



Transport and *Dispersion* of

Exciton-Polariton

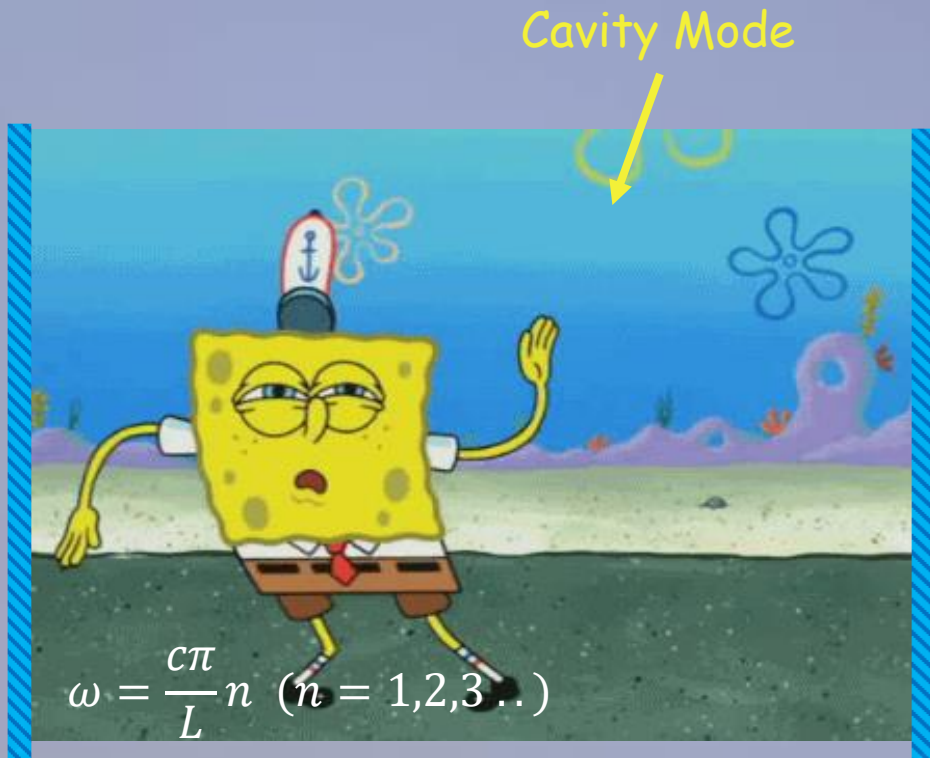
Arkajit Mandal and David R. Reichman

Experiment: Ding Xu and Milan Dilor

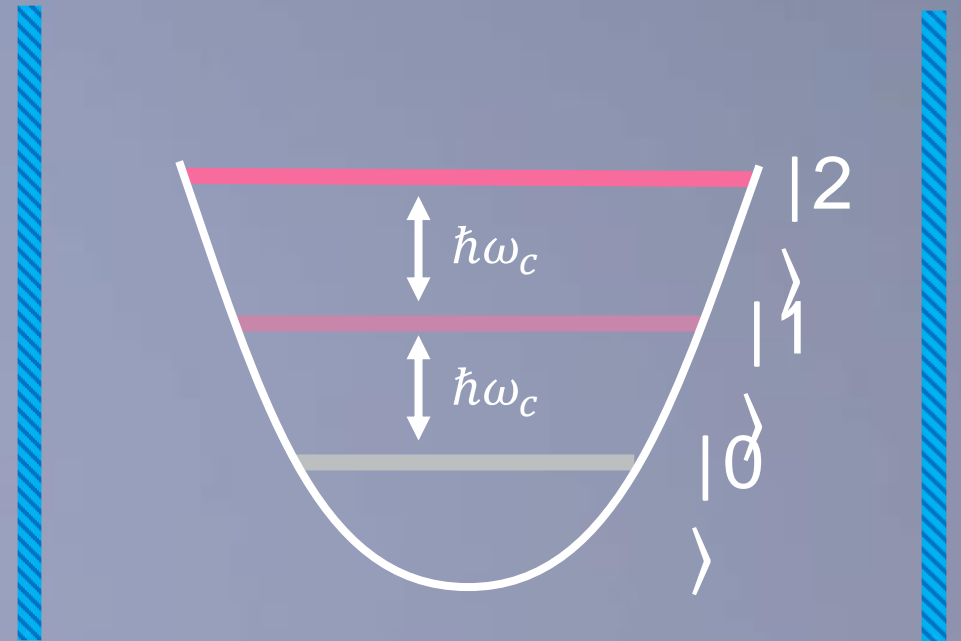
Xu† *Mandal*† Baxter Cheng Lee Su Liu Reichman* Delor*
Arxiv: 2205.01176 (2022) † *Equal*

