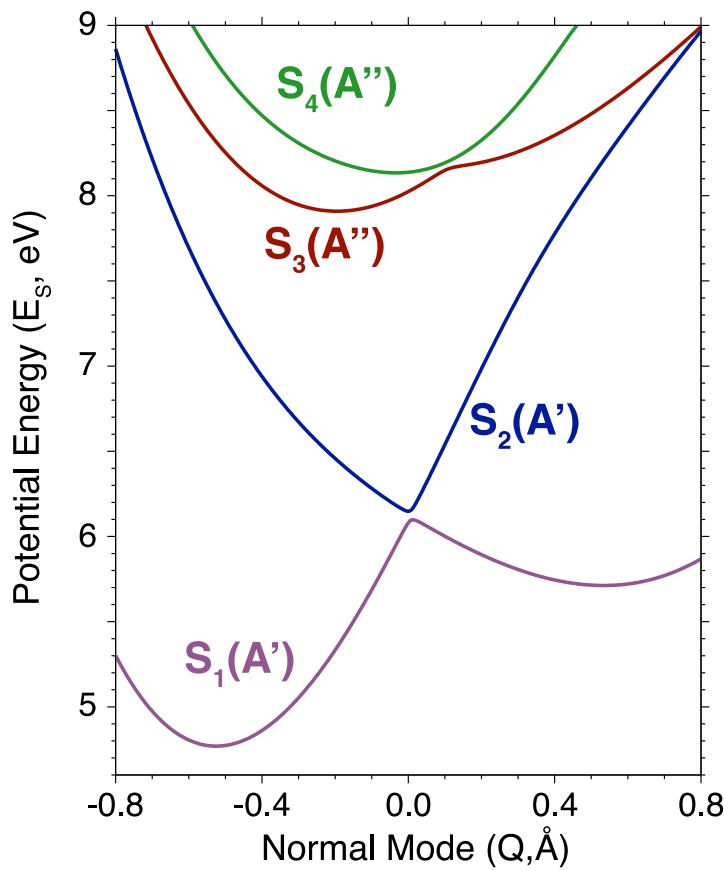
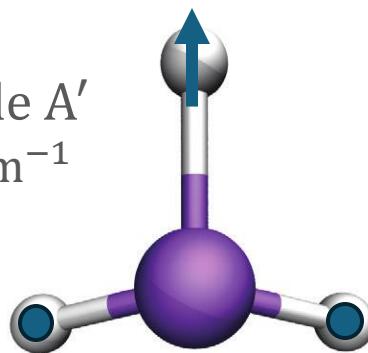
planarizes to form T-shaped configuration



S_2 , mega mode A'
 $\omega = 6884 \text{ cm}^{-1}$

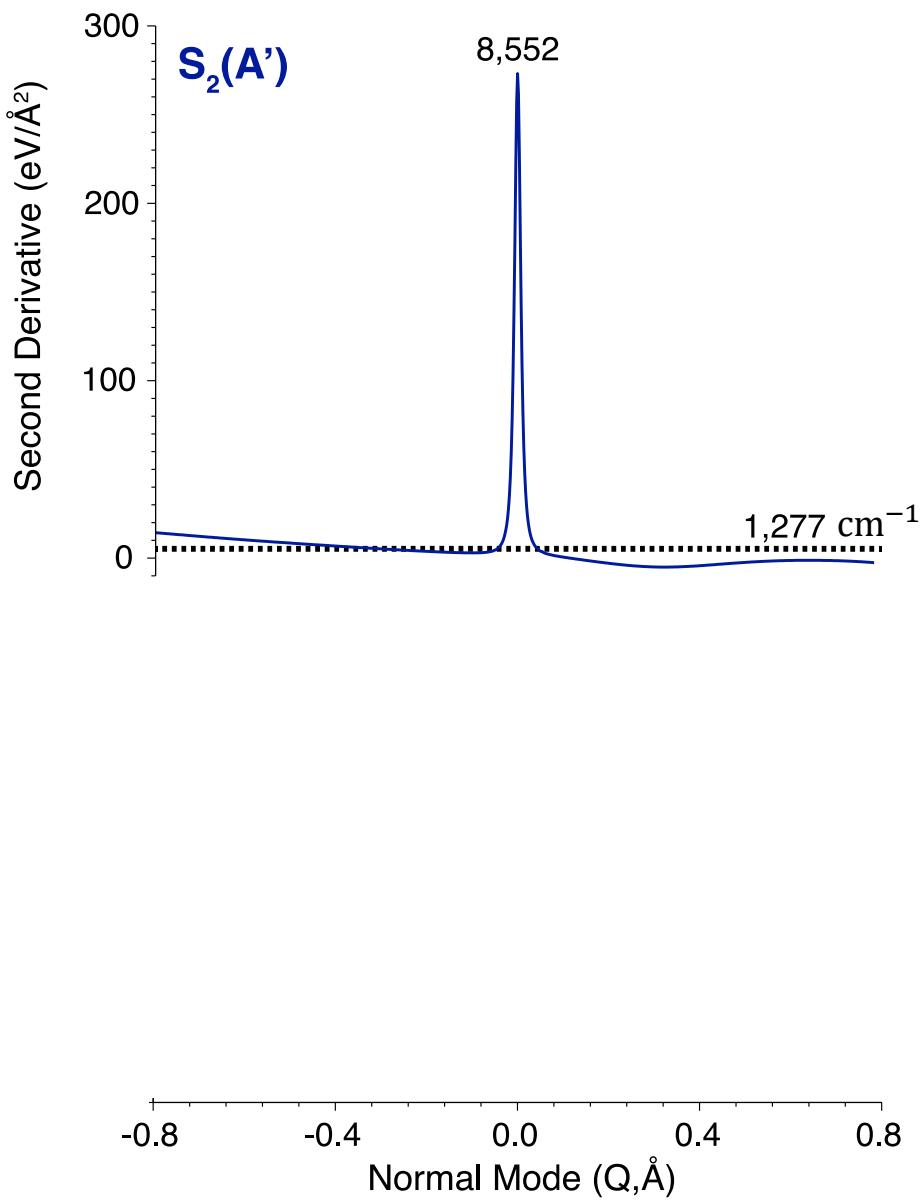
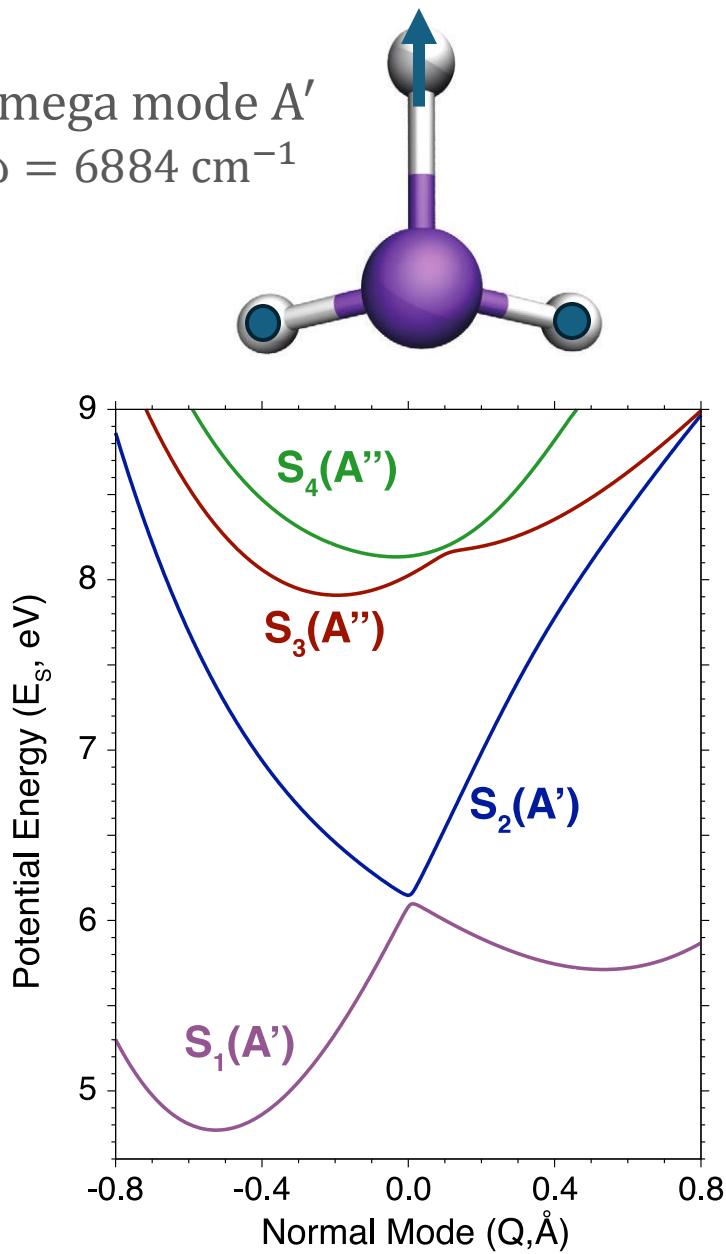
Phosphine (PH_3)

