

Theoretical Insight into CO₂ Capture and Conversion

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Acknowledgment

- ORNL



- **Jingsong Huang**
- **Syed Islam**
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- **David S. Sholl**

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- **Sonya Garashchuk**
- **Vitaly Rassolov**

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- **Jerry Bernholc**
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Spallation Neutron Source (SNS) & Center for Nanophase Material Science (CNMS)



This work was performed at the Center for Nanophase Materials Sciences, a U.S. Department of Energy Office of Science User Facility.

Molecular dynamics of nuclei and electrons

Parameterized force fields

Energy and forces
on molecules from
parameters

Molecules moved:
Newton's laws

(MM)

Born-Oppenheimer dynamics

(Time-independent
Quantum Mechanics)

Solve electronic
Schrödinger Eq.
(convergence) at nuclear
Configuration

$$\hat{H}\psi(r;t) = E\psi(r;t)$$

Nuclei propagated
from gradients
(classically)

(BOMD)

Time-dependent Quantum Mechanics

(electrons)

Electronic structure:
Quantum dynamics:

$$i\hbar \frac{\partial}{\partial t} \psi(r;t) = \hat{H}\psi(r;t)$$

Nuclei propagated
from gradients
(classically)

(QD-electrons)

Time-dependent Quantum Mechanics

(nuclei)

Electronic structure
or
force fields

Nuclei propagated
quantum dynamically

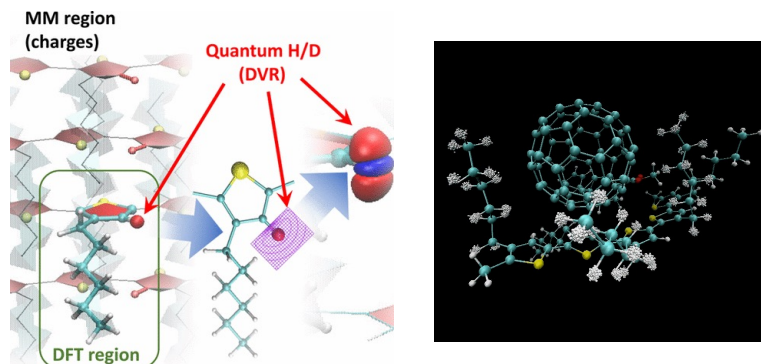
$$i\hbar \frac{\partial}{\partial t} \psi(R;t) = \hat{H}\psi(R;t)$$

(QD-nuclei)

Jacek Jakowski

Isotopic substitution & quantum nuclear effects

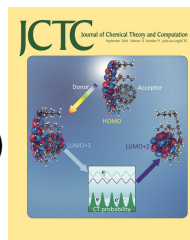
- development of new quantum methods
- deuterations
- electronic structure



Quantum trajectories

Collaborations:

- Jingsong Huang
- Bobby Sumpter
- Sophya Garashchuk (USC)
- Vitaly Rassolov (USC)

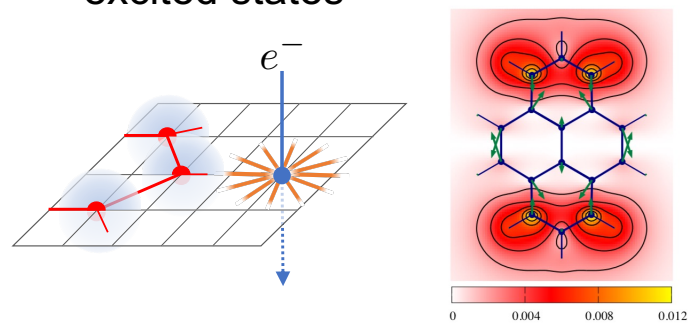


Selected publications:

- [1] *J. Chem. Theory Comp* **12**, 4487-4500. 2016
- [2] *J. Phys. Chem. Lett*, **8**, 4333-4340 (2017)
- [3] *Macromolecules*, (2021), 54, 3555-3584

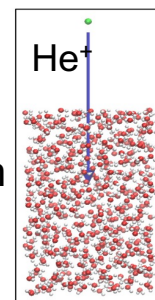
Electron/ion beam interactions with materials

- beam of energetic ions or electrons
- electron dynamics
- excited states



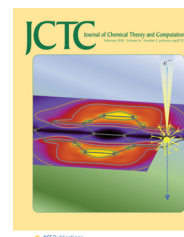
Collaborations:

- David Lingerfelt
- Ganesh Panchakepasan
- Jerry Bernholc (NCSU)



Selected publications:

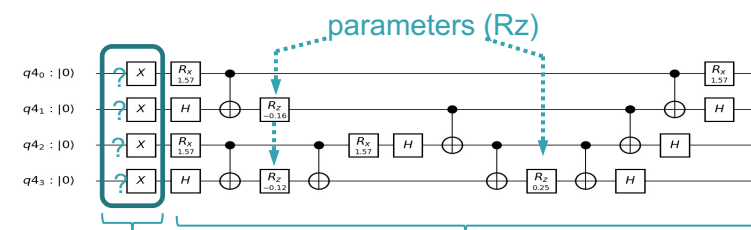
- [1] *Nanoscale*, **9**, 12949-12956 (2017)
- [2] *Science* **363**, 525 (2019)
- [3] *J. Chem. Theory Comp* (2020) **16**, 1200
- [4] *Theoretical Comp. Chem* (2022) **21**, 61



Quantum Computing

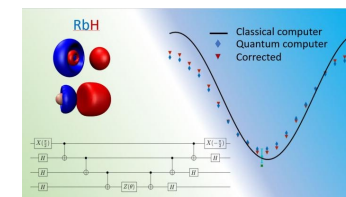
- quantum chemistry benchmarks
- small molecules
- many-body theory $|\psi(\theta)\rangle = e^{T-T^\dagger} |\psi_0\rangle$

$$E(\theta) = \langle \psi(\theta) | H | \psi(\theta) \rangle = \sum_{p,q} h_{pq} \langle \psi(\theta) | a_p^\dagger a_q | \psi(\theta) \rangle + \frac{1}{2} \sum_{p,q,r,s} h_{pqrs} \langle \psi(\theta) | a_p^\dagger a_q^\dagger a_s a_r | \psi(\theta) \rangle,$$



Collaborations:

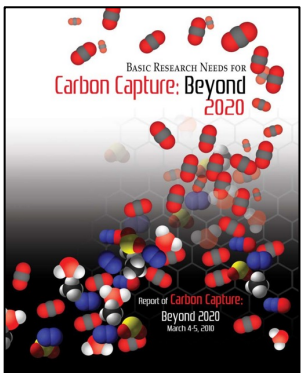
- Titus Morris
- Stephan Irle
- Gonzalo Alvarez
- Ryan Benink



Selected publications:

- [1] *NPJ-Quantum Inf.* (2019) **5**:99
- [2] *Adv. Quantum Techn.* (2021) **4**, 2100012
- [3] *ACM Trans. on Quant. Comput.* (2023), **4**, 27:1-14

Challenge: Closing Carbon Cycle

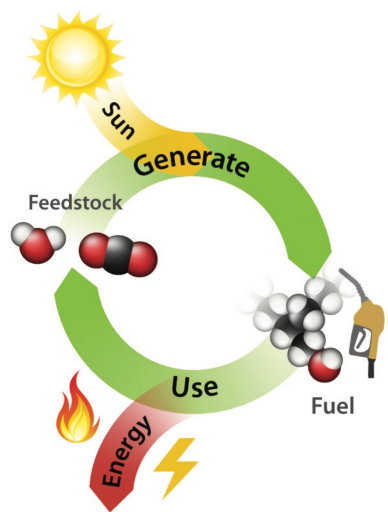


Key DOE questions:

How to balance release and capture of CO_2 to mitigate climate change?

- *Reduce emission of CO_2 (solar, wind nuclear energy, efficiency?)*
- *Carbon capture and storage*
- *Conversion of CO_2 to useful chemicals (solar liquid fuels)*

Solar to Hydrocarbons



Liquid solar fuels (DOE definition):

- *Energy dense chemicals at (or near) ambient conditions (methanol, hydrocarbons, oxygenated hydrocarbons, and nitrogen-containing compounds)*
- *Catalysis: sequential reduction processes.*

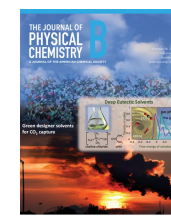
Advances require ***molecular-level understanding*** and control of the microenvironment ***around catalytic sites*** to direct reactions for key bond-making and bond-breaking steps

Overview

- **Part I. Quantum chemistry simulations of CO₂ capture** in reline, a prototypical deep eutectic solvent
 - ab initio dynamics
 - ground state, DFTB

[1] S. Z. Islam, [Ind. & Eng. Chem. Res. (2023) 62, 10,4455

[2] J. Jakowski, et al. J. Phys. Chem. B, (2023), 127, 8888

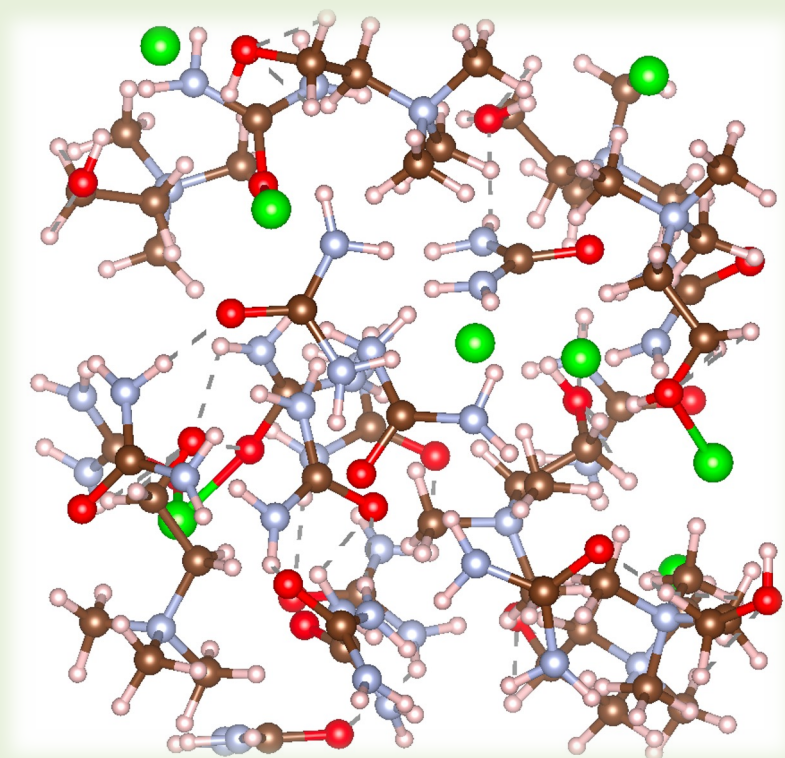


- **Part II. Towards modeling of CO₂ reduction via real time TDDFT**
 - theory, implementation, benchmarking
 - electronic excitation, non-equilibrium processes

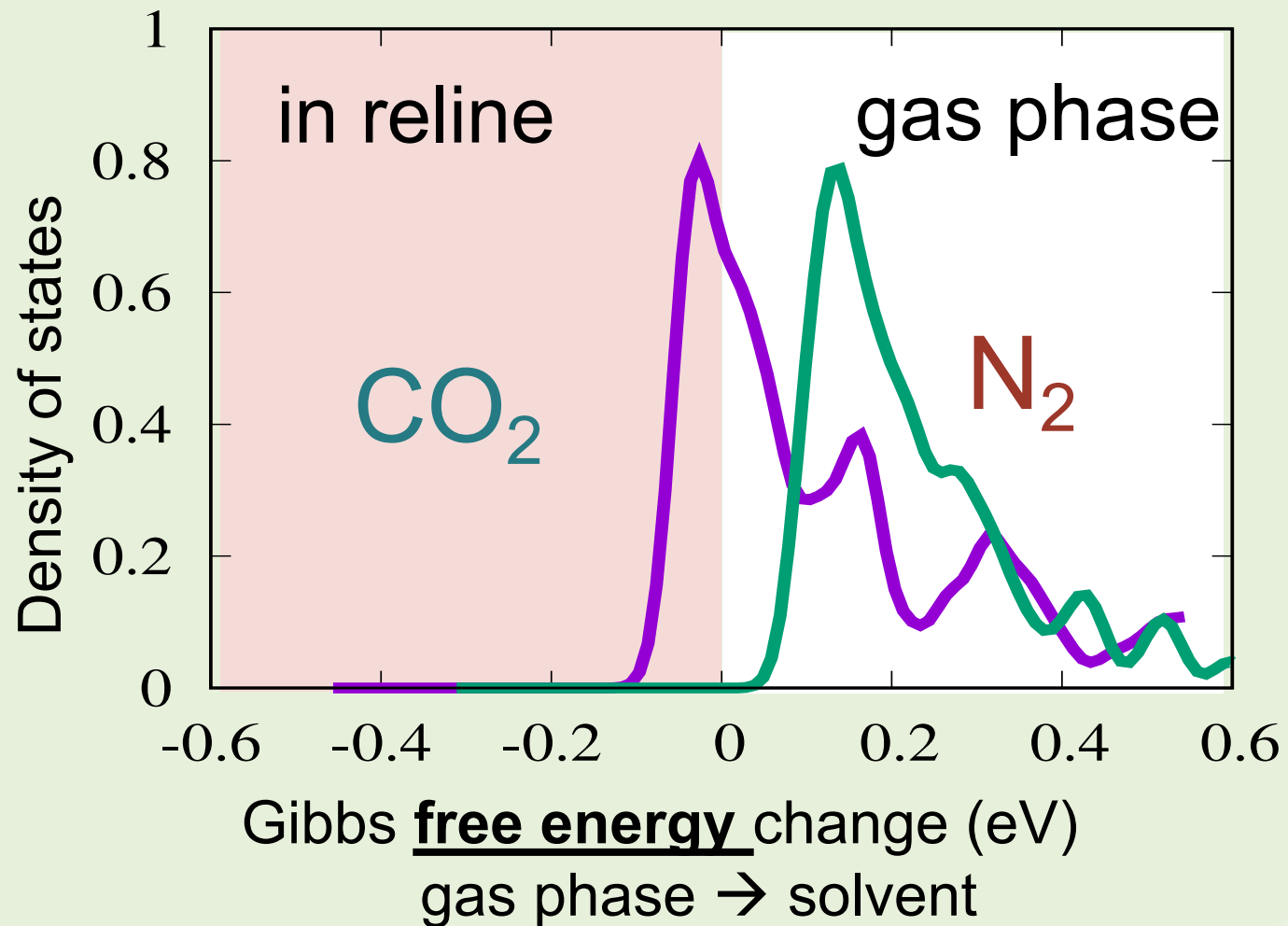
Part I. Quantum chemistry simulations of CO₂ capture in reline, a prototypical deep eutectic solvent

Part I. Summary of Results

Electronic and entropic effects lead to selective capture of CO_2 vs N_2 in reline (DES)



1:2 choline chloride/urea
(Deep Eutectic Solvent)



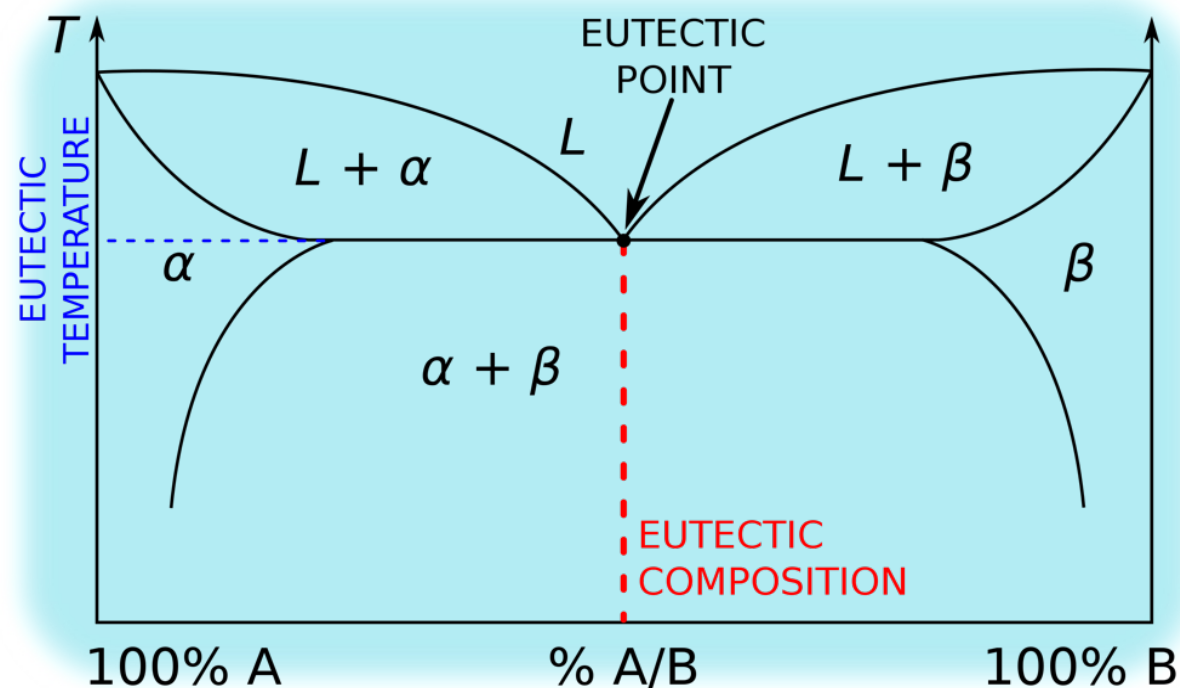
Quantum Chemical Simulations of CO₂ and N₂ Capture in Reline, a Prototypical Deep Eutectic Solvent

What are Deep Eutectic Solvents?