*Mandal** Xu Mahajan Lee Delor Reichman*
Nano Lett. 2023

A Cavity

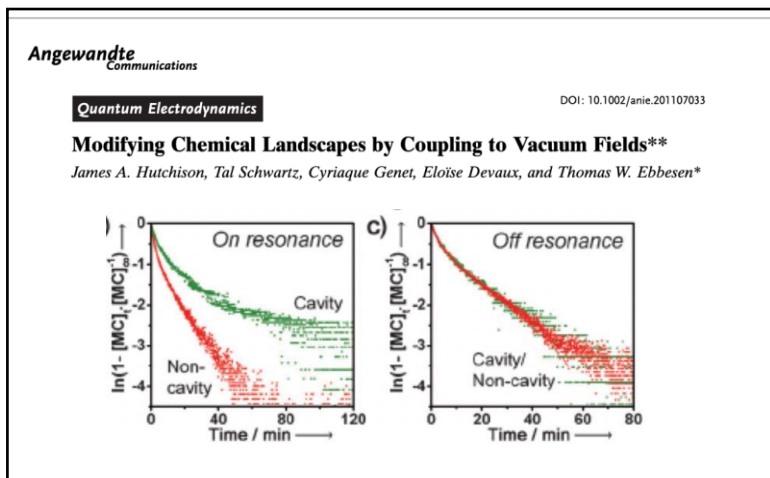


Quantization

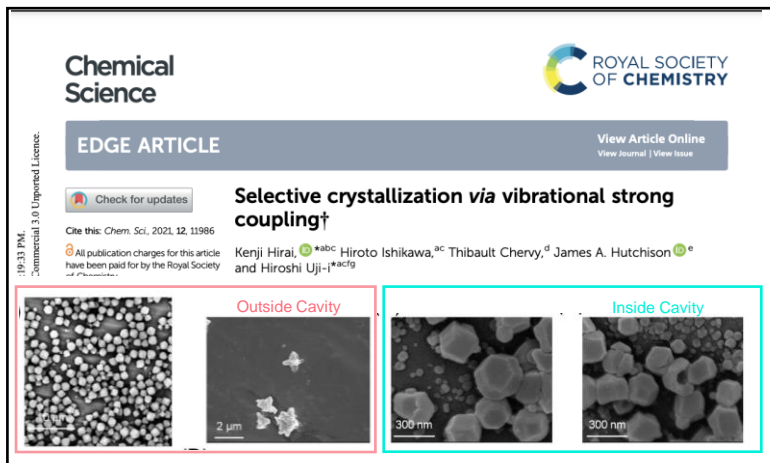


Polaritons

Photochemistry

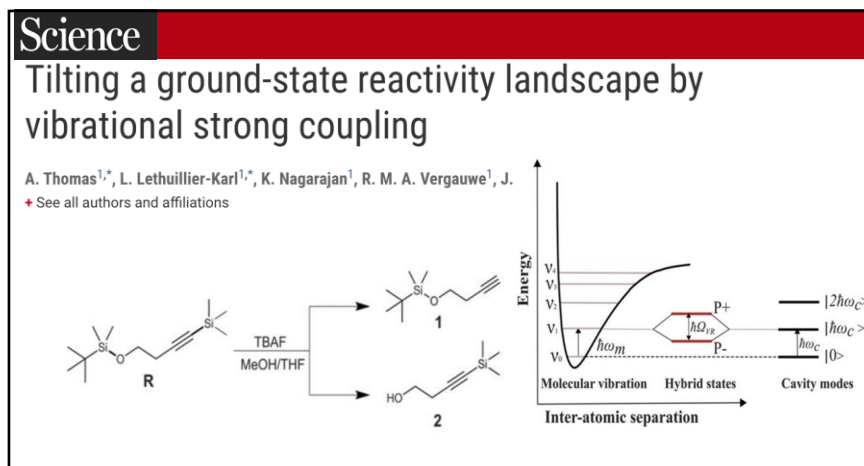


Crystallization

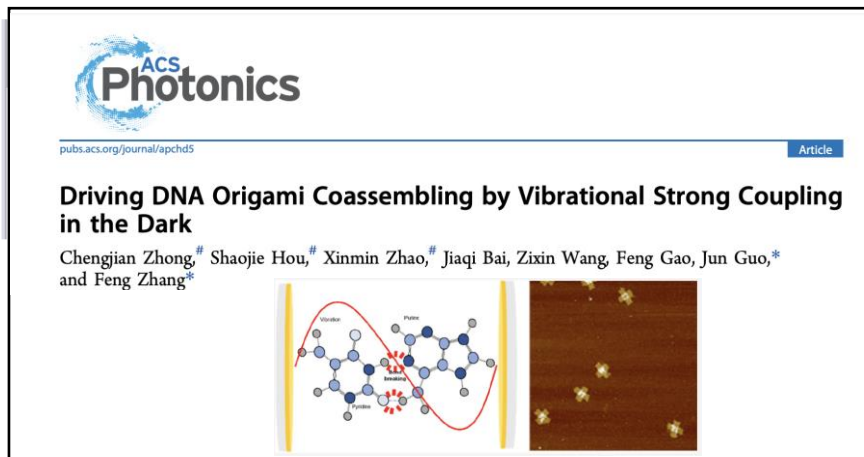


Theoretical Advances in Polariton Chemistry

Rubio (Max Planck), Mukamel (UCI), Huo (Rochester), Yuen-Zhou (UCSD), Herrera (U. Santiago), Groenhoff (U. Jyväskylä), Narang (UCLA), Keeling (St. Andrews), Rebeiro (Emory), Subotnik (UPenn), Feist (UAM), Nitzan (UPenn), Saalfrank (U. Potsdam), Vendrell (Heidelberg), Garcia-Vidal (UAM), Cederbaum (Heidelberg), Koch (NTNU), Kowalewski (Stockholm), Deprince (FSU), Vivok (U. Debrecen), Hammes-Schiffer (Yale), Scholes (Princeton), Foley (UNCC) and many more groups