S_2 mega mode A'
 $\omega = 6884 \text{ cm}^{-1}$



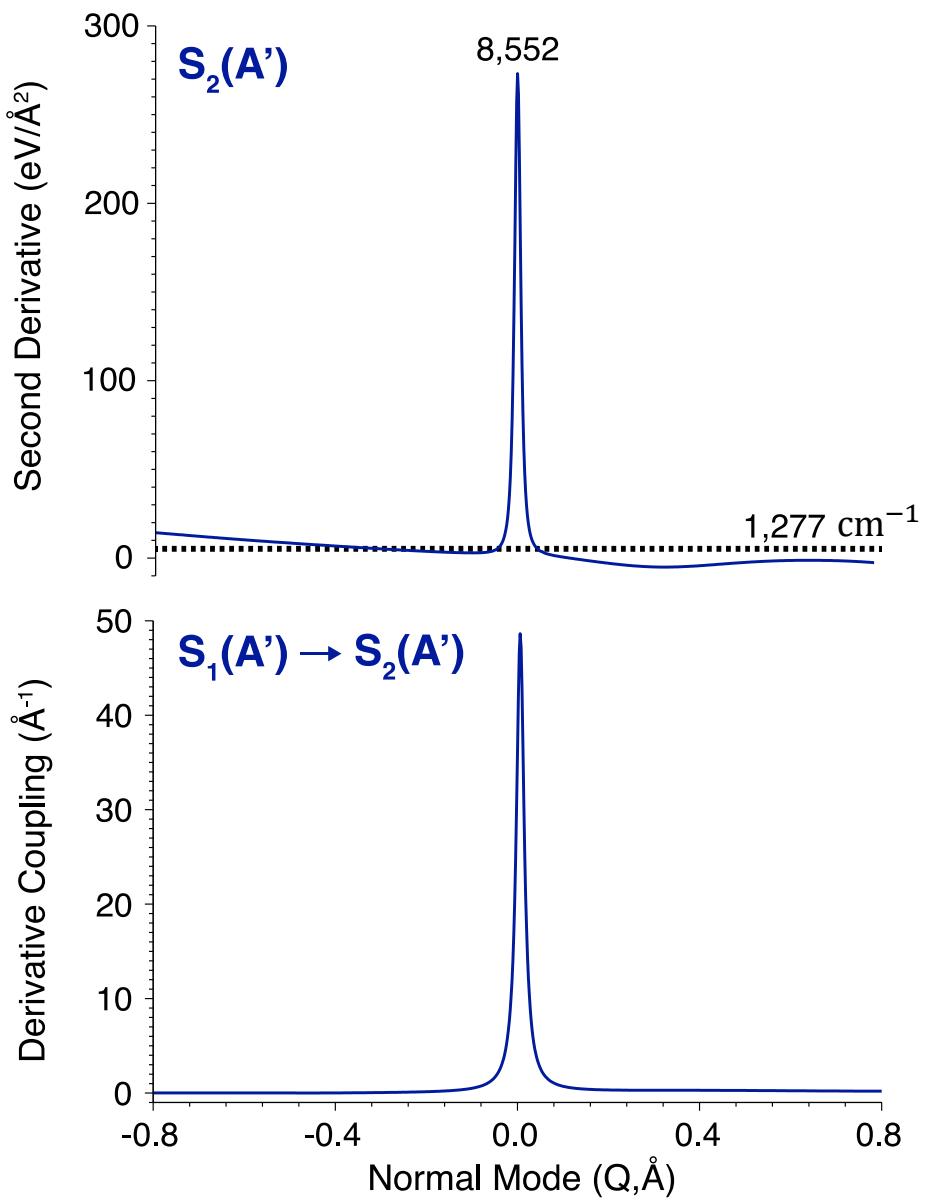
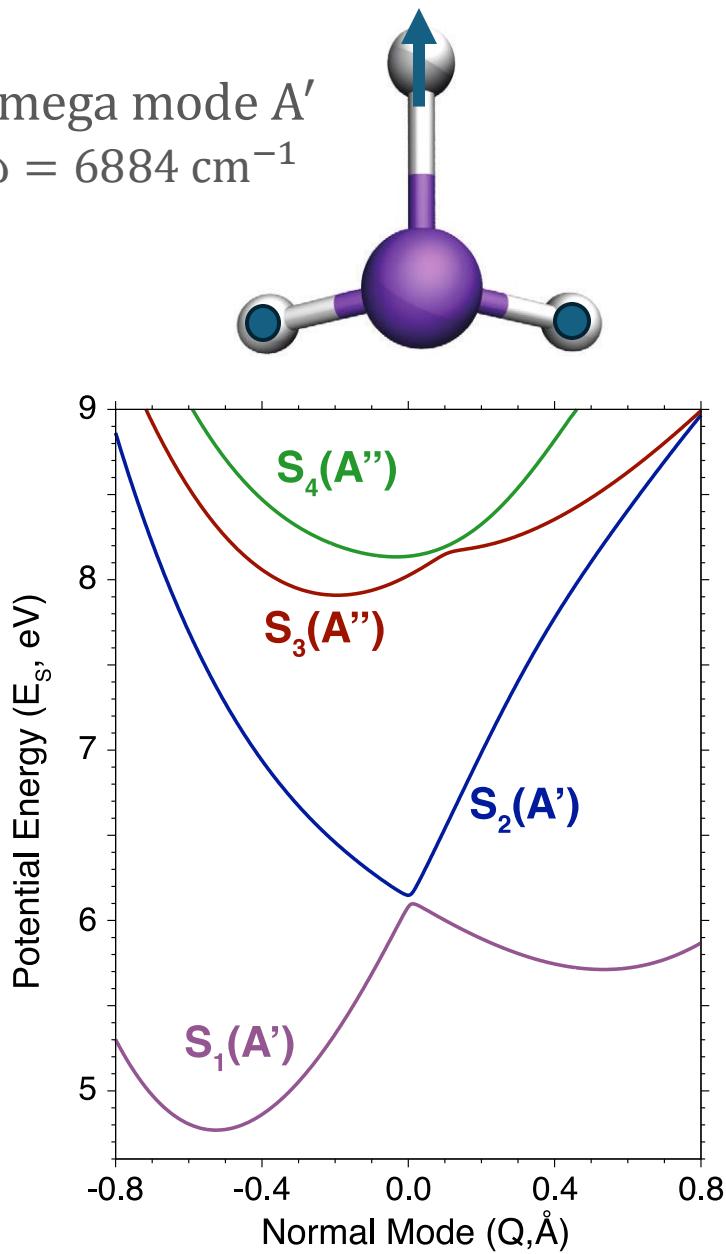
Phosphine (PH_3)