Eutectic systems

- A binary mixture of $A+B$ (example: metal alloys)
- Eutectic composition (L): homogeneous mixture at eutectic point
- Melting temperature: $T_L < T_A$ and $T_L < T_B$
- Non-eutectic composition:
 - mixture of L (liquid) and solid A or B

A phase diagram of binary mixture of $A+B$ (source: Wikipedia)



α	- solid A
β	- solid B
$L+\alpha$	- solid A + liquid L
$L+\beta$	- solid B + liquid L

Deep Eutectic Solvents (DES)

Properties

- Mixture of hydrogen bond donor (HBD) and acceptor (HBA)
- HBA : salts with cation acting as H-acceptor
- HBD : critical in suppressing melting Temp
- Tunable (modify HBA/ HBD)
- Cheap, biodegradable, low toxicity,
- Low vapor pressure

Example components

- Choline chloride
- Tetraethylammonium bromide
- Urea
- Acetamide
- Glycerol
- Phenol
- Lactose

Applications

- Pharmaceuticals
- Biocatalysis
- Separation
- Extraction

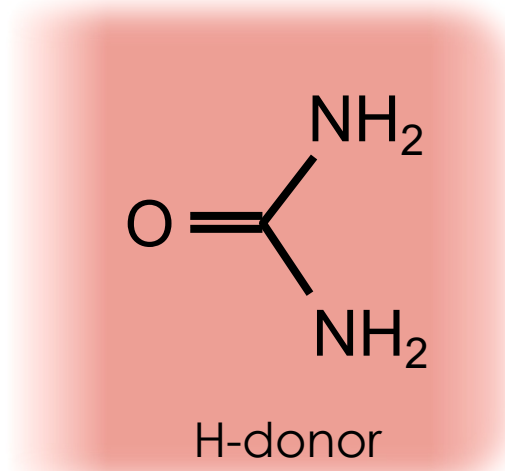
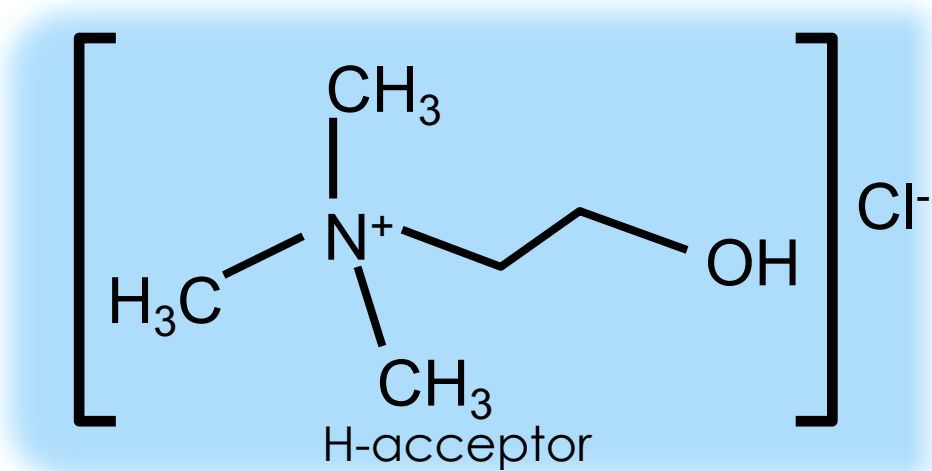
Reline as a Deep Eutectic Solvent

• Reline:

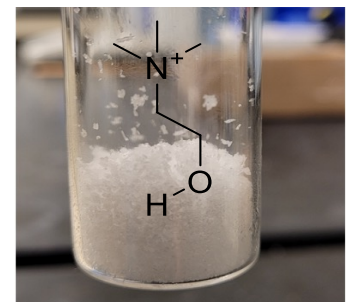
- choline chloride (HBA) + urea (HBD)
- 1:2 molar ratio

Melting Temperatures

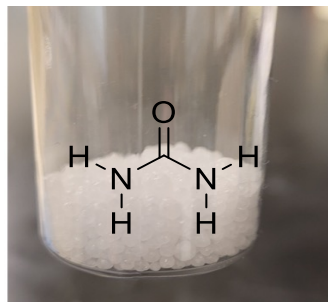
- Choline chloride: 302 °C
- Urea: 130 °C
- Reline: 12 °C



Choline chloride



Urea

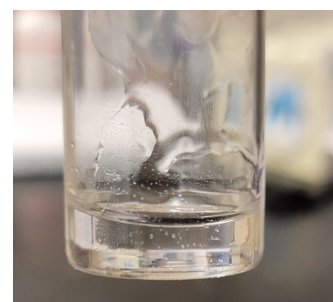


1:2
+

80°C



Reline



Properties:

- Thermally stable
- Non-toxic
- Biodegradable
- Negligible vapor pressure
- Inexpensive

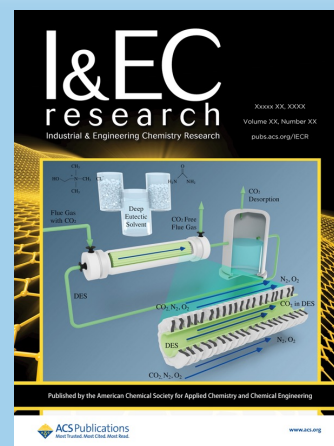
Experimental work

A Membrane Contactor Enabling Energy-Efficient CO₂ Capture from Point Sources with Deep Eutectic Solvents

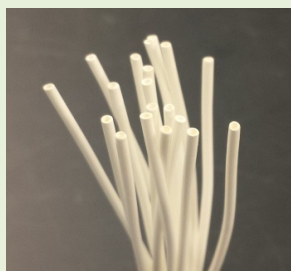
Syed Z. Islam,* Md Arifuzzaman, Gernot Rother, Vera Bocharova, Robert L. Sacchi, Jacek Jakowski, Jingsong Huang, Ilia Nicolaevich Ivanov, Ramesh R. Bhave,* Tomonori Saito, and David S. Sholl

Cite This: <https://doi.org/10.1021/acs.iecr.3c00080>

Read Online



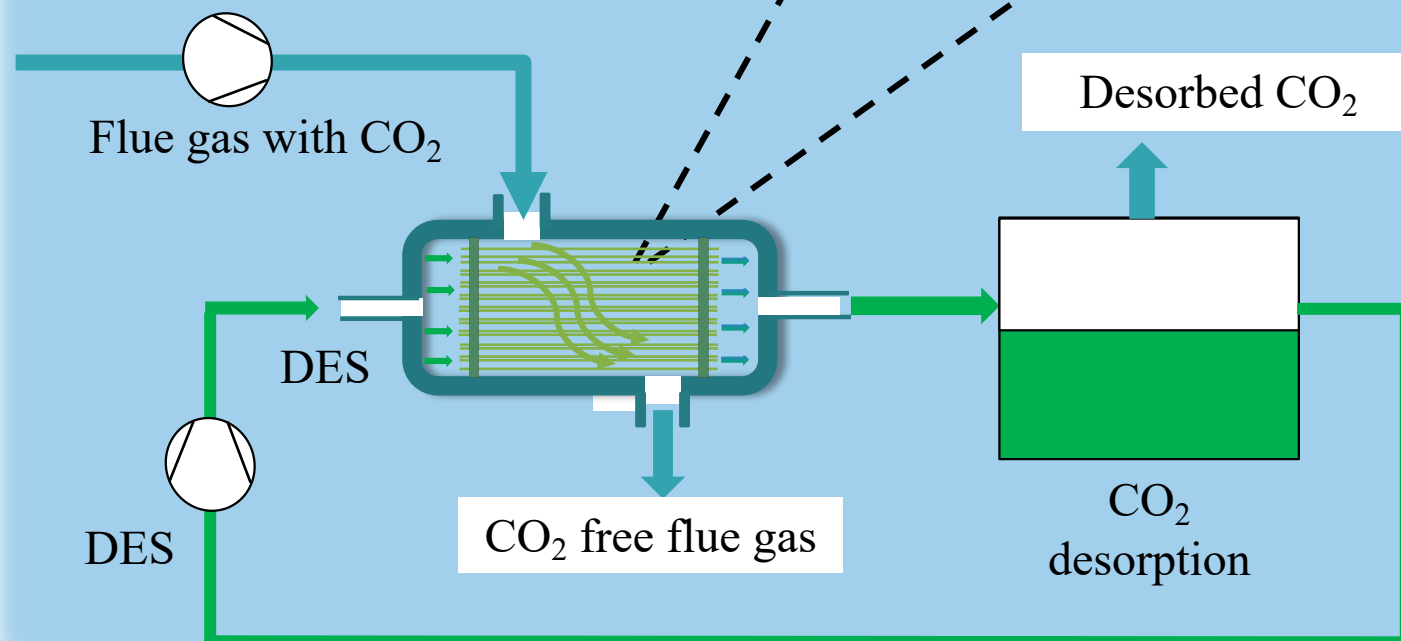
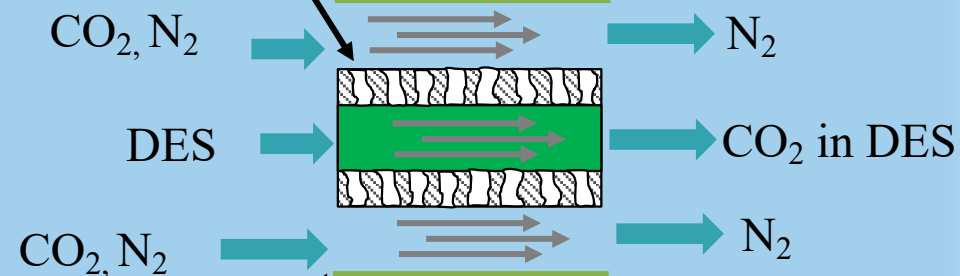
Polypropylene hollow fibers



- Purity recovered CO₂ of 96.7%

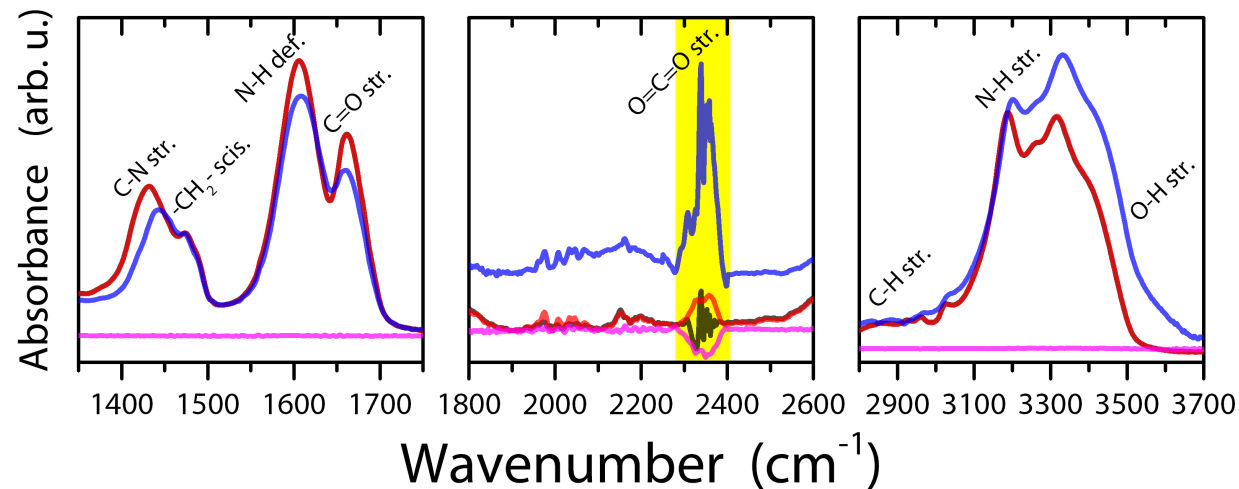
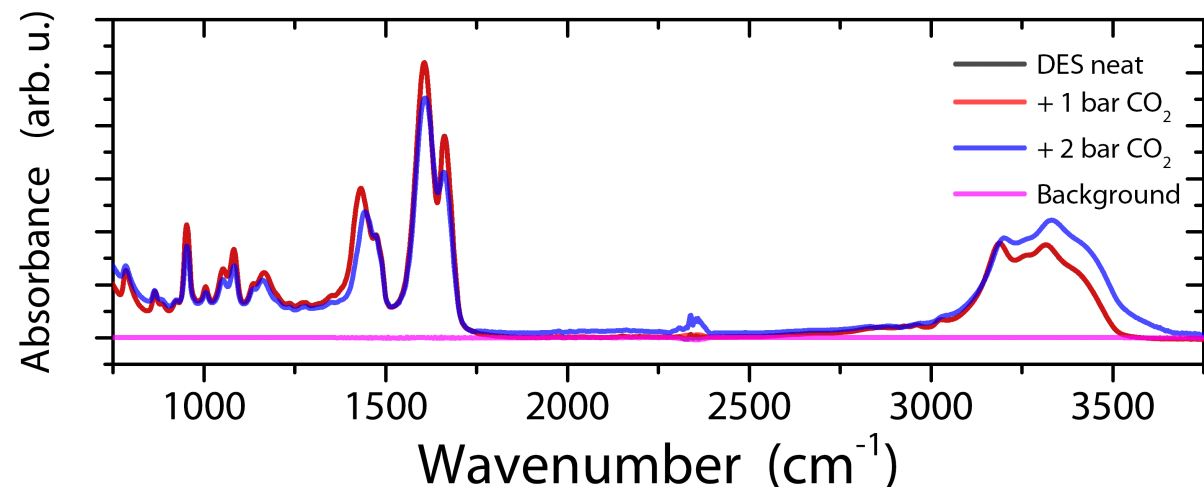
Polymer Hollow Fiber Membrane Contactor

Microporous polymer hollow fiber



Experimental results

- Separation of CO₂ with 96.7% purity from 50%/50% mixture of CO₂/N₂
- No N₂ detected
- Input pressure up to 2 bars
- FTIR suggests physisorption
- **Question: what is the mechanism?**



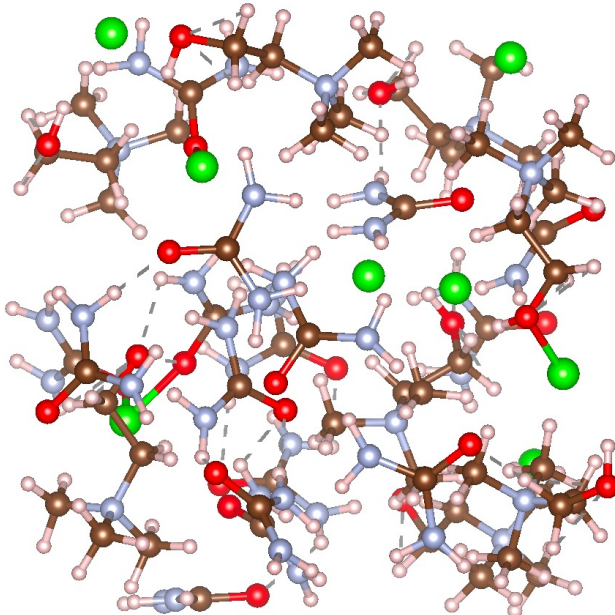
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Simulations