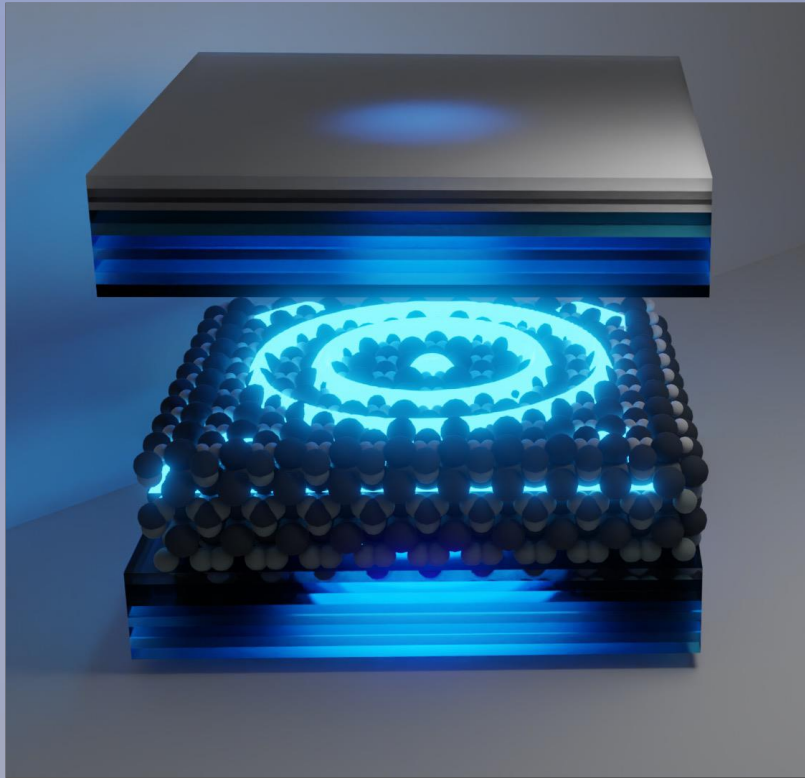
Chemical Kinetics



Biophysics

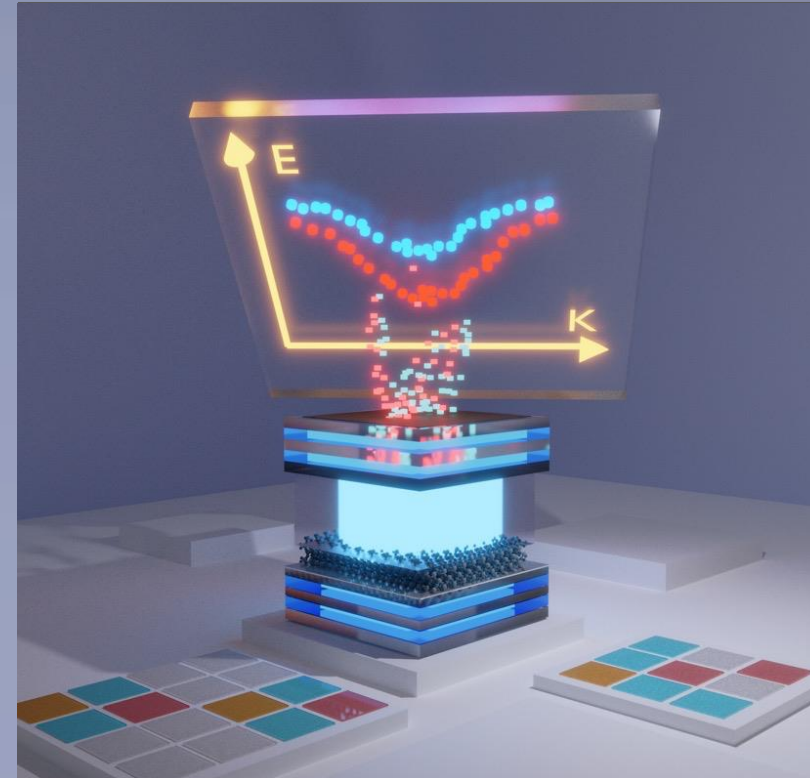
Experiments in Polariton Chemistry/Physics

Ebbesen (Strasbourg), Xiong (UCSD), Menon (CCNY), Schwartz (Tel Aviv), Giebink (Penn), George (IISER-M), Simpkins (NRL), Baumberg (St. Andrews), Vamivakas (Rochester), Krauss (Rochester), Haran (Weizmann), Witchman (Princeton), XYZ (Columbia), Delor (Columbia), Musser (Cornell) many more group...