S_2 mega mode A'
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Phosphine (PH_3)

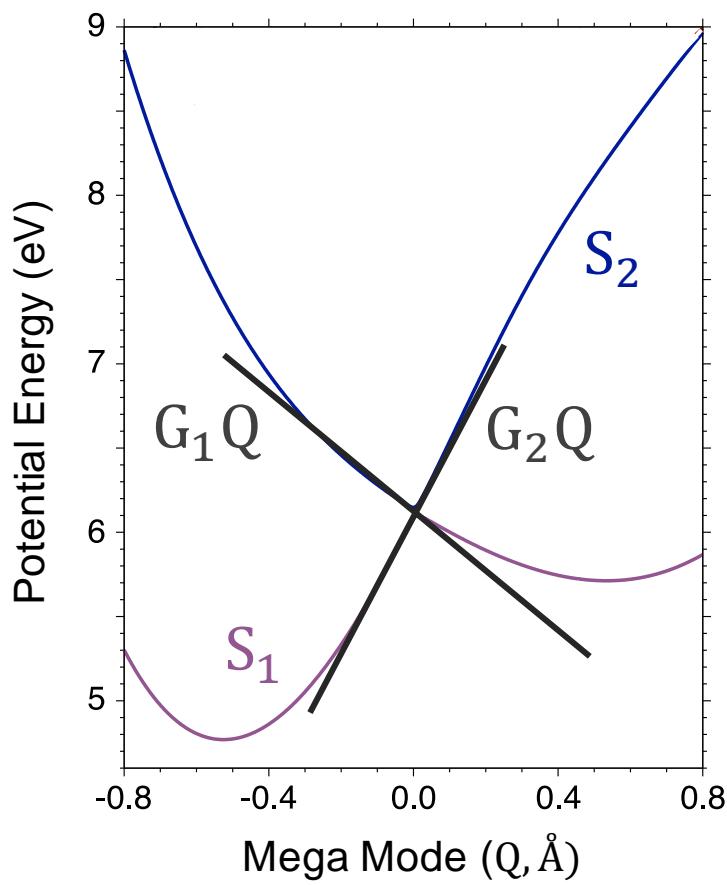
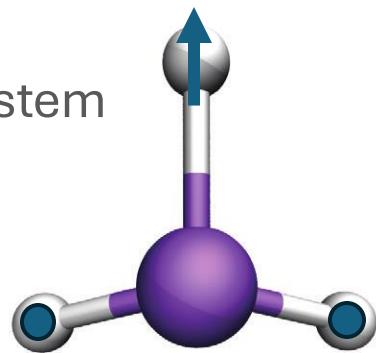
S_2 mega mode A'
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Phosphine (PH_3)