Computational model:

- urea 8 atoms
- choline 22 atoms
- DES (304 atoms= 8 cholines+16 ureas)
- periodic box: 1.5x1.5x1.5nm

Siepmann, JPCB 2018, 122, 1245



Goal:

- Understand FTIR experimental data
- Explain binding energy and affinity of reline towards CO₂, N₂
- Validate computational model towards search for future DES

Methodology:

- Electronic structure: DFTB(periodic) & DFT
- IR from MD (ACF) vs IR from Hessian
- Binding energy & motifs
- Statistical mechanics
(ZPE, thermal effects, entropy)
- Temperature: 333.15K

Overview of Density Functional Tight-Binding

Extended Hückel type method using atomic parameters from DFT (PBE, GGA-type), diatomic repulsive potentials from B3LYP

- Seifert, Eschrig (1980-86): STO-LCAO; 2-center approximation
- Porezag *et al.* (1995): efficient parameterization scheme: **NCC-DFTB**
- Elstner *et al.* (1998): charge self-consistency: **SCC-DFTB**
- Köhler *et al.* (2001): spin-polarized DFTB: **SDFTB**
- Houraine *et al.* (2020): **DFTB+, a software package**

$$E^{(NCC-)DFTB} = \sum_i^{\text{valence orbitals}} n_i \varepsilon_i + \frac{1}{2} \sum_{A \neq B}^{\text{atoms}} E_{AB}^{\text{rep}}$$

**Zeroth-order (TB) Hamiltonian:
no e-e interactions**

$$E^{(SCC-)DFTB} = E^{(NCC-)DFTB} + \frac{1}{2} \sum_{A \neq B}^{\text{atoms}} \gamma_{AB} \Delta q_A \Delta q_B$$

Self-consistent charge-charge interactions

$$E^{S(\text{pin-polarized})DFTB} = E^{(SCC-)DFTB} + \frac{1}{2} \sum_A^{\text{atoms}} \sum_{I \in A} \sum_{I' \in A} p_{AI} p_{AI'} W_{AI'}$$

Self-consistent spin-spin interactions

$$E = \text{Tr}[h^{\text{core}} + \frac{1}{2} G(P)P]$$

$$F = h^{\text{core}} + G(P)$$

Overview of Density Functional Tight-Binding

- Only valence electrons considered
 - minimal basis set, 1 to 9 per atom, Slater type orbitals
 - energy obtained by diagonalization of generalized DFTB eigenvalue problem:

$$\mathbf{H}^0 \mathbf{C} = \mathbf{S} \mathbf{C} \boldsymbol{\varepsilon} \quad \text{with} \quad S_{\mu\nu} = \langle \chi_\mu | \chi_\nu \rangle$$

$$H_{\mu\nu}^0 = \langle \chi_\mu | \hat{H}[\rho_0^M, \rho_0^N] | \chi_\nu \rangle$$

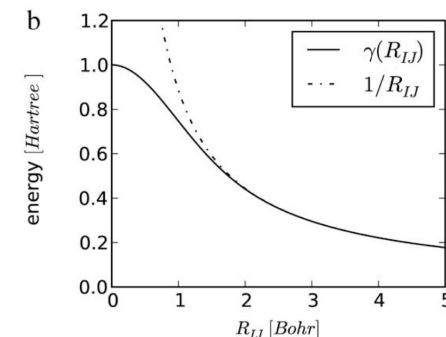
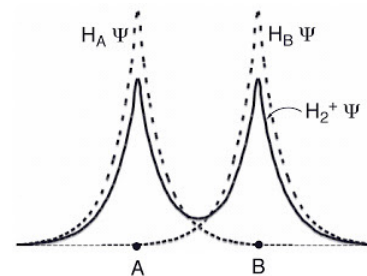
- Coulomb asymptotic for electron-electron term:

$$E_{el-el} = \frac{1}{2} \sum_{A \neq B}^{atoms} \Delta q_A \cdot \gamma_{AB}(R_{AB}) \cdot \Delta q_B$$

γ_{AB} — distance-dependent charge-charge interaction functional;

$\gamma_{AB} = \gamma_{AB}(U_A, U_B, R_{AB})$ for $R_{AB} \rightarrow \infty$: Coulomb potential $1/R_{AB}$

$\gamma_{AA} = \gamma_{AA}(U_A, U_A, R_{AA})$ for $R_{AA} \rightarrow 0$: Hubbard $U_A = \frac{1}{2}(IP_A - EA_A)$



- Parameters are publically available and transferable (not all elements are parametrized)

Main repositories (U. of Bremen, Germany)

<http://www.dftb-plus.info/>

<http://www.dftb.org>

Overview of Density Functional Tight-Binding

Main Features & Advantages

- Localized A.O. with PBC
- Very fast:
 - routine MD for ~1000 atoms on a desktop
 - 30ps long MD for ~300 atoms within a day timescale
- Accuracy comparable to DFT
- Code is open source
- Many features implemented:
band structure, transport (NEGF), TDDFT, Grimme dispersion

Weaknesses

- Parameters not comprehensive
- Parameters often need tweaking & benchmarking before use

Simulations

- Simulations of FTIR: CO_2 in gas phase and liquid reline
- Binding energy: CO_2 vs N_2 in reline
- Thermal, entropy effects
- Binding motifs

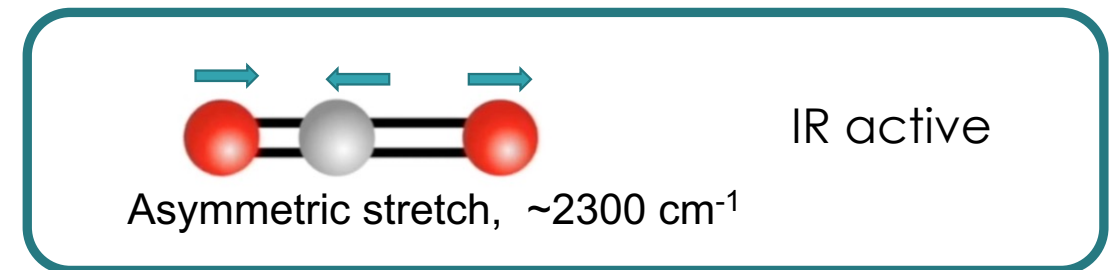
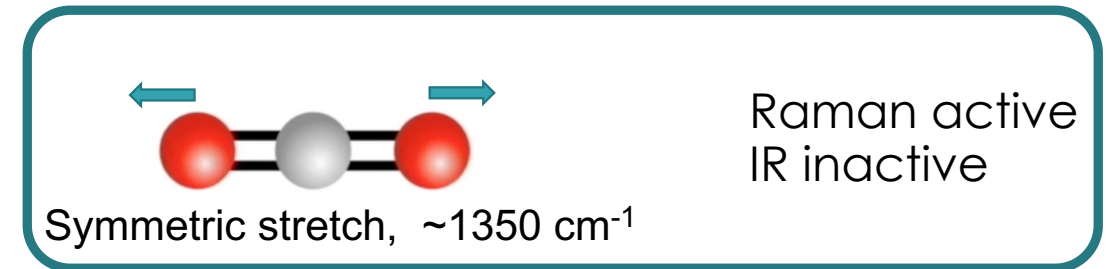
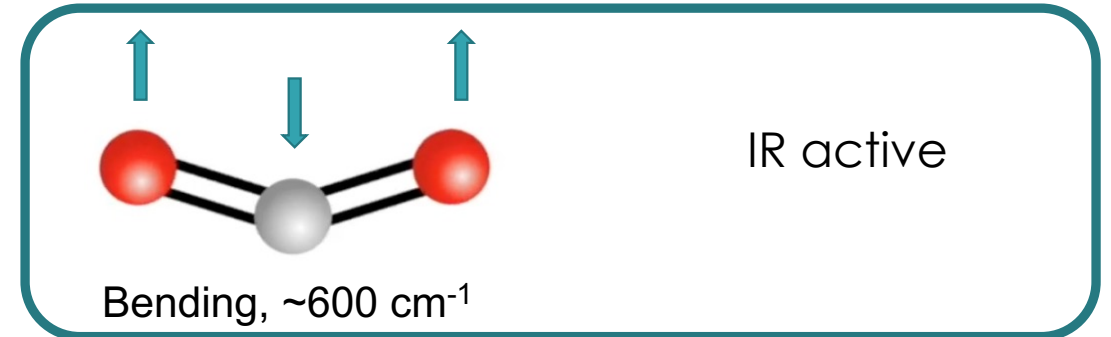
Vibrational spectra of CO₂ in gas phase and in reline

IR of CO₂ molecule (linear)

- 3 atoms → 4 vibrations ($=3N-5$)

Normal modes analysis

- Bending (double degenerate)
- Symmetric stretching
- Asymmetric stretching



Benchmark: CO₂ molecule gas phase

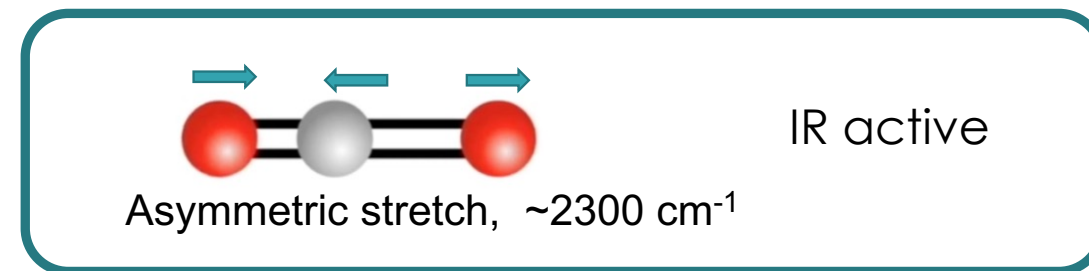
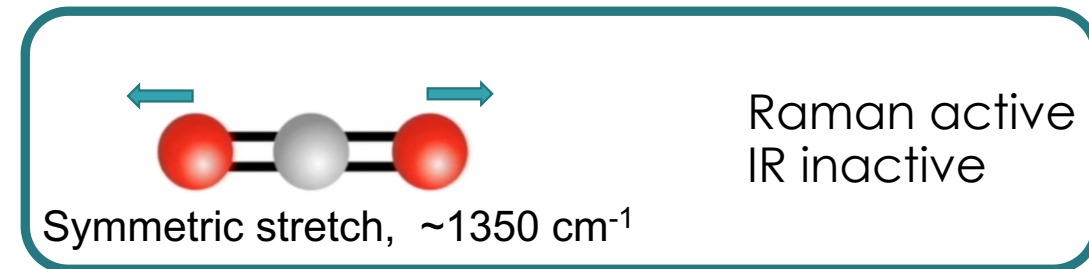
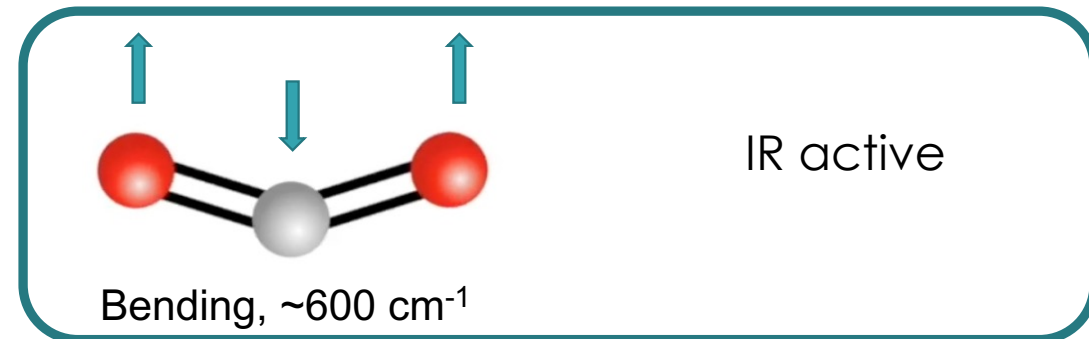
FTIR spectra from MD:

- Save time dependent dipoles
- ... or save charges and velocities
- Dipole-dipole autocorrelation function
- Fourier transform it

$$I(\omega)_{cl} = \frac{1}{2\pi\omega^2} \int_{-\infty}^{\infty} dt e^{-i\omega t} \left\langle \frac{d\vec{M}(0)}{dt} \cdot \frac{d\vec{M}(t)}{dt} \right\rangle$$

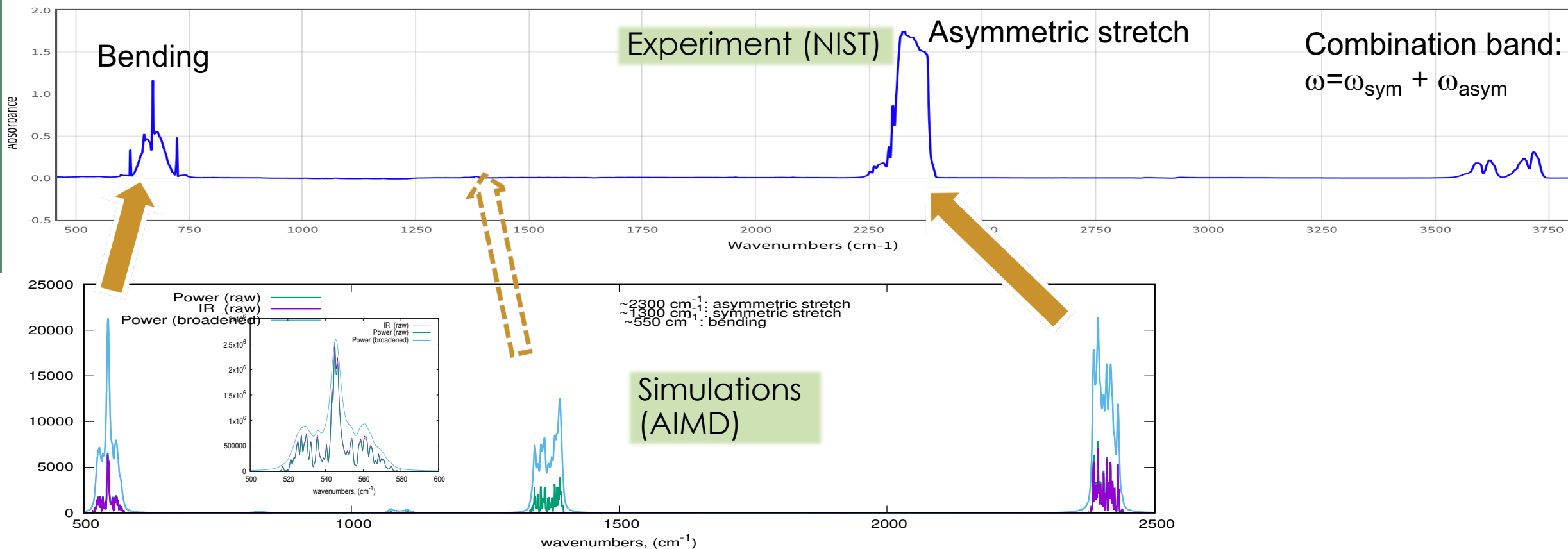
$$= \frac{1}{2\pi\omega^2} \int_{-\infty}^{\infty} dt e^{-i\omega t} \left\langle \left(\sum_{i=1}^n q_i \vec{v}_i(0) \right) \cdot \left(\sum_{j=1}^n q_j \vec{v}_j(t) \right) \right\rangle$$

$$\frac{d\vec{M}}{dt} = \frac{d}{dt} \sum_i q_i(t) \vec{R}_i(t) = \sum_i [\dot{q}(t) \vec{R}_i(t) + q_i(t) \dot{\vec{R}}_i(t)]$$