Exciton-Polariton *Transport*

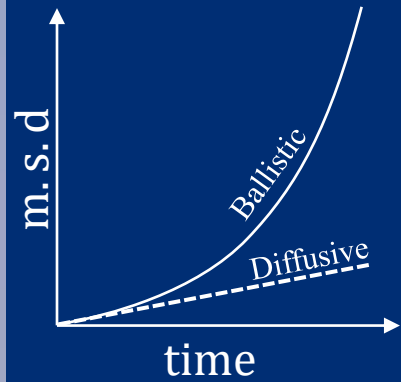
Xu[†] Mandal[†] Baxter Cheng Lee Su Liu Reichman* Delor*
Arxiv: 2205.01176 (2022) [†] Equal



Exciton-Polariton *Dispersion*

Mandal* Xu Mahajan Lee Delor Reichman*
Nano Lett. 2023

1



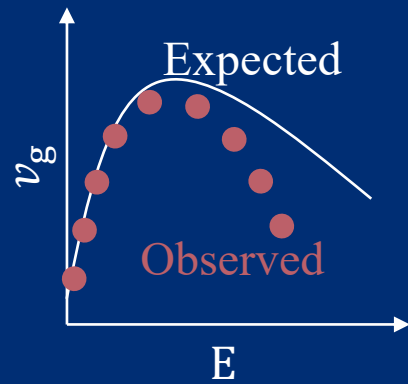
Introduce the key concepts
Coherent and Incoherent
Transport

2

$$\hat{c}\hat{a}^\dagger + \hat{c}^\dagger\hat{a}$$

Light-Matter
Interactions

3

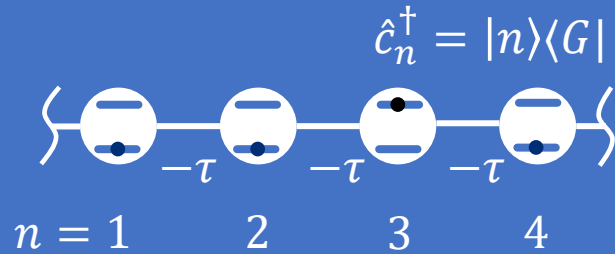


Simulation of Exciton
Polariton Transport
Ballistic and Diffusive
motion of Exciton-Polariton
Experiment + Theory

4



Microscopic theory of
Dispersion
Experiment + Theory



$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

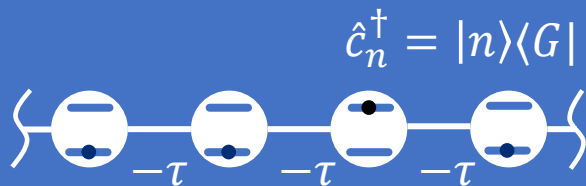
$$|k\rangle = \frac{1}{\sqrt{N}} \sum_n e^{ikn} |n\rangle \quad \hat{c}_k = \frac{1}{\sqrt{N}} \sum_n e^{ikn} \hat{c}_n$$

$$\hat{H}_{1D} |k\rangle = (\epsilon_0 - 2\tau \cos k) |k\rangle$$

$$\hat{H}_{1D} = \sum_k (\epsilon_0 - 2\tau \cos k) \hat{c}_k^\dagger \hat{c}_k = \sum_k \epsilon_k \hat{c}_k^\dagger \hat{c}_k$$

A set of two level systems with nearest neighbor coupling.

1D Exciton (Group Velocity)