two-level system

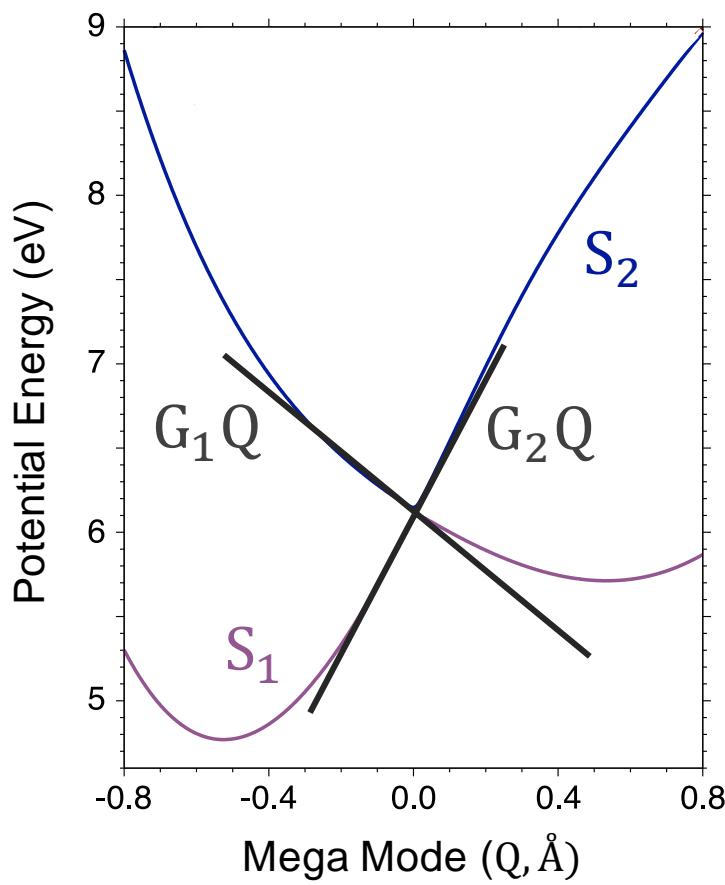
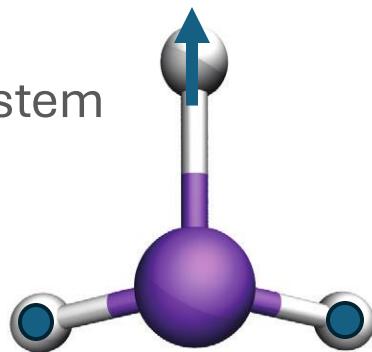
S_1 & S_2



Phosphine (PH_3)

two-level system

S_1 & S_2



Hamiltonian

$$H_{11}(Q) = G_1 Q$$

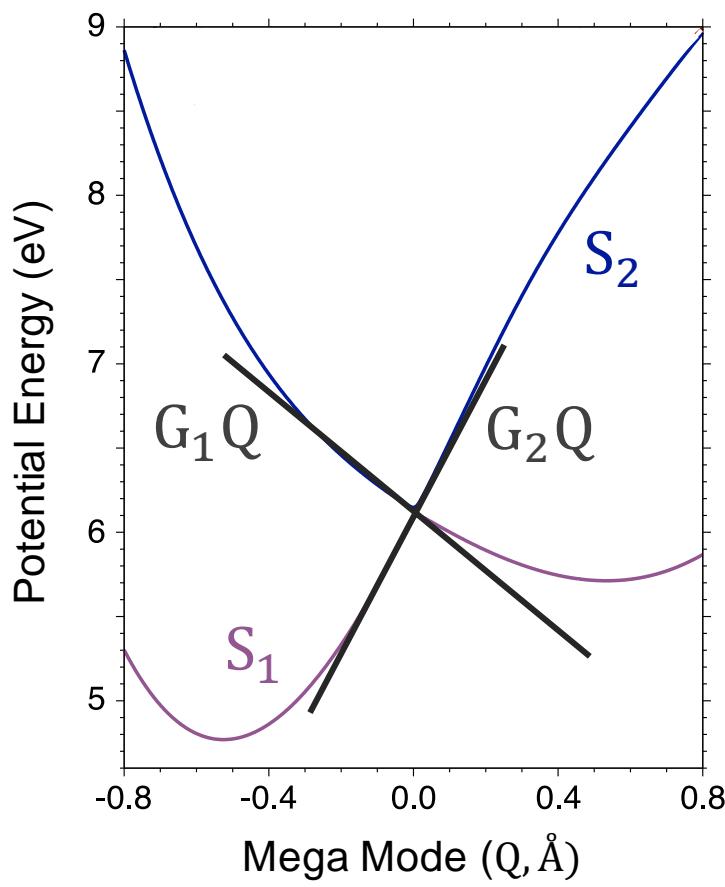
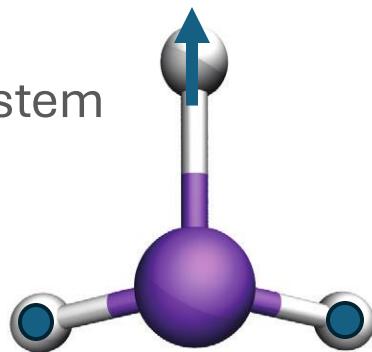
$$H_{22}(Q) = G_2 Q$$

$$H_{12}(Q) = \Delta$$

Phosphine (PH_3)

two-level system

S_1 & S_2



Hamiltonian

$$H_{11}(Q) = G_1 Q$$

$$H_{22}(Q) = G_2 Q$$

$$H_{12}(Q) = \Delta$$

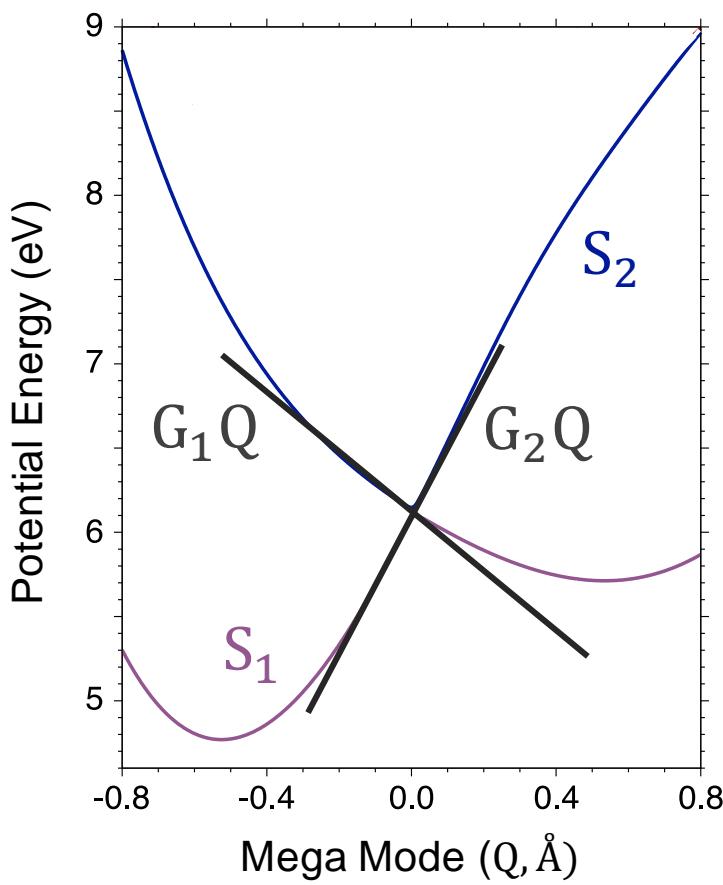
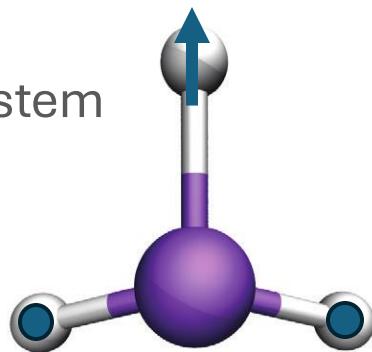
Eigenvalues