Benchmark: CO₂ molecule gas phase

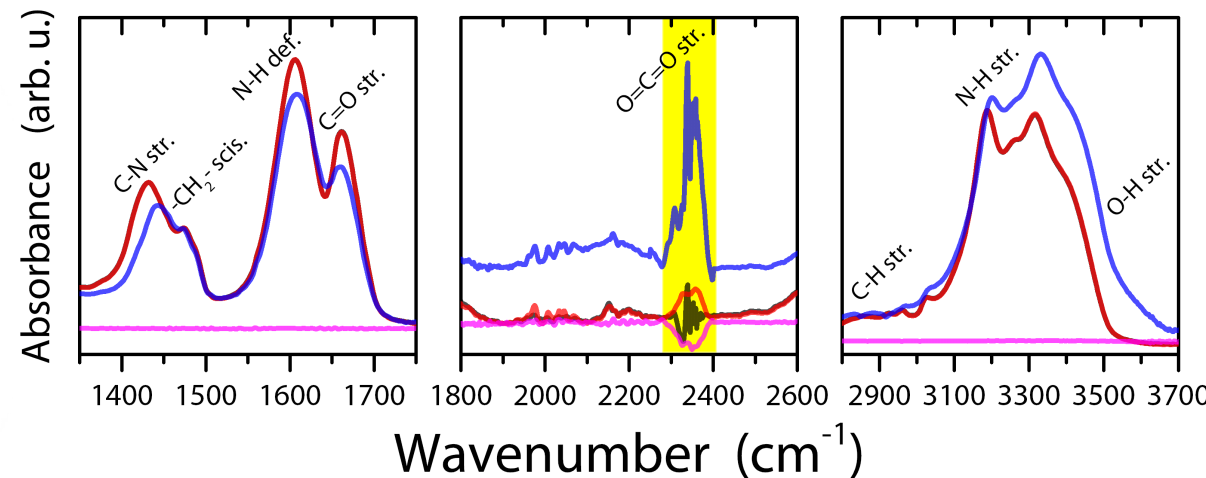
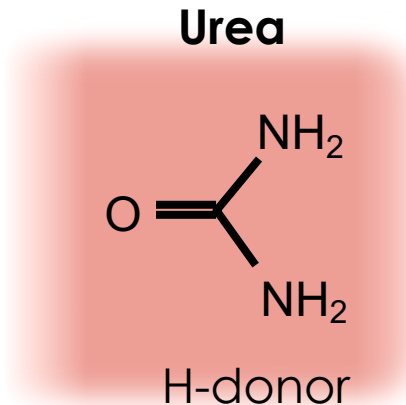
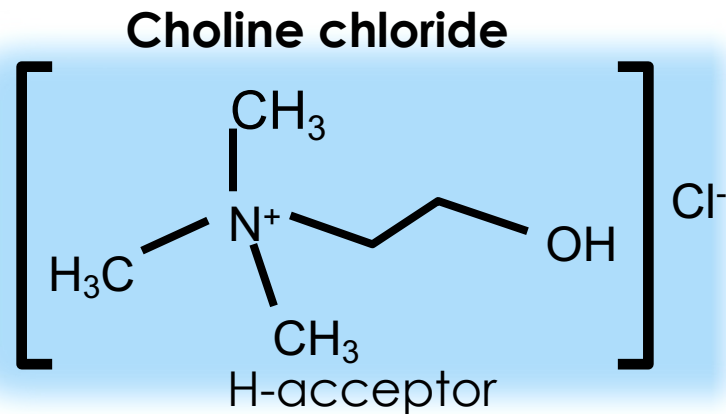
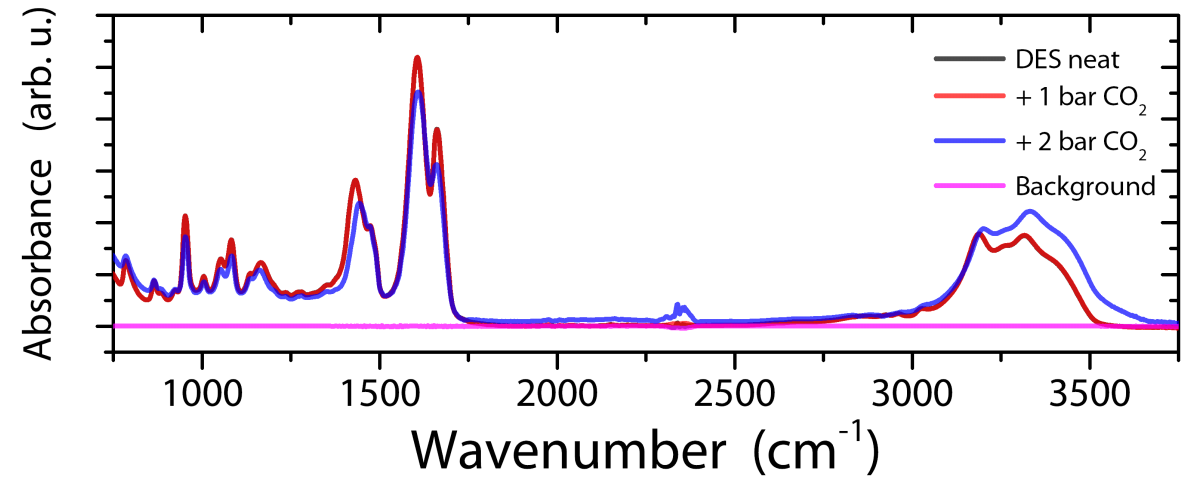
- **FTIR from Experiment** (data from NIST):
<https://webbook.nist.gov/cgi/cbook.cgi?ID=C124389&Type=IR-SPEC&Index=1#IR-SPEC>
- **FTIR from Simulations:**
 - calculated as average over **100 MD simulations**
 - NVE with initial random velocities corresponding to T=300K



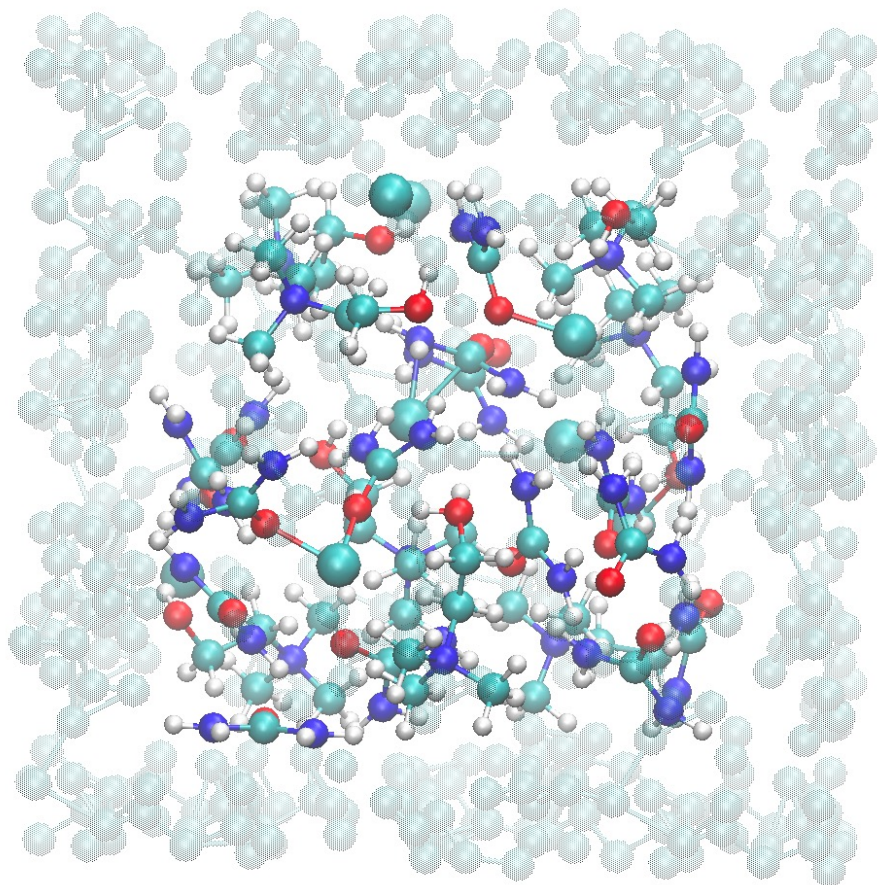
Vibrational spectra of CO₂ in gas phase and in reline

- Experiment:
no chemistry, physisorption
- What is the effect of reline on CO₂ spectra?
- How does CO₂ binds o reline?

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Vibrational spectra of CO₂ in reline

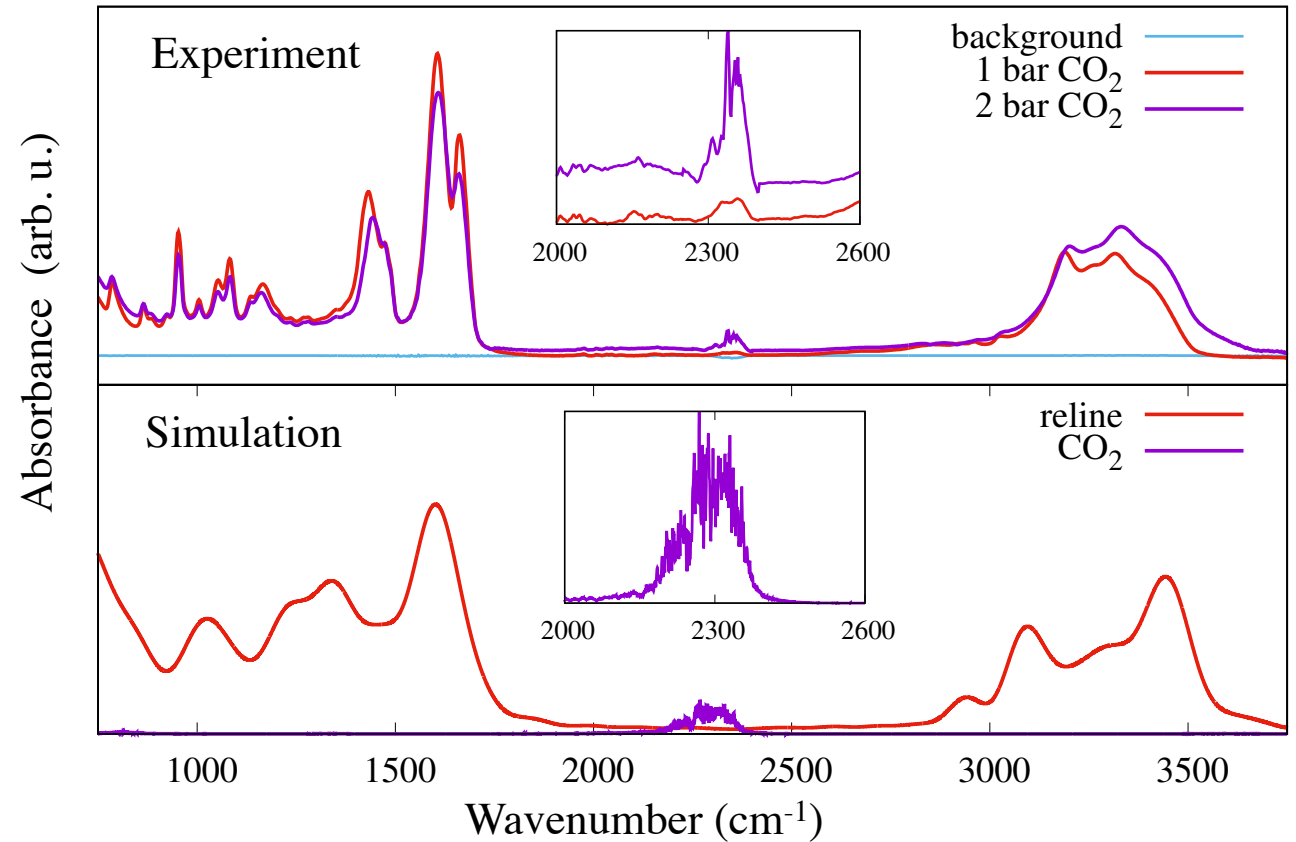


- Molecular dynamics simulations
- Periodic simulation box cube (1.43 nm)
- 10 randomized structures of reline + CO₂:
8 cholines + 16 ureas + 1 CO₂ (total 307 atoms)
- Monte Carlo based insertion of gas
- Electronic structure from DFTB3 + dispersion
- 3ob parametrization
- Periodic boundary condition with Gamma point sampling
- Constant energy microcanonical ensemble
- Initial kinetic energy corresponding to 300 K
- Total time = 30ps, time step dt = 1ps
- IR / power spectra as average over all simulations
- IR spectra from dipole-dipole autocorrelation function
- All modes (IR + Raman) from velocity-velocity autocorrelation function

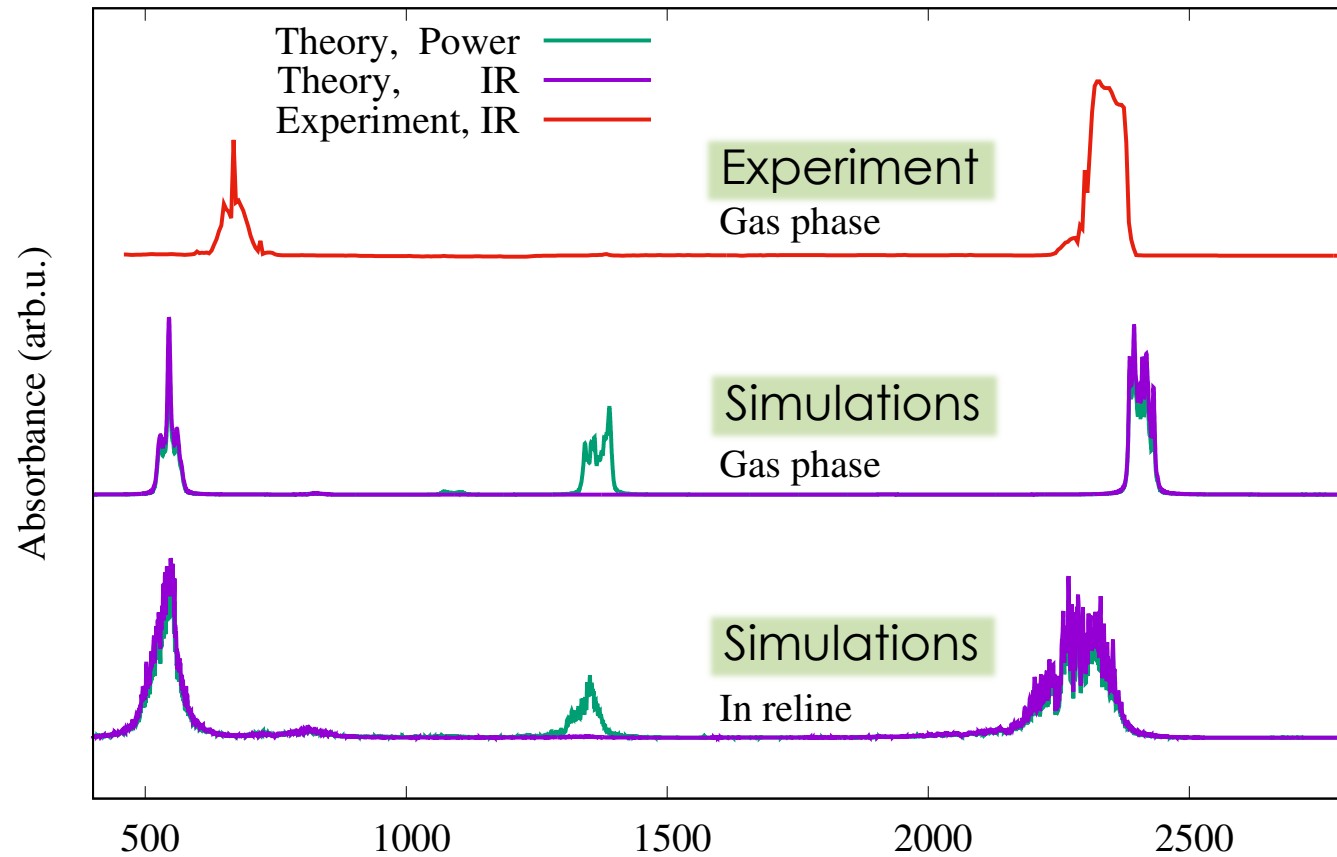
Vibrational spectra of CO₂ in reline

Simulations details

- 3rd order DFTB+dispersion
- Periodic boundary condition
- no chemistry, physisorption
- What is the effect of reline on CO₂ spectra?
- How does CO₂ binds o reline?