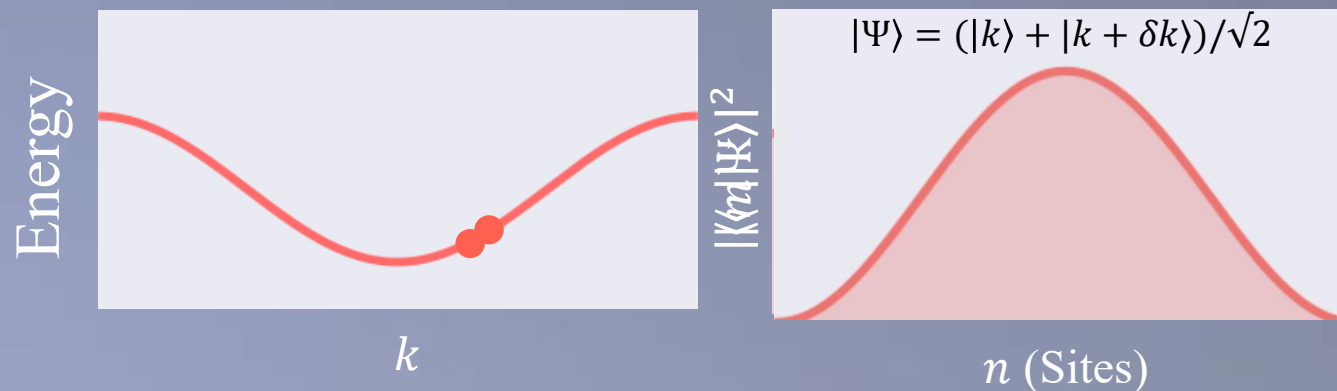


$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

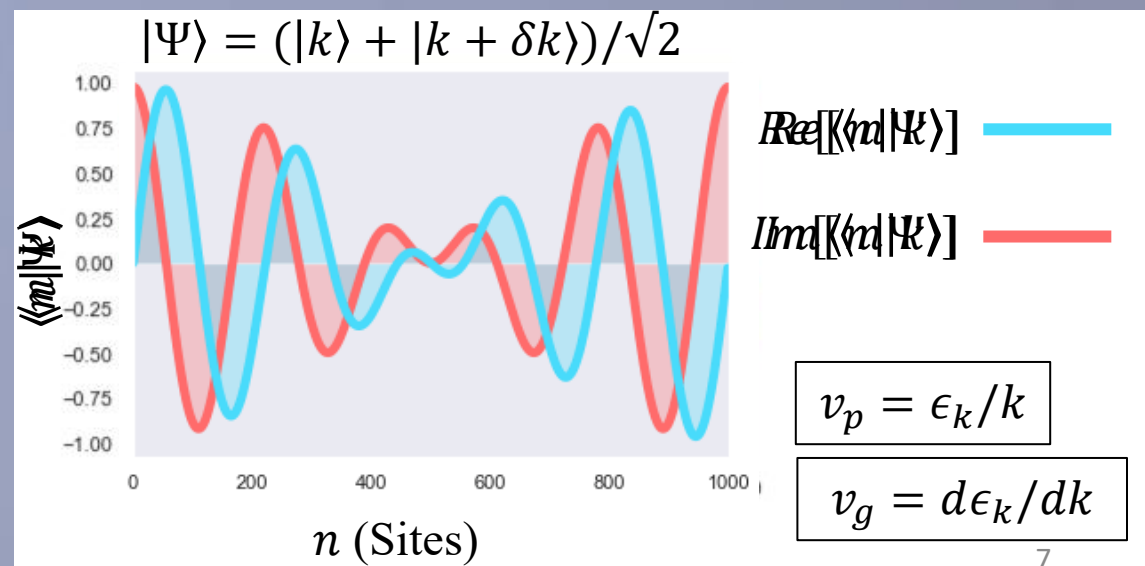
$$|k\rangle = \frac{1}{\sqrt{N}} \sum_n e^{ikn} |n\rangle \quad \hat{c}_k = \frac{1}{\sqrt{N}} \sum_n e^{ikn} \hat{c}_n$$

$$\hat{H}_{1D} |k\rangle = (\epsilon_0 - 2\tau \cos k) |k\rangle$$

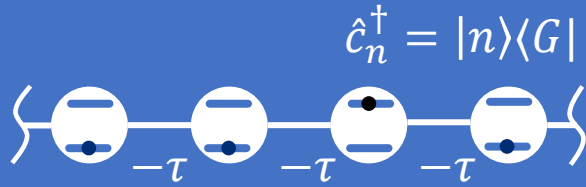
$$\hat{H}_{1D} = \sum_k (\epsilon_0 - 2\tau \cos k) \hat{c}_k^\dagger \hat{c}_k = \sum_k \epsilon_k \hat{c}_k^\dagger \hat{c}_k$$



Eigenfunctions are delocalized in site space.
Localized in reciprocal space.



Ballistic (Coherent) Transport

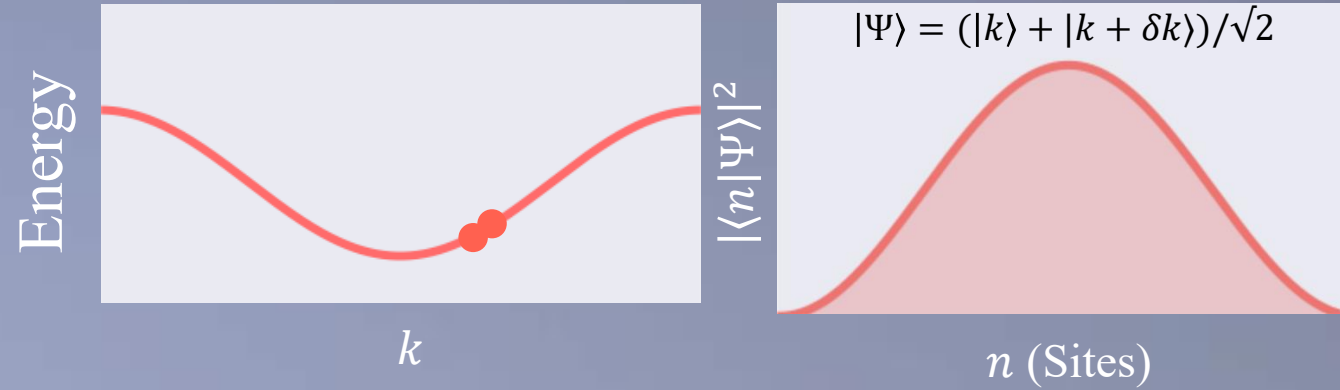


$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

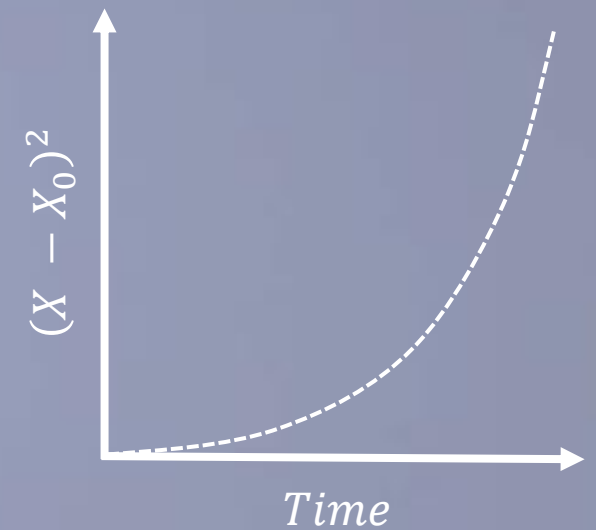
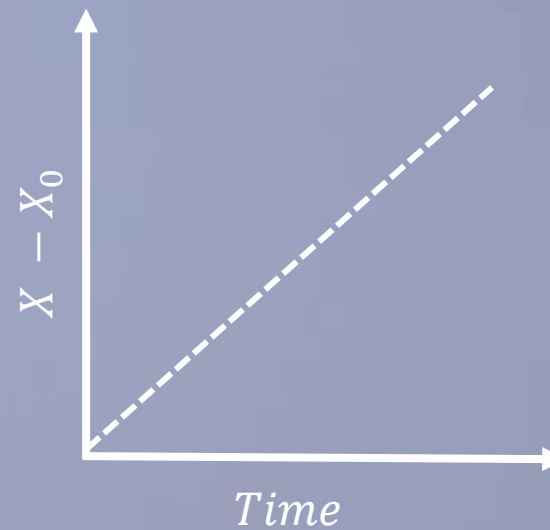
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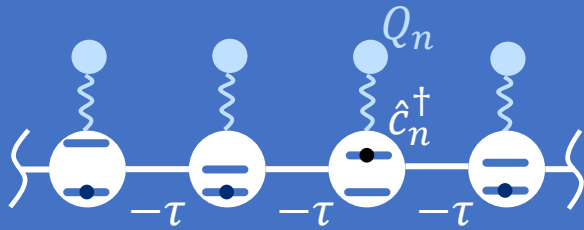
$$\hat{H}_{1D} |k\rangle = (\epsilon_0 - 2\tau \cos k) |k\rangle$$