$$E_{\pm}(Q) = (G_1 + G_2)Q + \frac{1}{2}\sqrt{Q^2(G_1 - G_2)^2 + 4\Delta^2}$$

Phosphine (PH_3)

two-level system

S_1 & S_2



Hamiltonian

$$H_{11}(Q) = G_1 Q$$

$$H_{22}(Q) = G_2 Q$$

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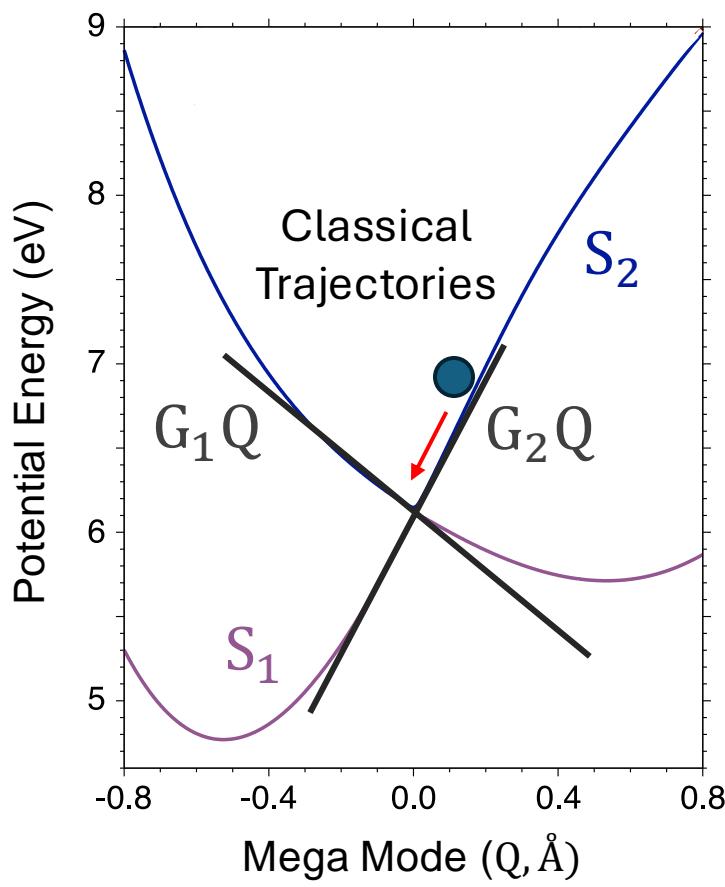
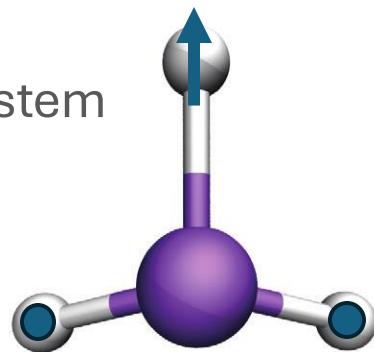
Second Derivative

$$\left. \frac{\partial^2 E_{+}(Q)}{\partial Q^2} \right|_{Q=0} = \frac{(G_1 - G_2)^2}{4\Delta}$$

Phosphine (PH_3)

two-level system

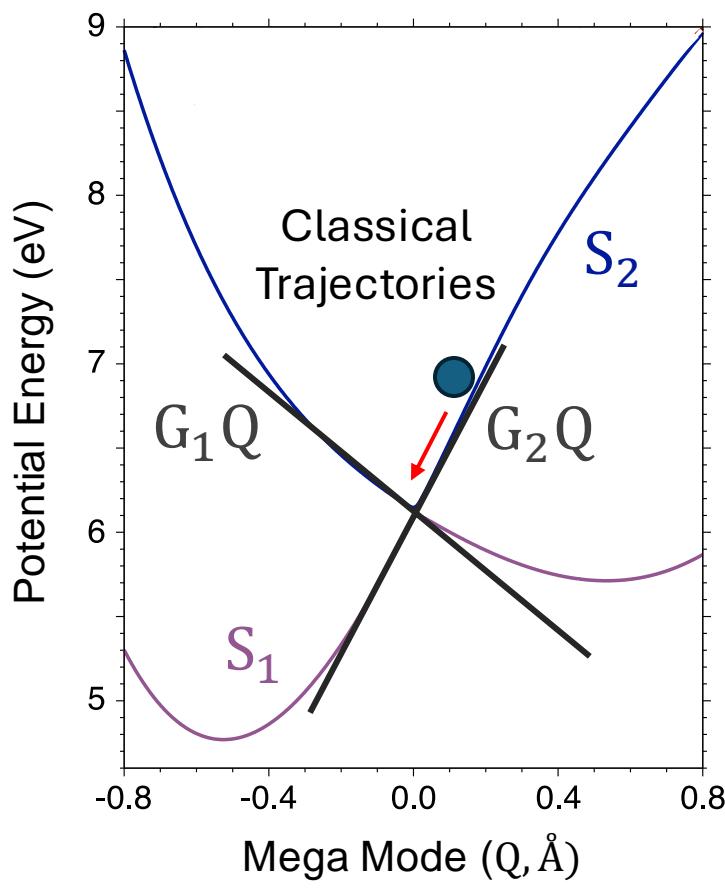
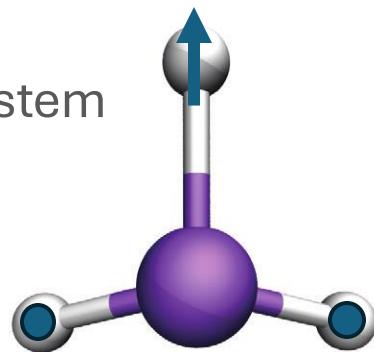
S_1 & S_2