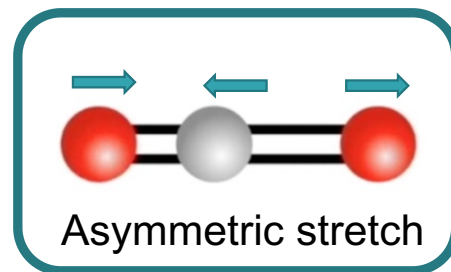
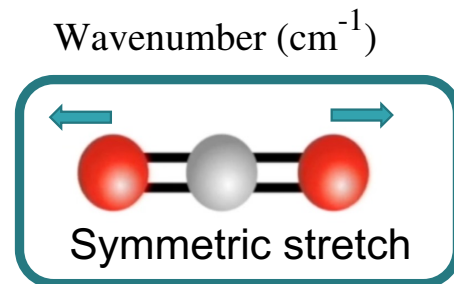
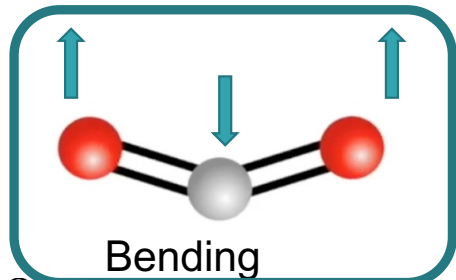


Vibrational spectra of CO₂ in gas phase and in reline



Simulations results

- Power spectrum:
 - velocity autocorrelation
- IR spectrum:
 - dipole autocorrelation
- Bending and symmetric stretch insensitive to reline (broadening)
- Asymmetric stretch redshifted



Correlation of vibrational modes, binding energy and structure descriptors

- Binding of CO₂ vs N₂ in reline
- 10 randomly packed structures of reline (thermalized, NVT)
- Monte Carlo based search for voids
- Optimization: 3rd order DFTB + dispersion, 300 parameters
- Normal modes analysis (mass weighted Hessian)
- Analysis: binding energy, separation (gas vs. reline), O-C-O angle, IR shift
- ZPE energy, entropy & thermochemistry corrections

Correlation of vibrational modes, binding energy and structure descriptors

- Binding energy (electronic)

$$E_{BE}^0 = E(G..S) - E(G) - E(S)$$

- Corrections (ZPE, thermochemistry)

$$\Delta E_{BE}^X = E^X(G_{solvent}) - E^X(G_{gas})$$

$$E_{BE}^X = E_{BE}^0 + \Delta E_{BE}^X$$

Thermochemistry (standard, harmonic approximation)

Internal energy (U)

$$U = RT^2 \left(\frac{\partial Q}{\partial T} \right)_V$$

Entropy (S)

$$S = R + R \ln(Q) + RT \left(\frac{\partial Q}{\partial T} \right)_V$$

Helmholtz free energy (F)

$$F = U - TS$$

Gibbs free energy (G)

$$G = F + pV$$

Translation

$$q_t = \left(\frac{2\pi m k_B T}{h^2} \right)^{3/2} \frac{k_B T}{P}$$

$$E_t = \frac{3}{2} RT$$

$$S_t = R \left(\ln(q_t) + \frac{5}{2} \right)$$

Rotation

$$q_r = \frac{1}{\sigma} \left(\frac{T}{\Theta_r} \right)$$

$$E_r = RT$$

$$S_r = R (\ln(q_r) + 1)$$

Vibrations

$$q_v = \prod_K \frac{e^{-\Theta_{v,K}/2T}}{1 - e^{-\Theta_{v,K}/T}}$$

$$E_v = R \sum_K \Theta_{v,K} \left(\frac{1}{2} + \frac{1}{e^{\Theta_{v,K}/T} - 1} \right)$$

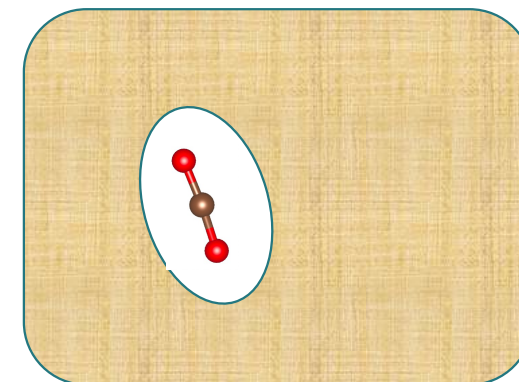
$$S_v = R \left(\ln(q_v) + T \left(\frac{\partial \ln q}{\partial T} \right)_V \right)$$

$$= R \sum_K \left(\frac{\Theta_{v,K}/T}{e^{\Theta_{v,K}/T} - 1} - \ln(1 - e^{-\Theta_{v,K}/T}) \right)$$

Thermochemistry: effects of entropy, Temp & Press

- Gas phase CO₂ & N₂ vs dissolved in reline
- Gas phase CO₂:
 - 3 translations, 2 (or 3) rotations, 6 vibrations
- Gas phase N₂:
 - 3 translations, 2 rotations, 1-vibration
- CO₂ in reline:
 - 0 translations, 0 rotation, 9 vibrations
- N₂ in reline:
 - 0 translations, 0 rotations, 6 vibrations

Gas molecules trapped in void



Partition function: $Q = q_{rot} * q_{transl} * q_{vib}$

$$Q = \left[\frac{k_B T}{P} \left(\frac{2\pi m k_B T}{h^2} \right)^{3/2} \cdot \frac{T}{\sigma \theta_{rot}} \right]^{\delta} \cdot \left\{ \prod_{j=1}^{N_{vib}} \frac{e^{-\theta_j^{vib}/2T}}{1 - e^{-\theta_j^{vib}/T}} \right\}$$

Gas phase: $\delta = 1, N_{vib} = 5$

In reline: $\delta = 0, N_{vib} = 9$

Main contribution to E_{BE} : conversion of transl, rot \rightarrow vibrations

Thermochemistry: effects of entropy, Temp & Press

Partition function: $Q = q_{\text{rot}} * q_{\text{transl}} * q_{\text{vib}}$

$$Q = \left[\frac{k_B T}{P} \left(\frac{2\pi m k_B T}{h^2} \right)^{3/2} \cdot \frac{T}{\sigma \theta_{\text{rot}}} \right]^{\delta} \cdot \left\{ \prod_{j=1}^{N_{\text{vib}}} \frac{e^{-\theta_j^{\text{vib}} / 2T}}{1 - e^{-\theta_j^{\text{vib}} / T}} \right\}$$

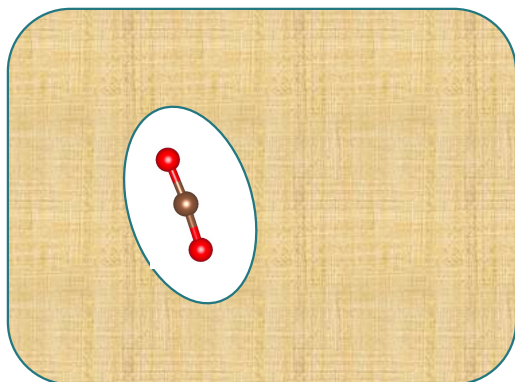
Gas phase: $\delta = 1, N_{\text{vib}} = 5$

In reline: $\delta = 0, N_{\text{vib}} = 9$

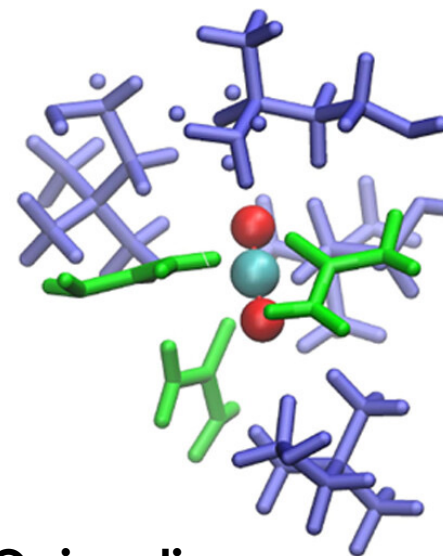
Main contribution to E_{BE} : conversion of transl, rot \rightarrow vibrations

Minimal Solvation model

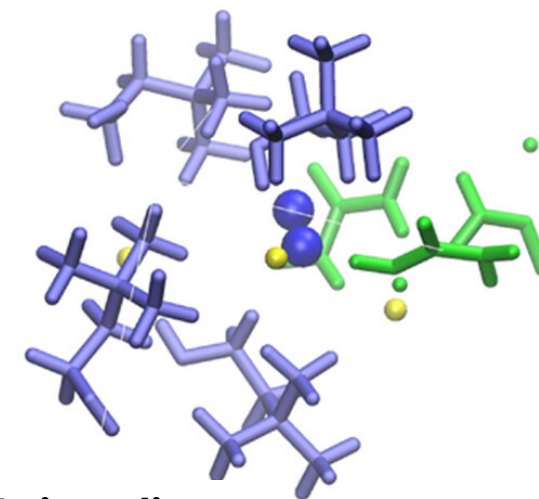
Gas molecules
trapped in void



1st solvation shell model

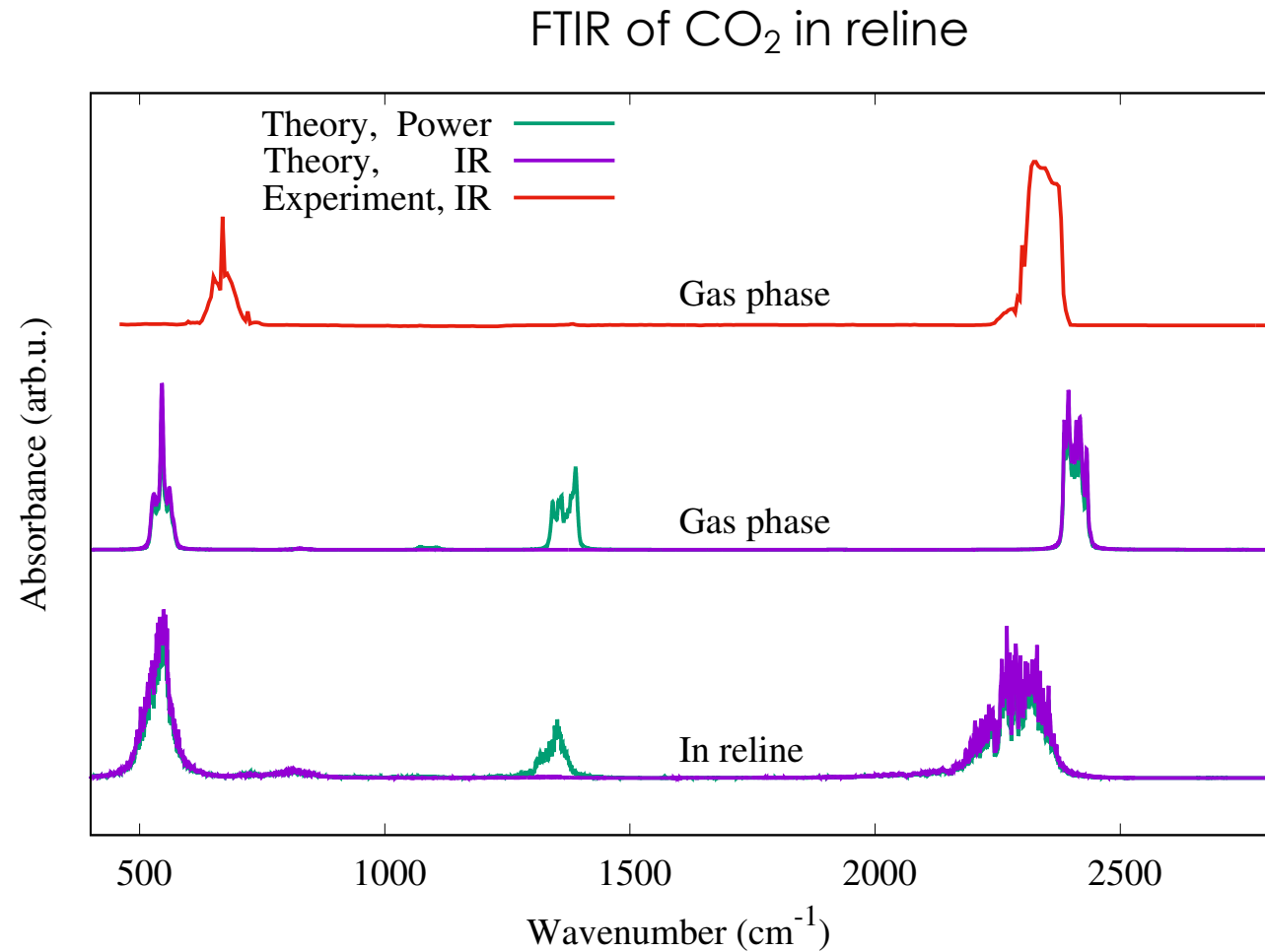
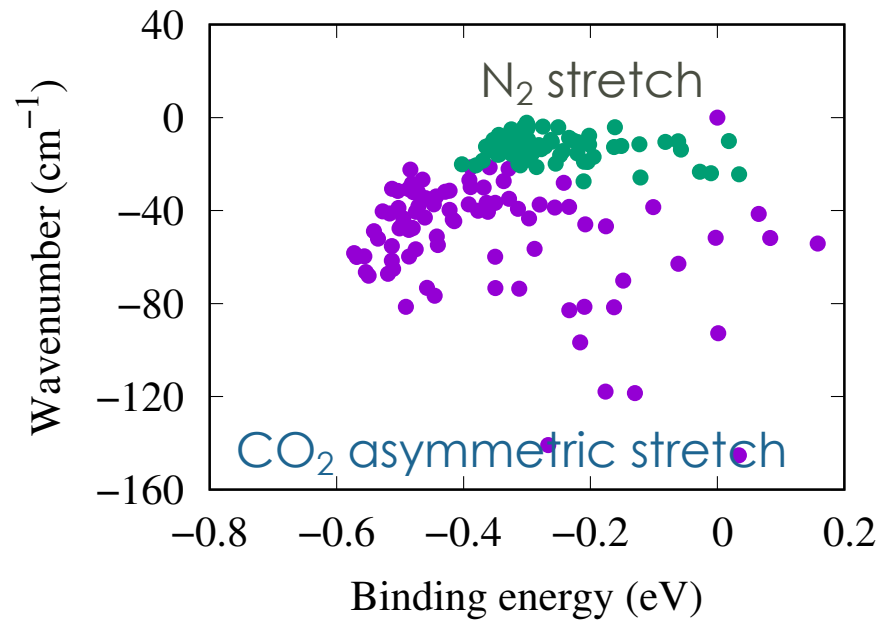