$$\hat{H}_{1D} = \sum_k (\epsilon_0 - 2\tau \cos k) \hat{c}_k^\dagger \hat{c}_k = \sum_k \epsilon_k \hat{c}_k^\dagger \hat{c}_k$$



Ballistic (Coherent) Motion



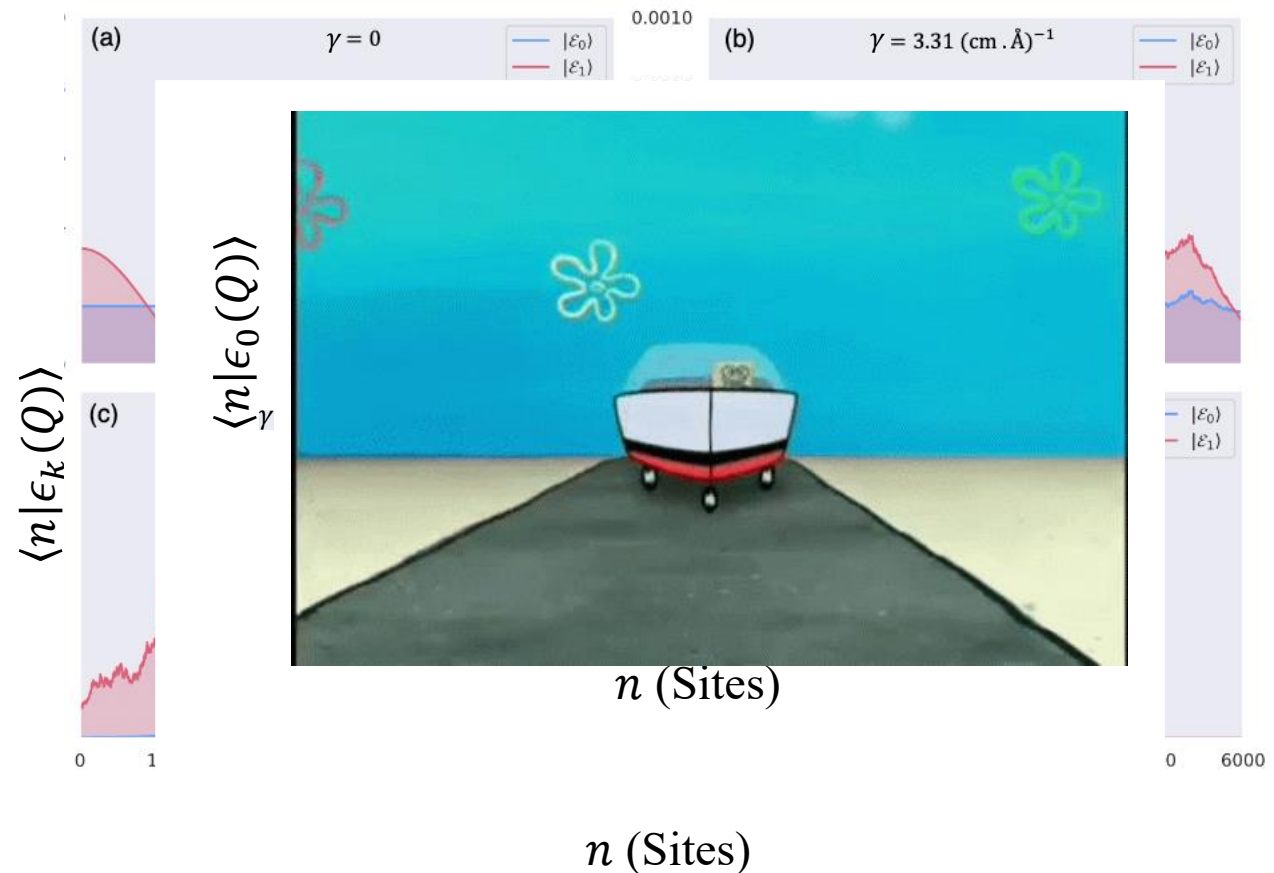


$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1}) + \gamma \sum_n Q_n \hat{c}_n^\dagger \hat{c}_n + \frac{1}{2} \sum_n (P_n^2 + \omega_p^2 Q_n^2)$$