Phosphine (PH_3)

two-level system

S_1 & S_2



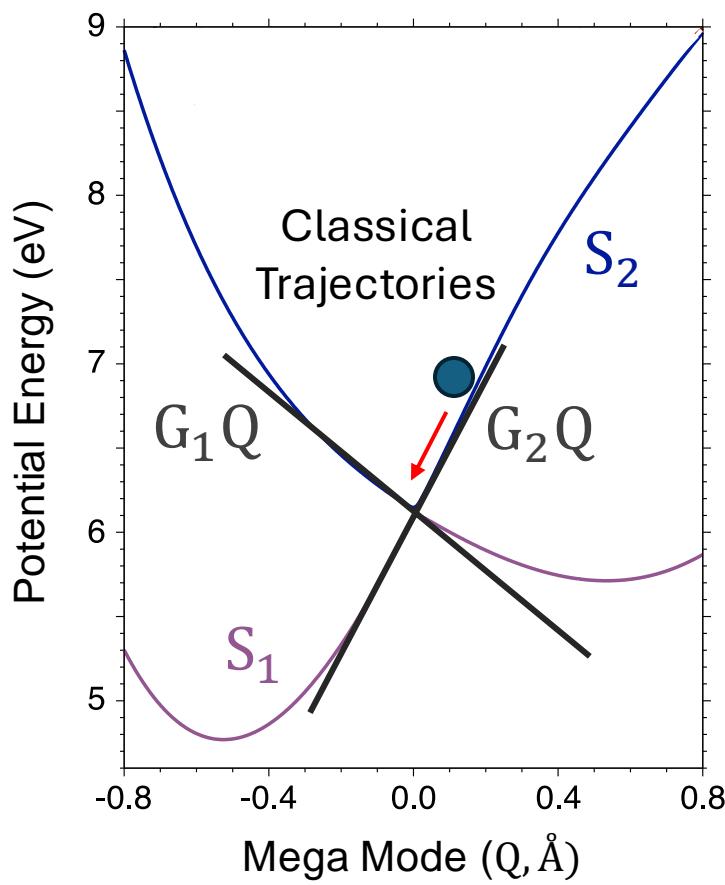
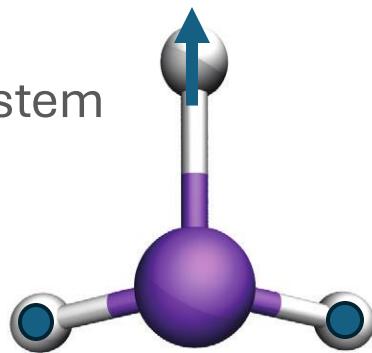
Landau-Zener Transition Probability:

$$P_{LZ} = 1 - \exp\left(-\frac{2\pi\Delta^2}{\hbar\dot{Q}|G_1 - G_2|}\right)$$

Phosphine (PH_3)