CO₂ in reline

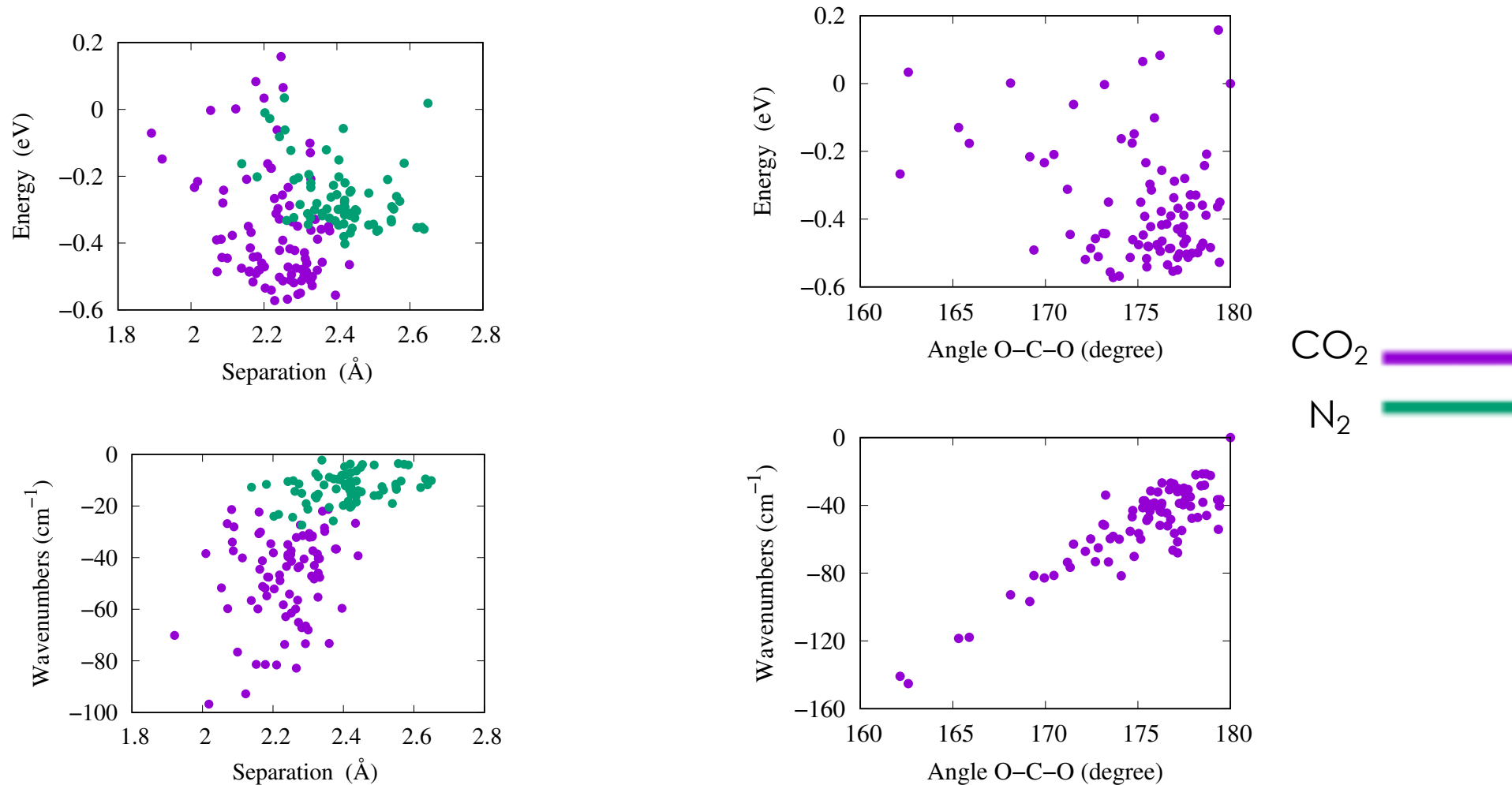


N₂ in reline

Correlation of vibrational modes, binding energy and structure descriptors

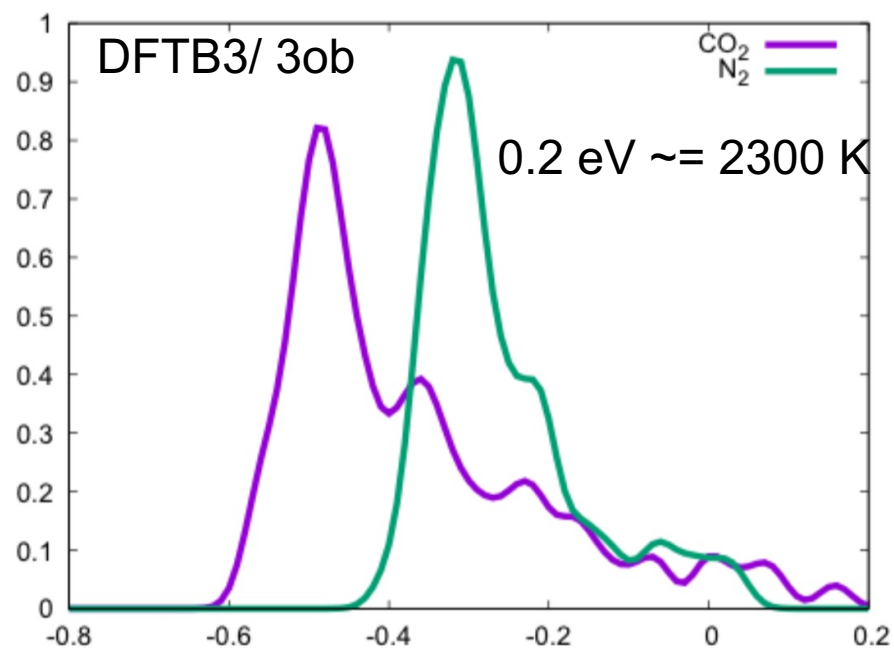


Correlation of vibrational modes, binding energy and structure descriptors



Binding energy (BE)

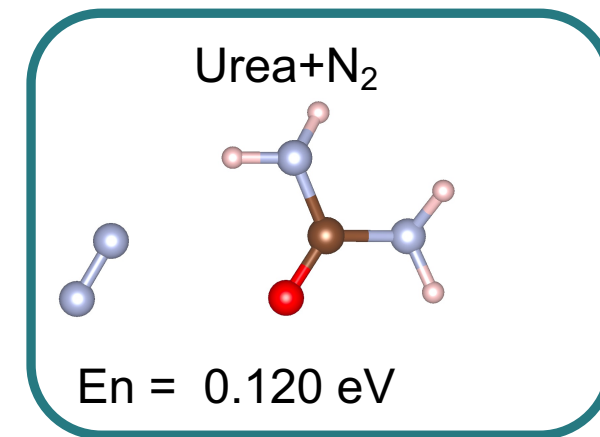
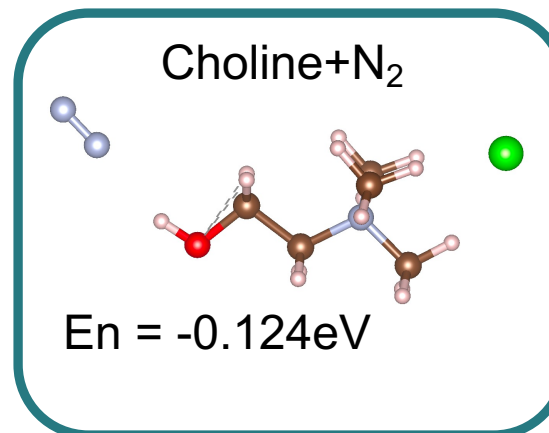
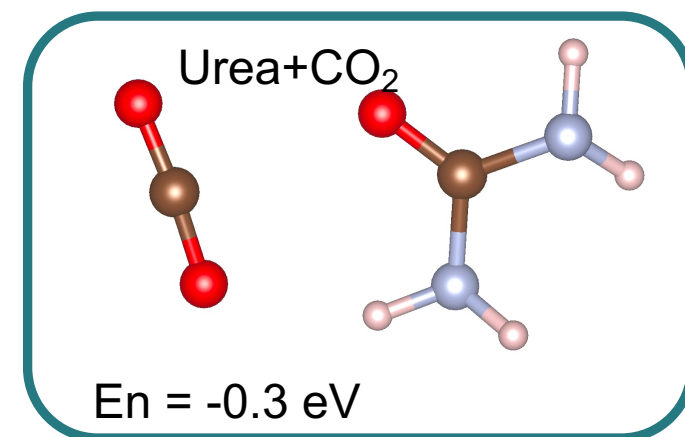
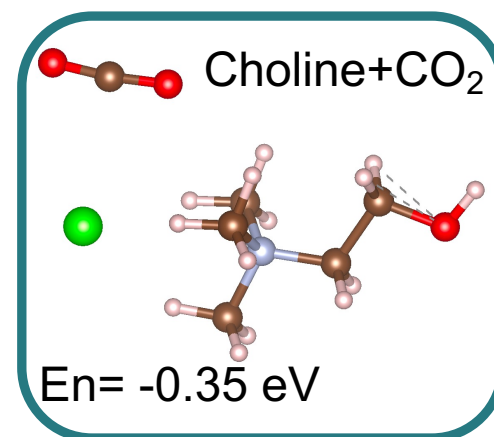
- Electronic energy only DFTB3/ 3ob
- No entropy /thermal effects
- Energy with respect to gas phase
- All structures optimized



Binding Energy (eV)

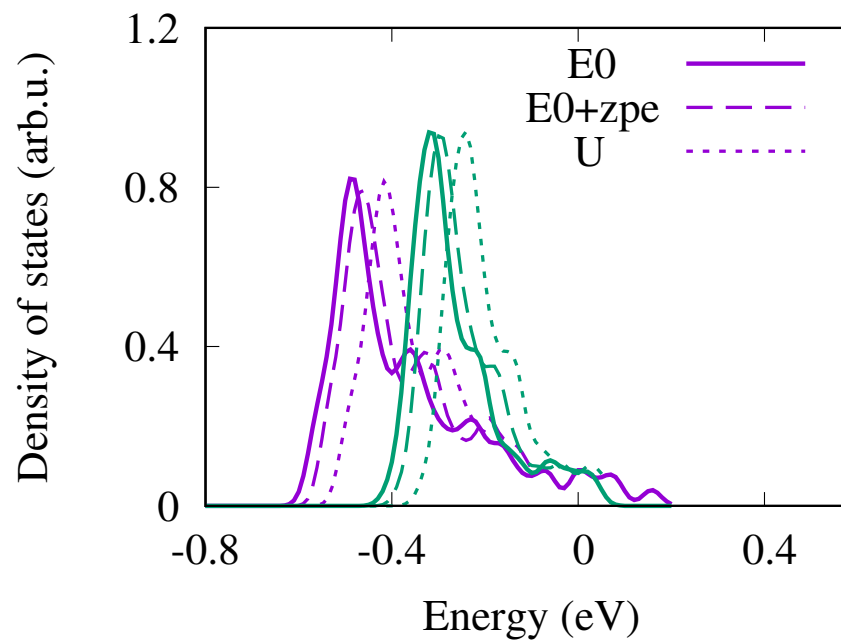
$$BE = E(\text{gas+reline}) - E(\text{reline}) - E(\text{gas})$$

B3LYP/6-31G(d)

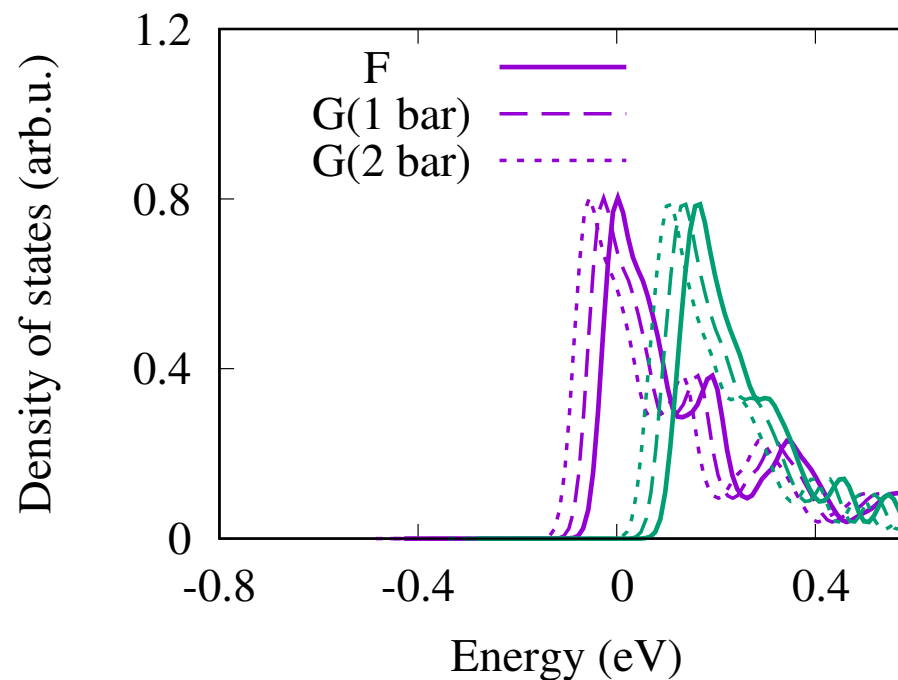


Binding energy

Electronic +vibrational corrections

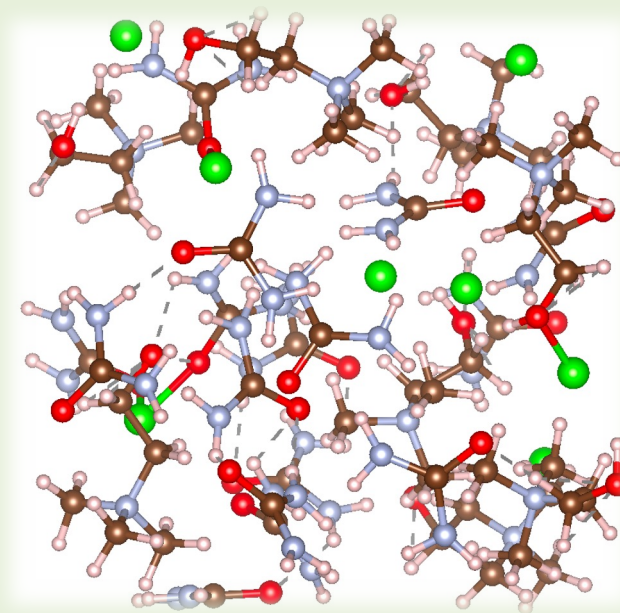
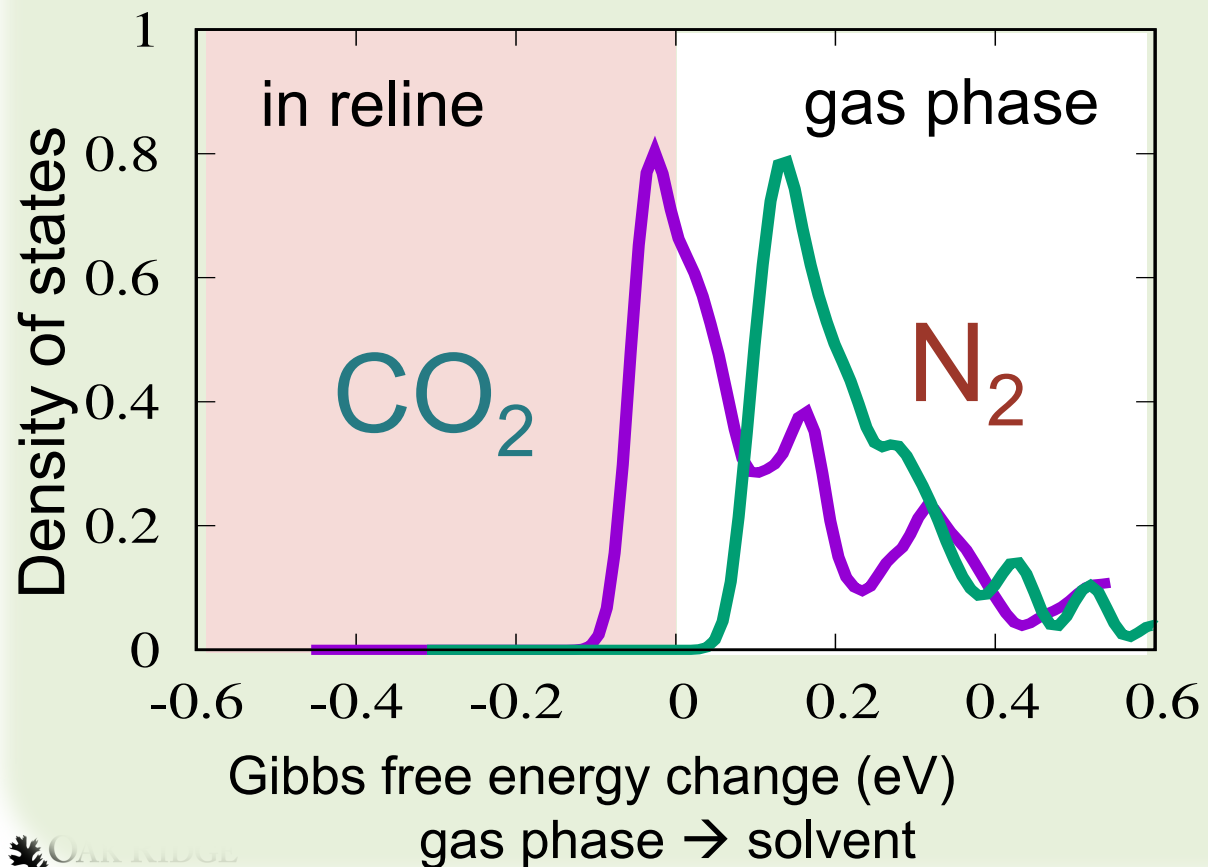


Entropy effects included



Summary of Results

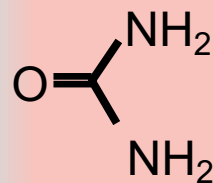
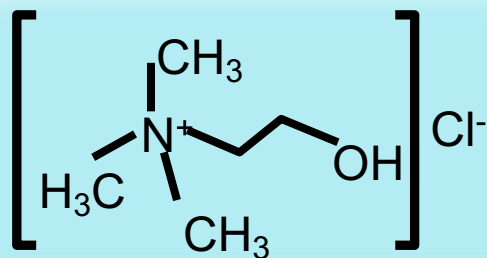
Electronic and entropic effects lead to selective capture of CO₂ vs N₂ in reline (DES)