Electronic Hamiltonian

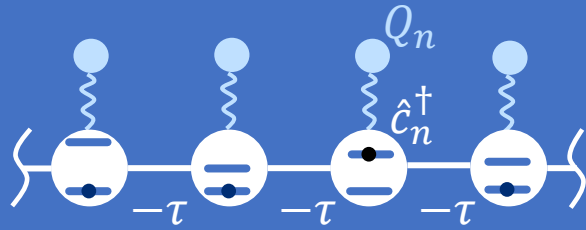
$$\hat{H}_{el} = \hat{H}_{1D} - \sum_n \frac{P_n^2}{2}$$

$$\hat{H}_{el} |\epsilon_k(\mathbf{Q})\rangle = \epsilon_k(\mathbf{Q}) |\epsilon_k(\mathbf{Q})\rangle$$



Phonon fluctuation leads to energetic disorder which leads to localization of eigenstates

This disorder is dynamic, i.e. time-dependent



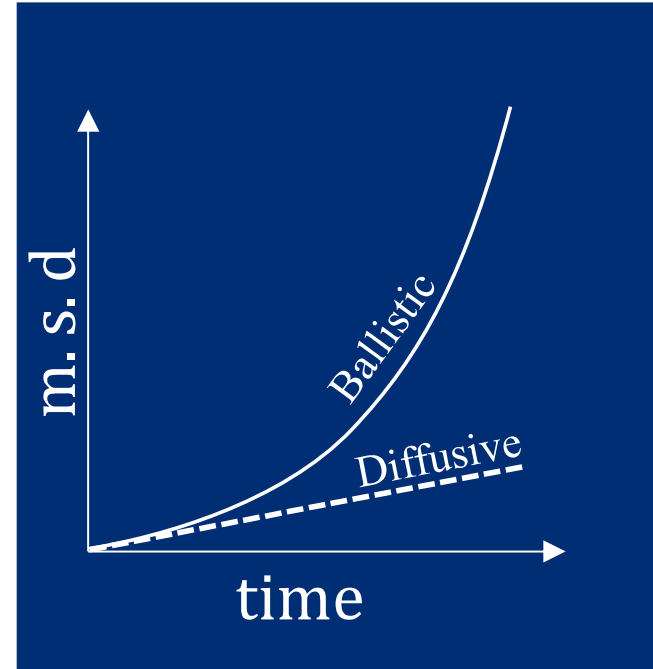
$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

$$+ \gamma \sum_n Q_n \hat{c}_n^\dagger \hat{c}_n + \frac{1}{2} \sum_n (P_n^2 + \omega_p^2 Q_n^2)$$

Electronic Hamiltonian

$$\hat{H}_{el} = \hat{H}_{1D} - \sum_n \frac{P_n^2}{2}$$

$$\hat{H}_{el} |\epsilon_k(Q)\rangle = \epsilon_k(Q) |\epsilon_k(Q)\rangle$$



THE JOURNAL OF CHEMICAL PHYSICS 134, 244116 (2011)

Mixed quantum-classical simulations of charge transport in organic materials: Numerical benchmark of the Su-Schrieffer-Heeger model

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PRL 96, 086601 (2006)