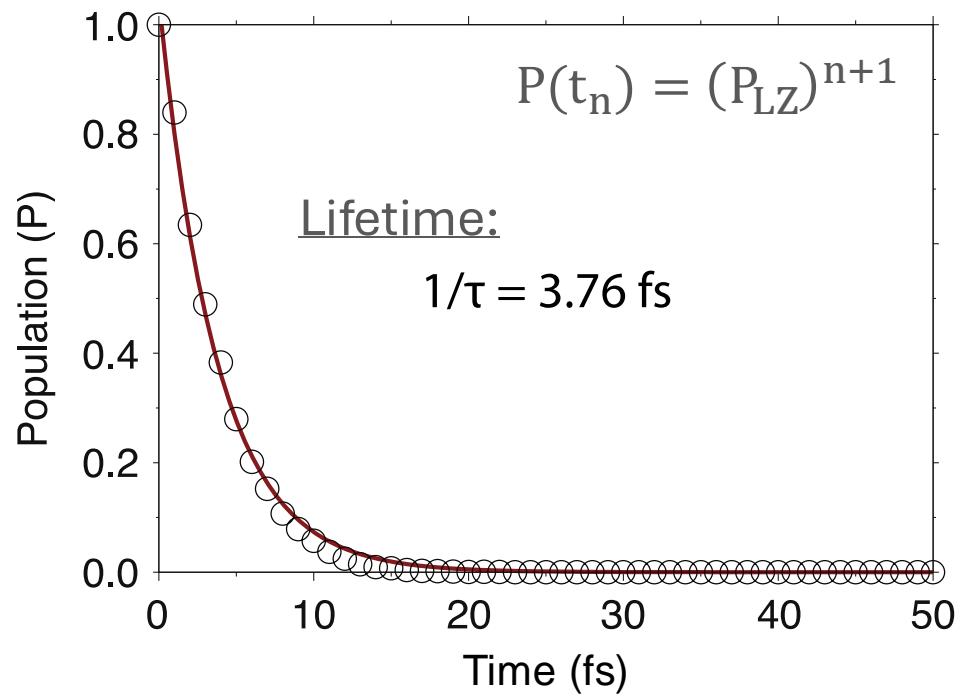
two-level system

S_1 & S_2



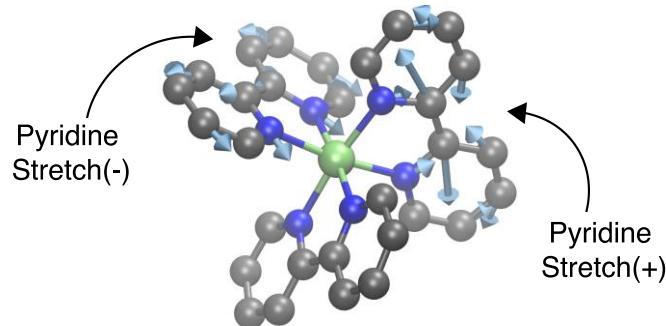
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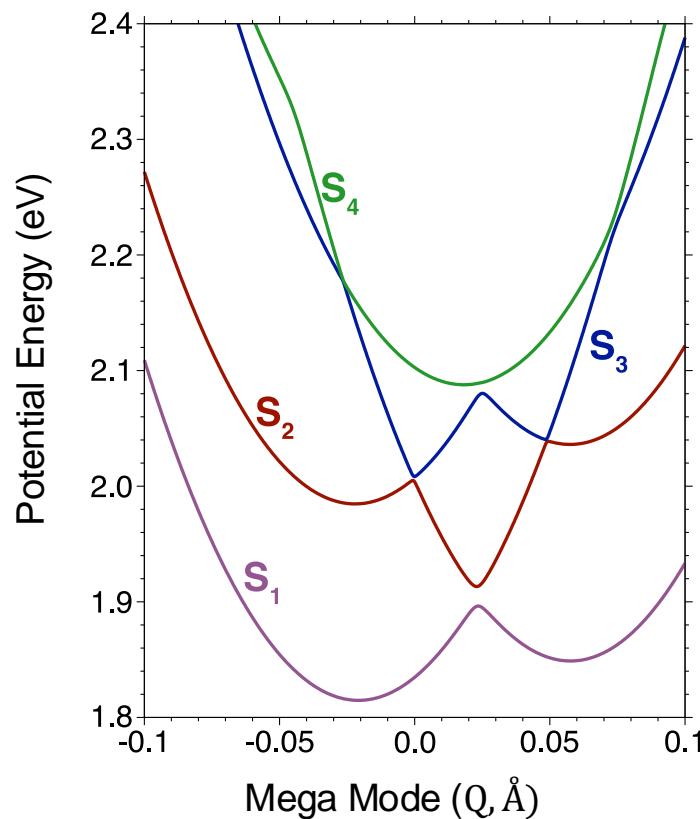
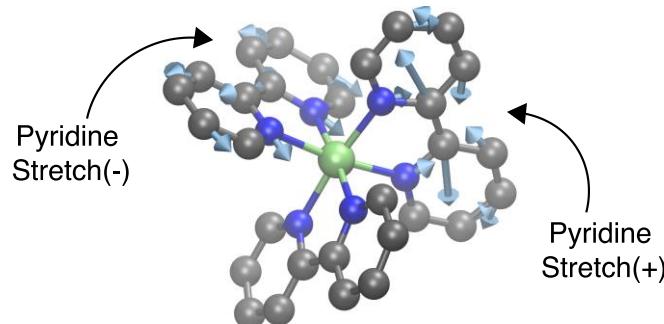
Solar Energy Catalyst

tris(2,2'-bipyridine)ruthenium(2+)