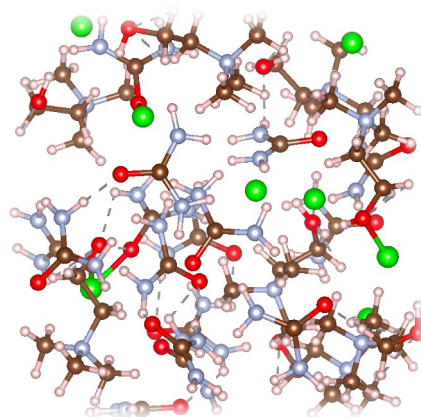
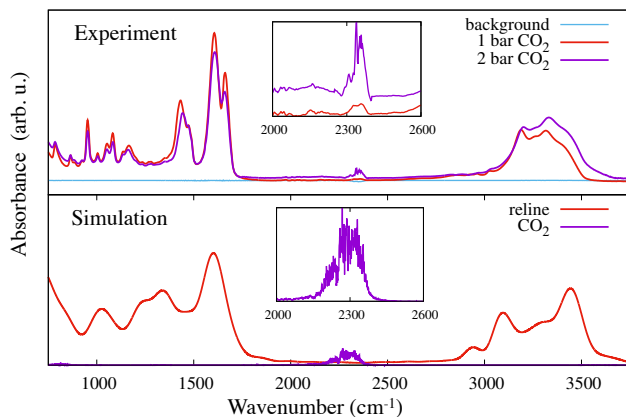
Experiment and simulations of CO₂ capture in deep eutectic solvents

Reline is a mixture of 1:2 molar ratio of:

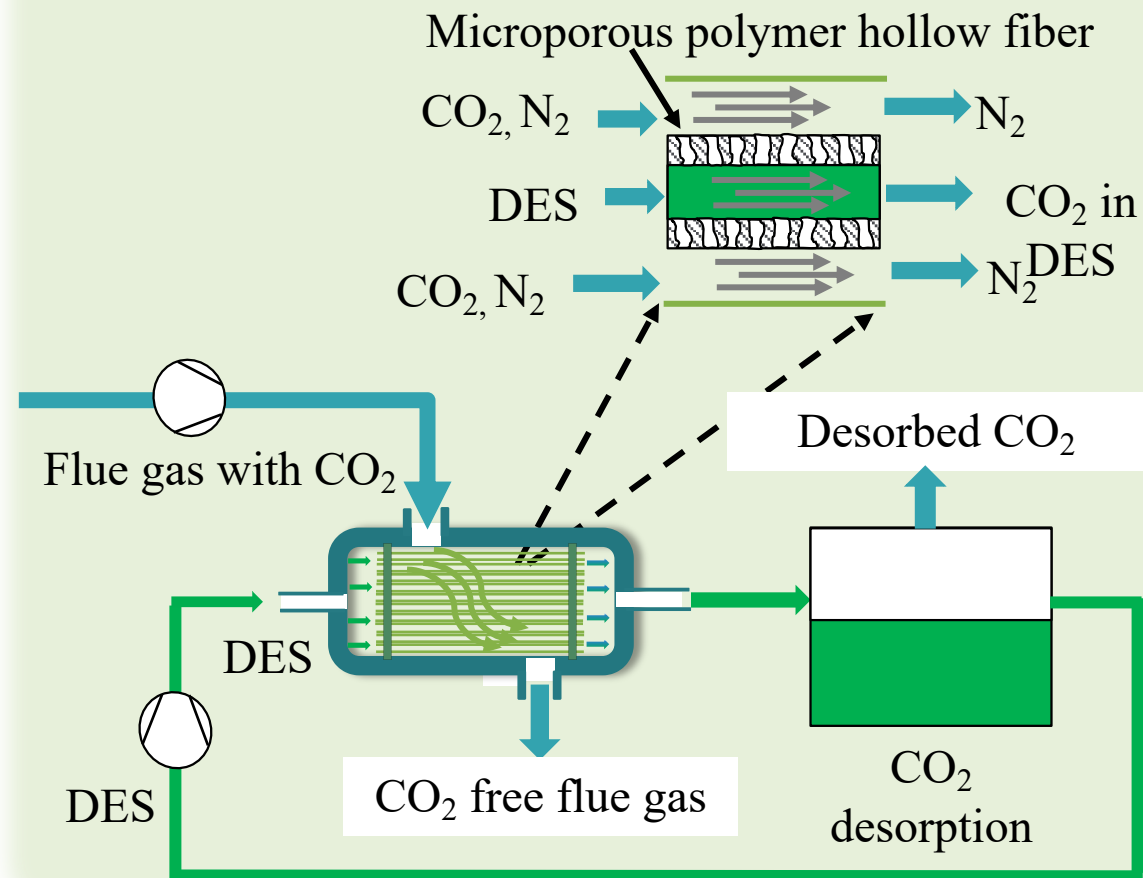
- choline chloride (HBA) + urea (HBD)



FTIR for CO₂ in reline

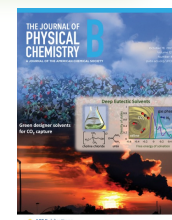


Polymer Hollow Fiber Membrane Contactor



Electronic and entropic effects lead to selective capture of CO₂ in reline (DES) with from CO₂/N₂ mixture with 97% purity

- [1] S. Z. Islam, [Ind. & Eng. Chem. Res. (2023) 62, 10,4455
[2] J. Jakowski, et al. J. Phys. Chem. B, (2023), 127, 8888



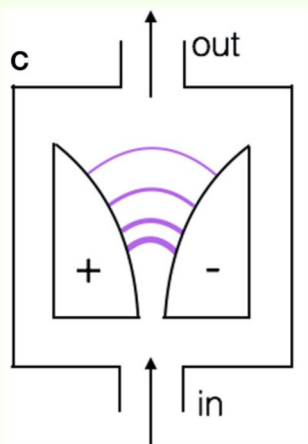
Part II. Towards modeling of CO₂ conversion from real time TDDFT

- Real-time TDDFT: electronic excitation, non-equilibrium processes
- Theory, implementation, benchmarking
- RMG-DFT program

Carbon dioxide conversion

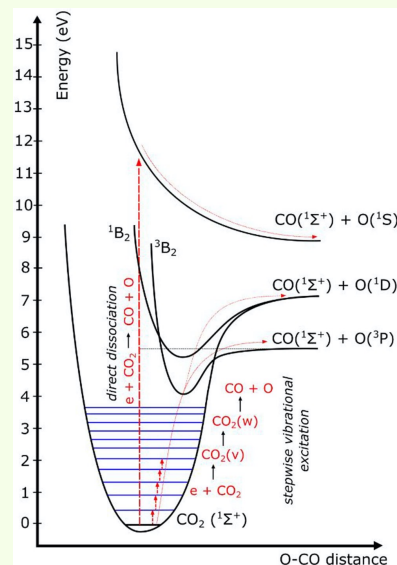
- Needs for computational models:
 - non-equilibrium charge transfer, redox
 - electronically excited states during dynamics
 - interaction with UV-VIS, laser pulses
 - coupling between electrons and nuclei
 - charge transfer, nanoelectronics
 - applicable for large systems

Plasma technology

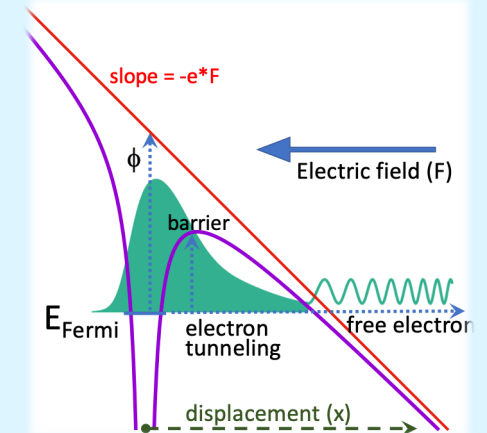
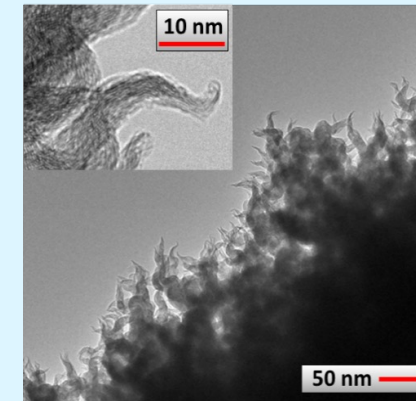


Gliding Arc Plasmatron reactor for CO₂ conversion

Front. Energy Res. 2020, 8:111

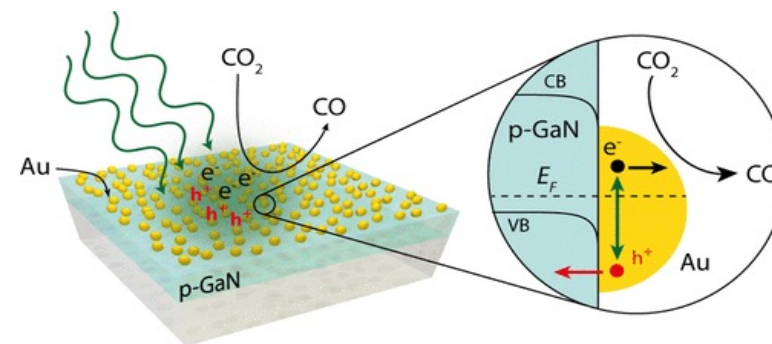


Electrochemical



J. Electrochem. Soc. 161, H558 (2014).

Plasmonics

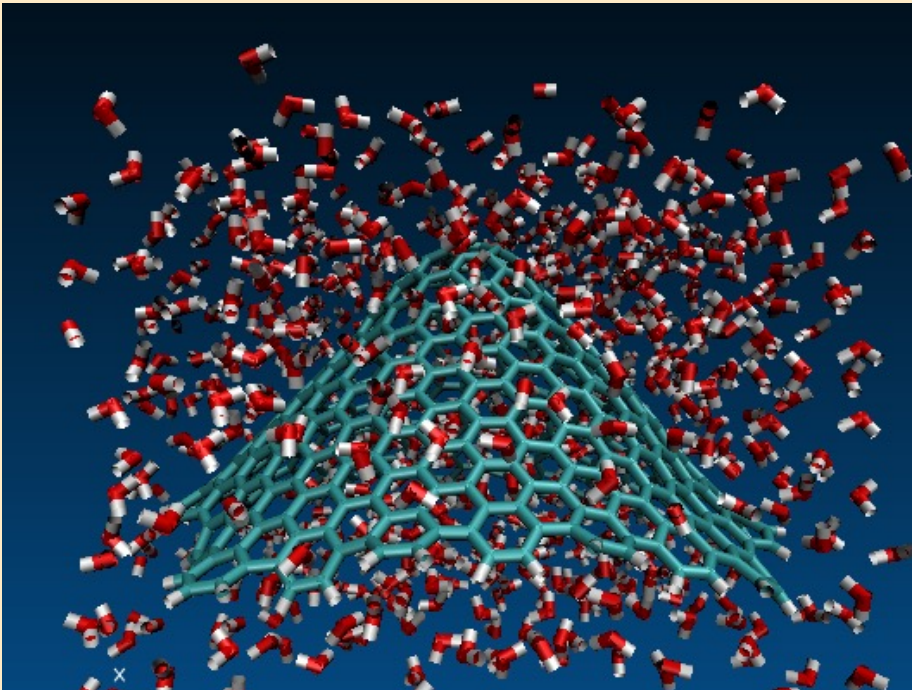


generation of non-equilibrium “hot” electron–hole pairs via surface plasmon decay within metal nanostructure

Nano Lett. 2018, 18, 4, 2545–2550

RMG-DFT calculations on Frontier

Graphene nanocone + waters:
2,979 atoms and 8,000 electrons



Important system for electric-
field-assisted catalysis



RMG - A REAL SPACE MULTIGRID DFT CODE

[Home](#) [Github Project Page](#) [Download](#) [Documentation](#) [Get Help](#)

About RMG

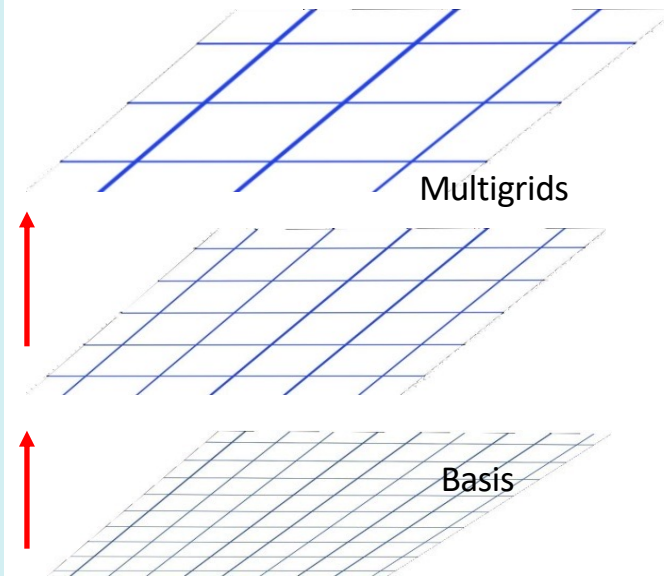
RMG is an Open Source computer code for electronic structure calculations and modeling of materials and molecules. It is based on density functional theory and uses real space basis and pseudopotentials. Designed for scalability it has been run successfully on systems with thousands of nodes and hundreds of thousands of CPU cores. It runs on Linux/UNIX, Windows and OS X.

Collaboration with RMG-DFT team at NCSU:
J. Bernholc, Wenchang Lu and Emil Briggs

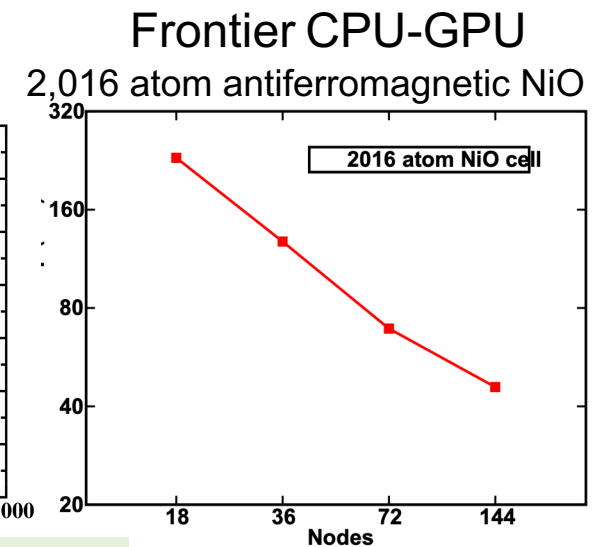
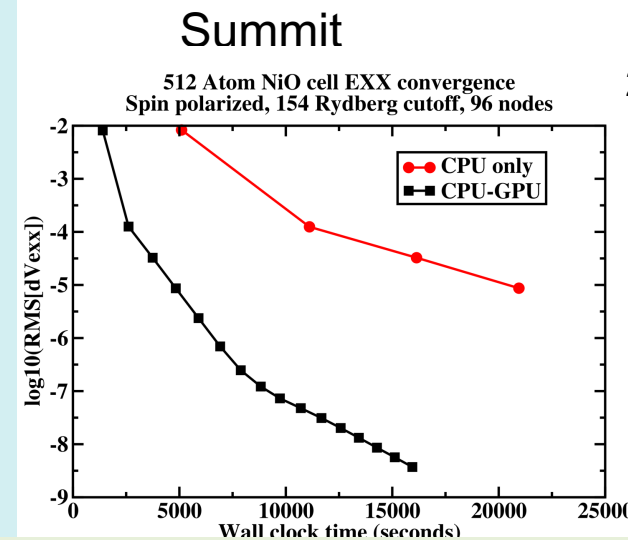
<http://www.rmgdft.org>

Real-space Multi-Grid method (RMG)

- Full-featured DFT/hybrid-DFT code: DFT equations solved directly on the grid.
- Multigrid techniques remove instabilities by working on one length scale at a time.
- Excellent parallelization via domain decomposition: multi-core CPUs, multiple GPUs/node, many nodes. Runs well on Frontier, Aurora, Summit, Perlmutter, Polaris, clusters, and workstations.
- Full Nvidia, AMD and Intel GPU support: uses all CPU cores and GPUs per node.
- Norm-conserving and ultrasoft pseudopotentials [included in the distribution](#).
- High performance for all lattice types.
- Hybrid functionals, LDA+U, vdW-DF, Grimme, and spin-orbit coupling.
- Web interface for setting up input using cif, xyz, VASP, or Quantum Espresso files.
- Web interface for analyzing results.
- Very high accuracy vs. Quantum Espresso: $\mu\text{Ha}/\text{atom}$.
- Supported by the Exascale Computing Project for large-scale DFT input to QMCPACK



www.rmgdft.org



Ref: Briggs, Lu, Bernholc, *npj Comput. Mater.* (2024) 10, 17

Electron dynamics

- **Theory:**

- Magnus Expansion
- Density matrix propagation (von Neuman eq.)
- Commutator expansion