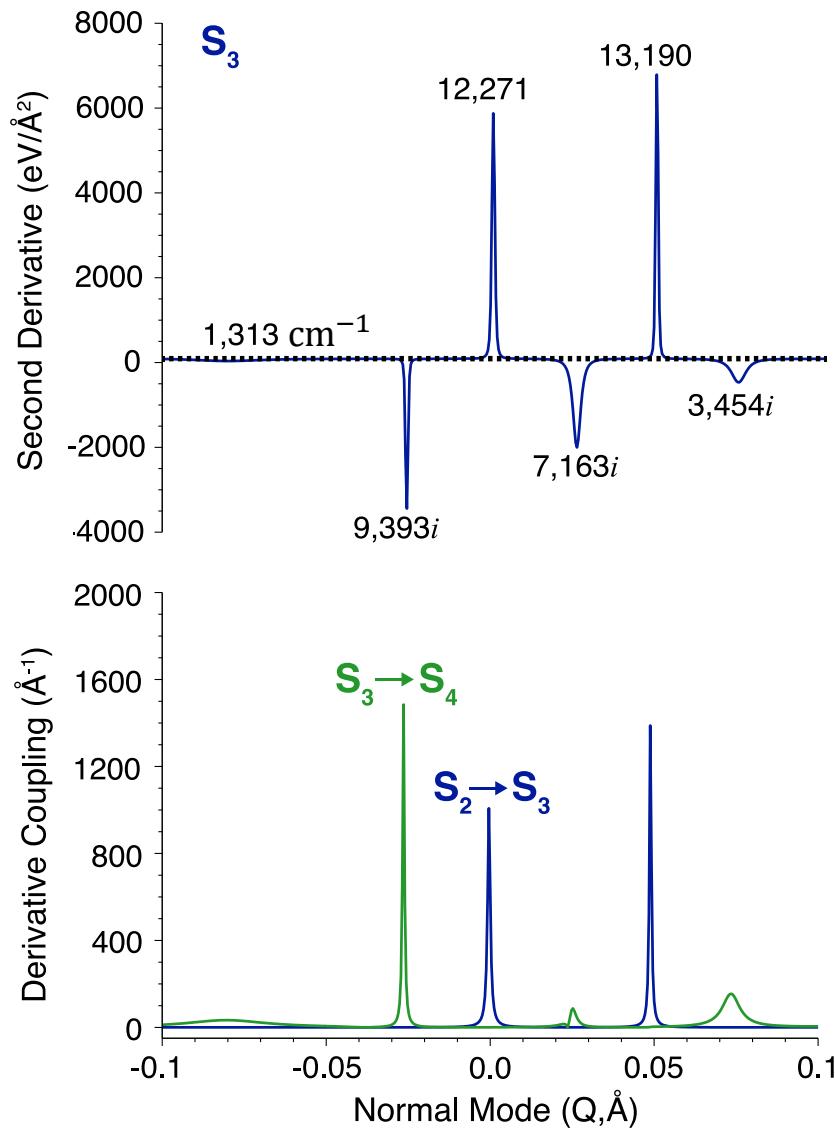
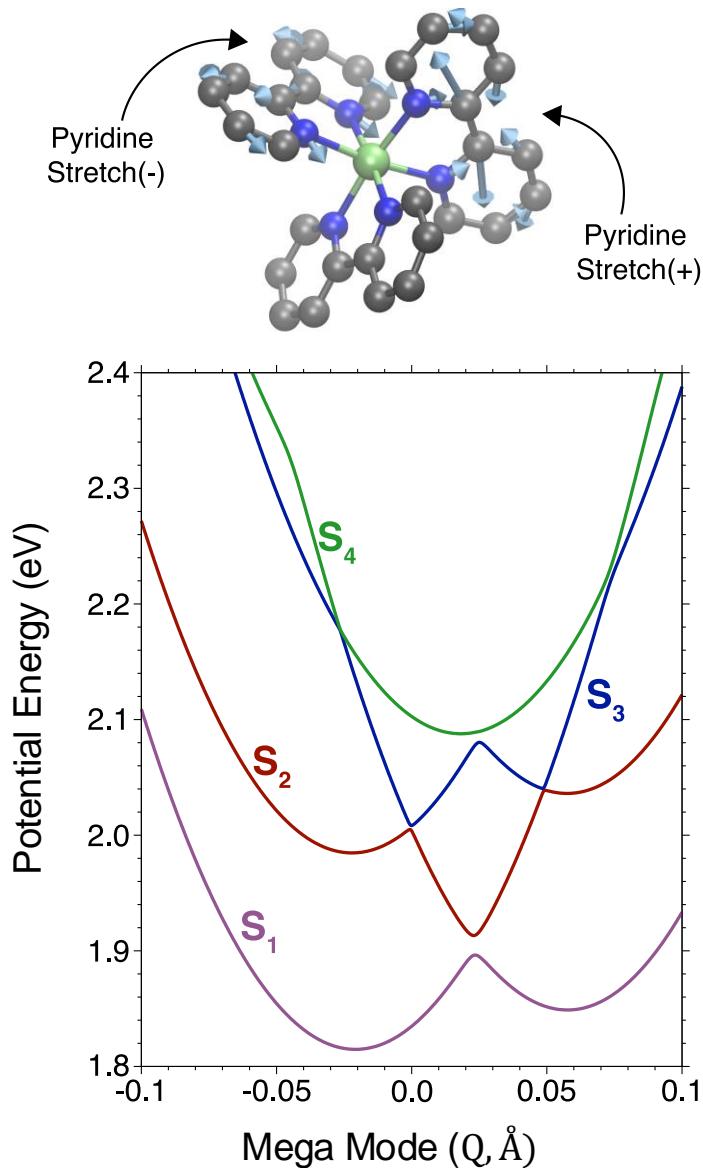
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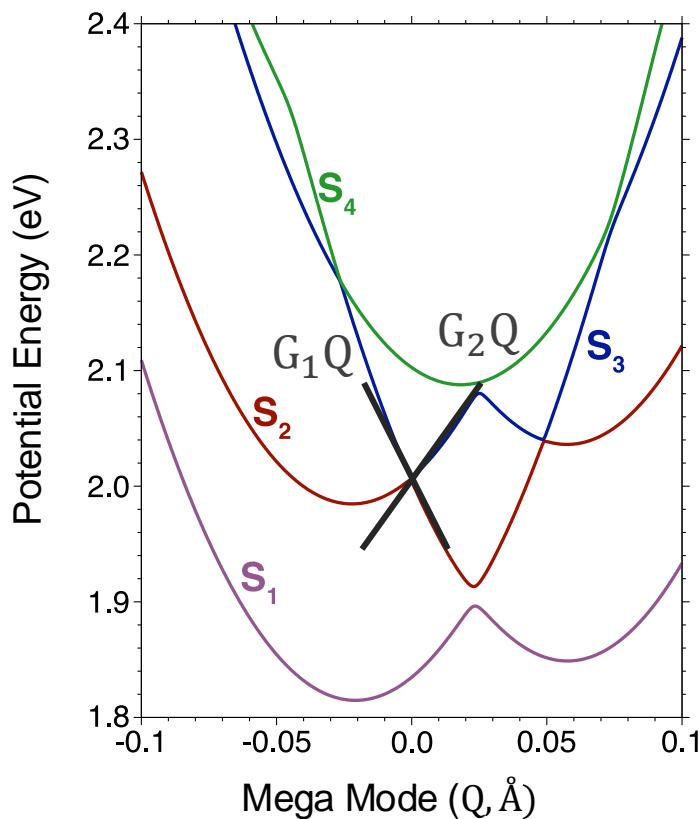
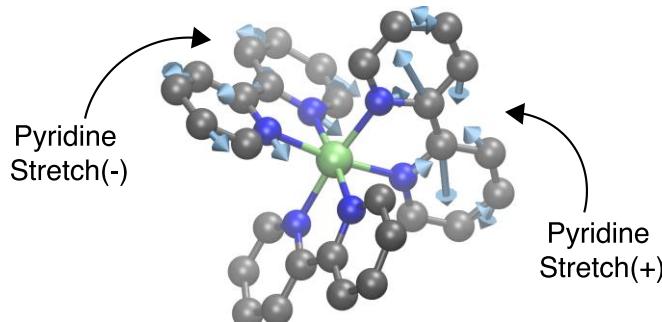
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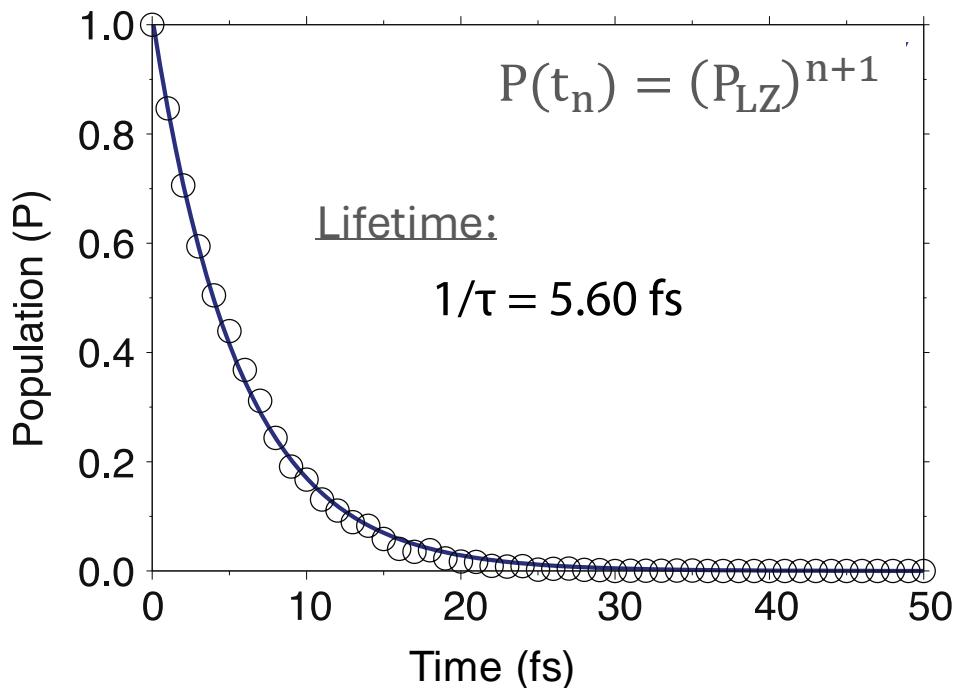
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Acknowledgments

Martin Head-Gordon



Stephen J. Cotton



Bill Miller



Grant #: CHE-1856707



Contract #: DE-AC02-05CH11231



Juan E. Arias-Martinez
Sandia National Lab
"Fantastical Excited States"