- **Implementation and benchmarks:**

- CPU/GPU
- Optical absorption spectra UV-VIS (benzene, plasmonics)
- timing information

Theory: Magnus expansion

- Evolution of density matrix for electrons

$$\frac{\partial P(t)}{\partial t} = -\frac{i}{\hbar} [H(t), P(t)]$$

- Formal solution through time-evolution operator

$$\mathcal{U}(t) = \exp\left(-\frac{i}{\hbar} \int_0^t H(t') dt'\right)$$

$$P(t) = \mathcal{U}(t) \cdot P(0) \cdot \mathcal{U}(t)^\dagger$$
$$= \exp(\Omega) \cdot P(0) \cdot \exp(\Omega)^\dagger$$

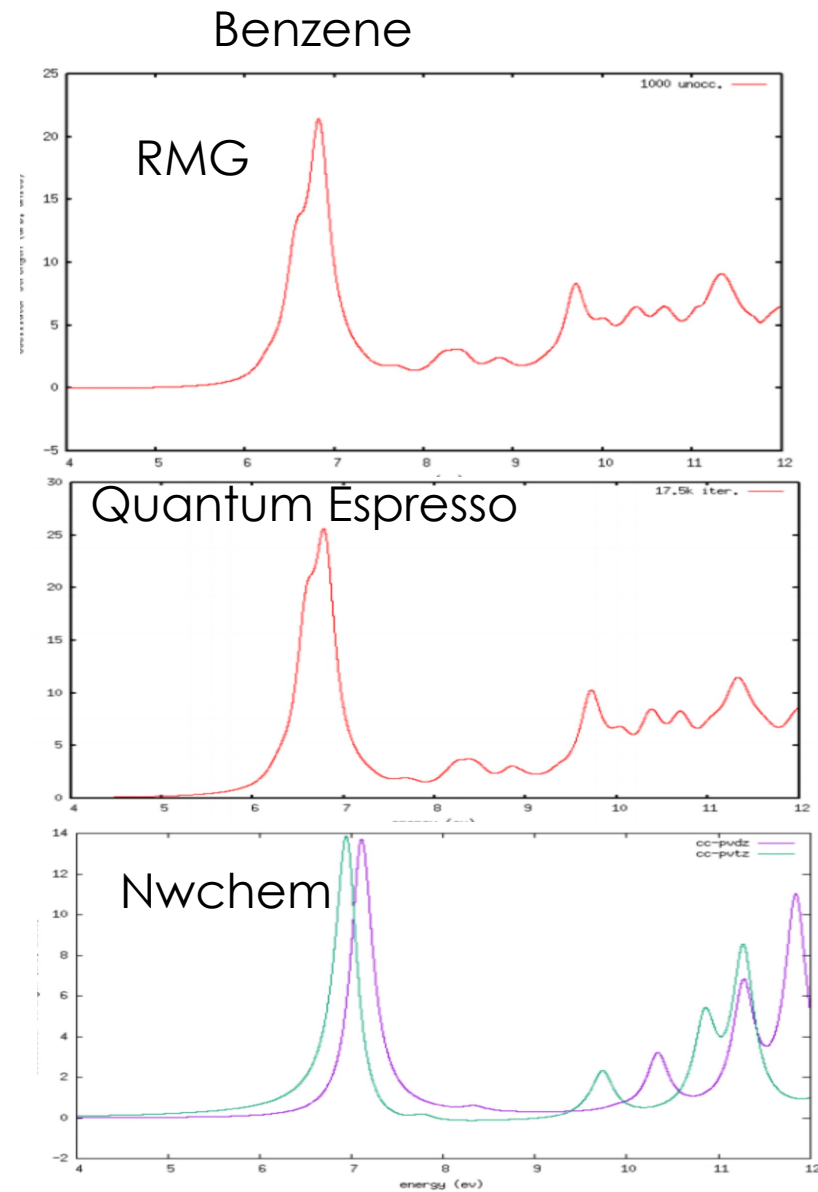
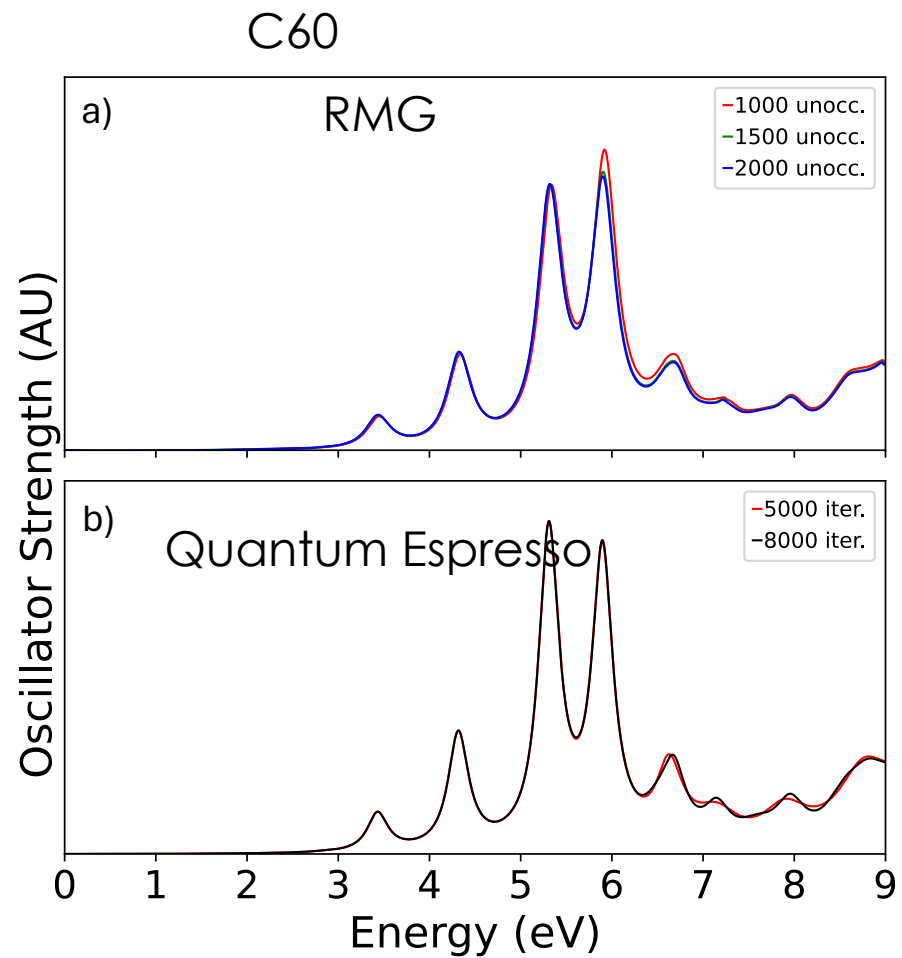
- where operator Ω is from **Magnus expansion**

refs: 1) W. Magnus, Commun. Appl. Math 7,649 (1954)

2) J. Oteo, J. Ros, J. Math Physics 41, 3268 (2000)

3) Jakowski, Morokuma J. Chem. Phys. 130, 224106 (2009)

Comparison with other codes



Real time TD-DFT simulations of plasmonic response of Ag nanorod

- **ORNL Frontier nodes:**
CPU: 64 core AMD EPYC,
GPU: 4x Radeon Instinct MI250X,
total 8GPU per node)



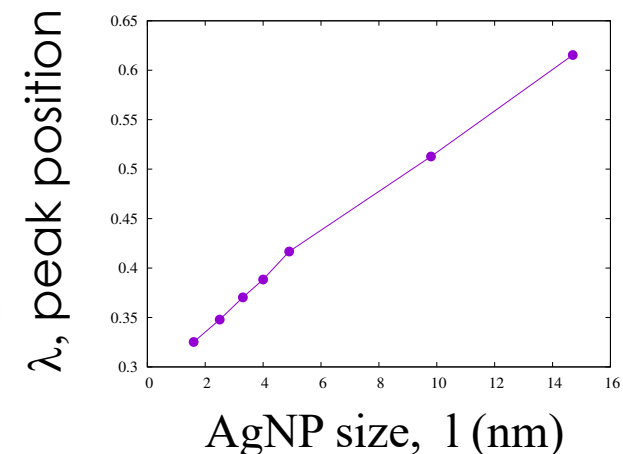
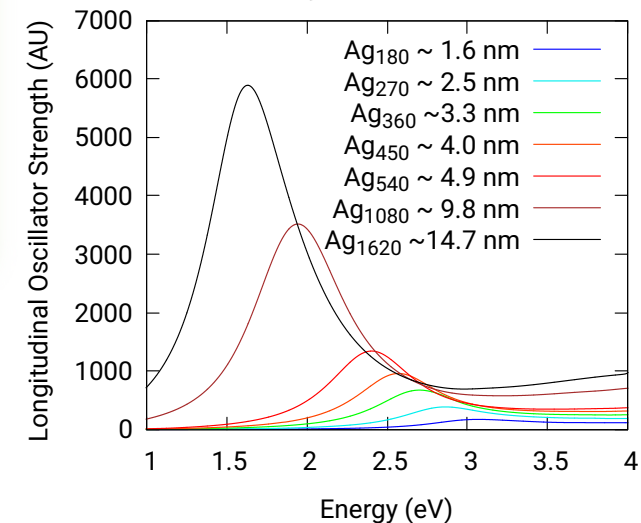
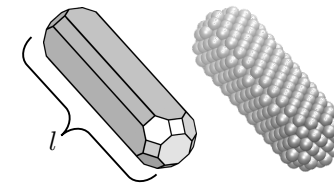
- **System:** Ag nanorod, up 1620 atoms, (17,820 electrons),
semicore (19e) vs frozen core calcs (11e)
- Investigating dipolar longitudinal localized surface plasmon.
2,500 time steps, 0.2 AU time steps (=500 AU),
walltime : **TDDFT: 11s /step**, **SCF: 114 sec/ iteration**
- **Redshifts of plasmon resonance peak with increasing size as expected.**

Empirical expression for plasmon peak position

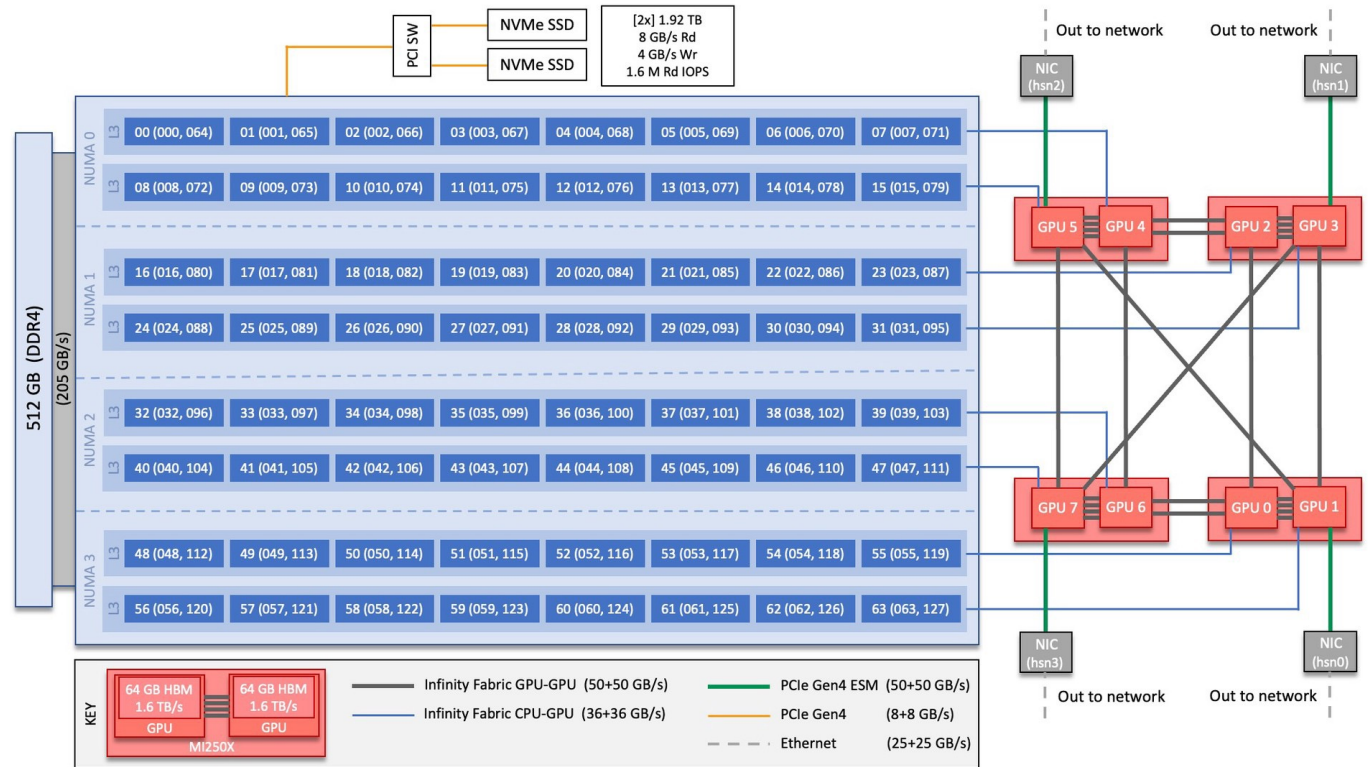
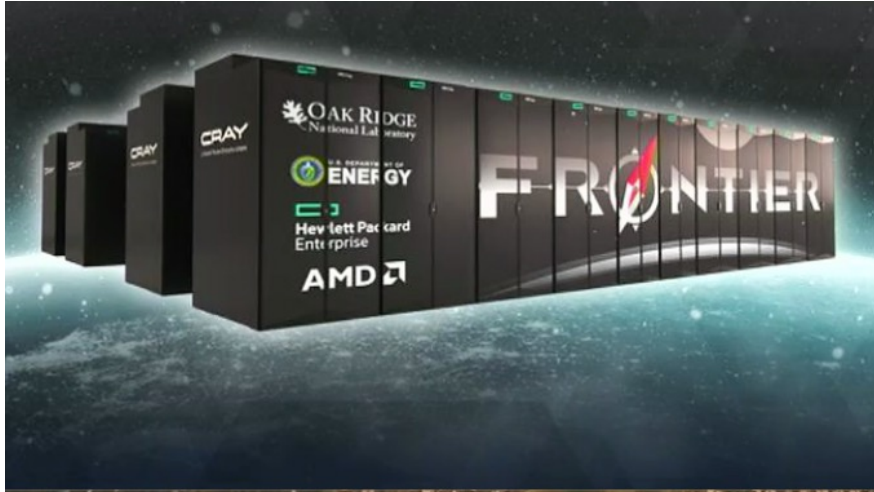
$$\lambda = \lambda_0 + k \cdot l$$

where

$$\lambda = 1/\omega$$



Frontier



Frontier:

- 9,408 AMD compute nodes
- Hybrid CPU/GPU

Compute node:

- 64-core AMD "Optimized 3rd Gen EPYC" CPU
- Memory: 512 GB
- 4x accelerators AMD Radeon Instinct MI250X
- 8X GPUs per node
- 9,408 AMD compute nodes.

GPU accelerators:

- 4x AMD Radeon Instinct MI250X
- 2x GPU /accelerator
- 14,080 cores
- 128 GB
- 1000 Mhz
- 6nm tech

Acknowledgment

- ORNL



- **Jingsong Huang**
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- **David Lingerfelt**
- **Bobby G. Sumpter**
- **David S. Sholl**

- University of South Carolina



- **Sonya Garashchuk**
- **Vitaly Rassolov**

- North Carolina State University (RMG-DFT)

- **Jerry Bernholc**
- **Wenchang Lu**
- **Emil Briggs**

Spallation Neutron Source (SNS) & Center for Nanophase Material Science (CNMS)



This work was performed at the Center for Nanophase Materials Sciences, a U.S. Department of Energy Office of Science User Facility.