PHYSICAL REVIEW LETTERS

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3 MARCH 2006

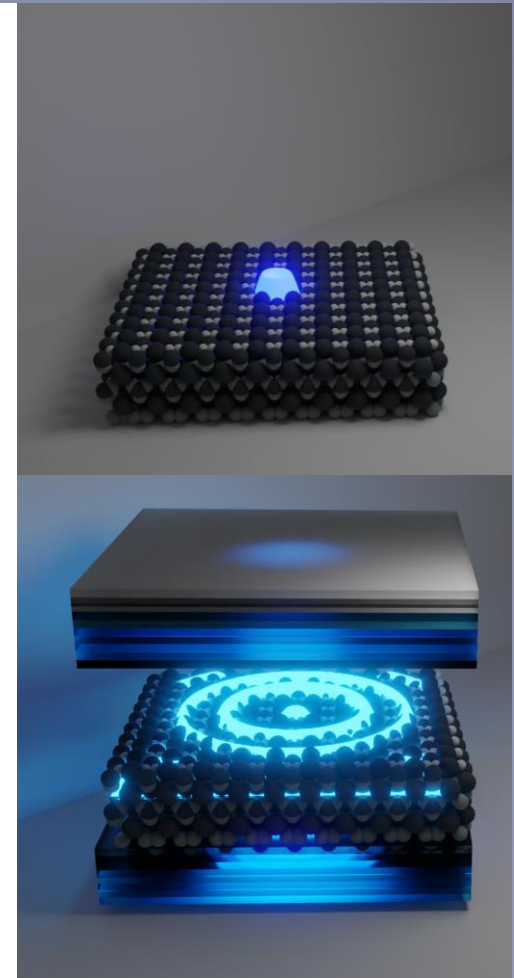
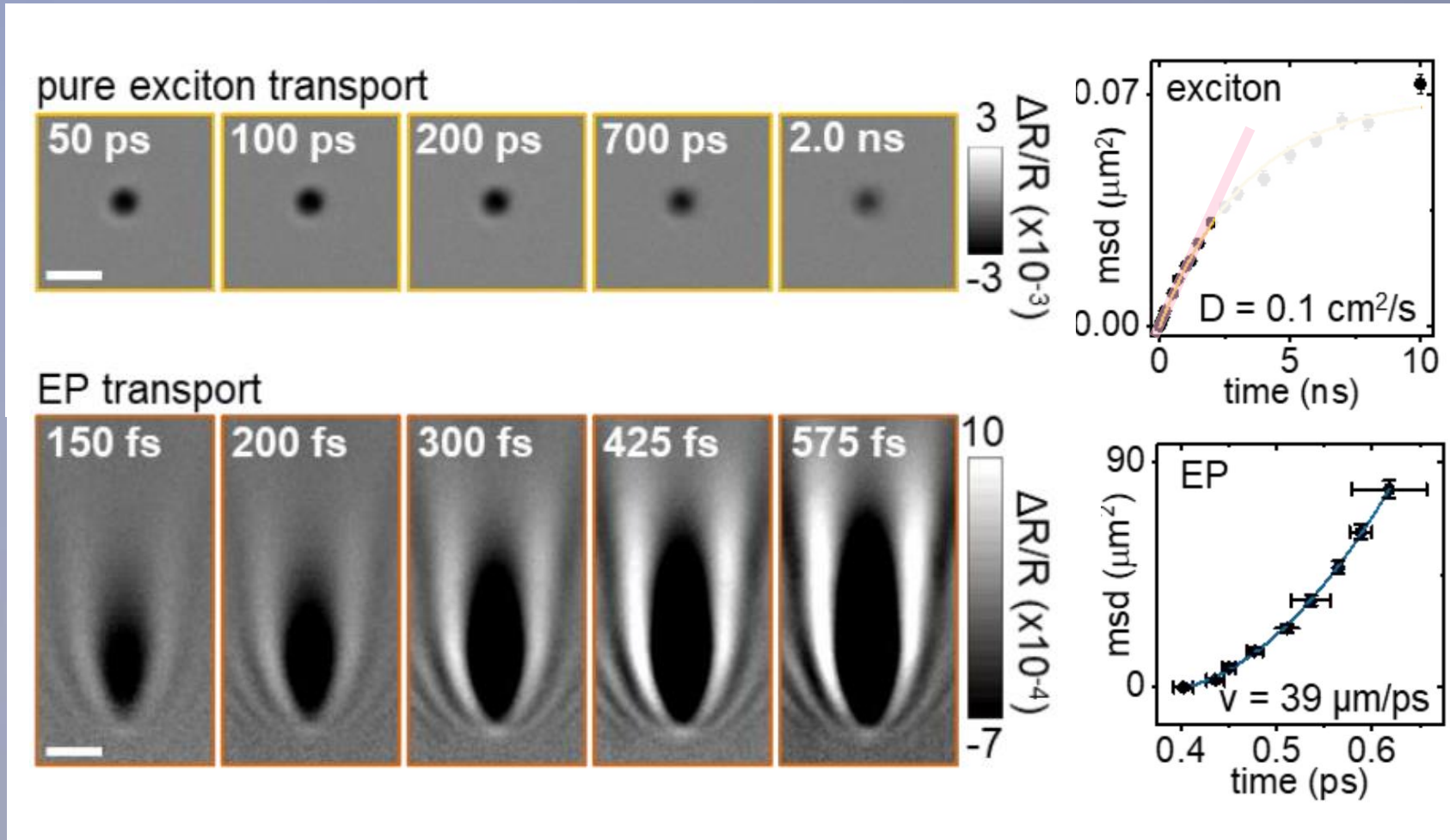
Charge-Transport Regime of Crystalline Organic Semiconductors: Diffusion Limited by Thermal Off-Diagonal Electronic Disorder

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²Dipartimento di Chimica "G. Ciamician," Università di Bologna, via F. Selmi 2, 40126 Bologna, Italy
(Received 23 November 2005; published 3 March 2006)

Exciton-Polariton Transport



Also see:

Pandya et. Al. Adv. Sci. 9, 2105569 (2022)

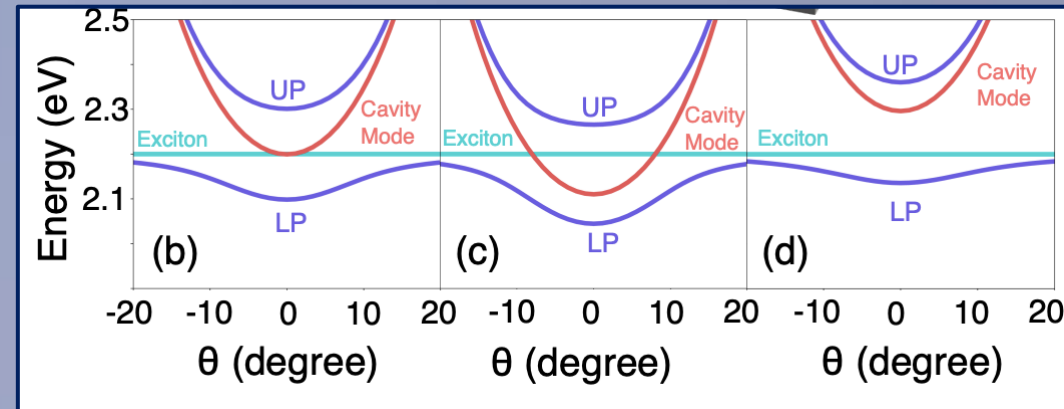
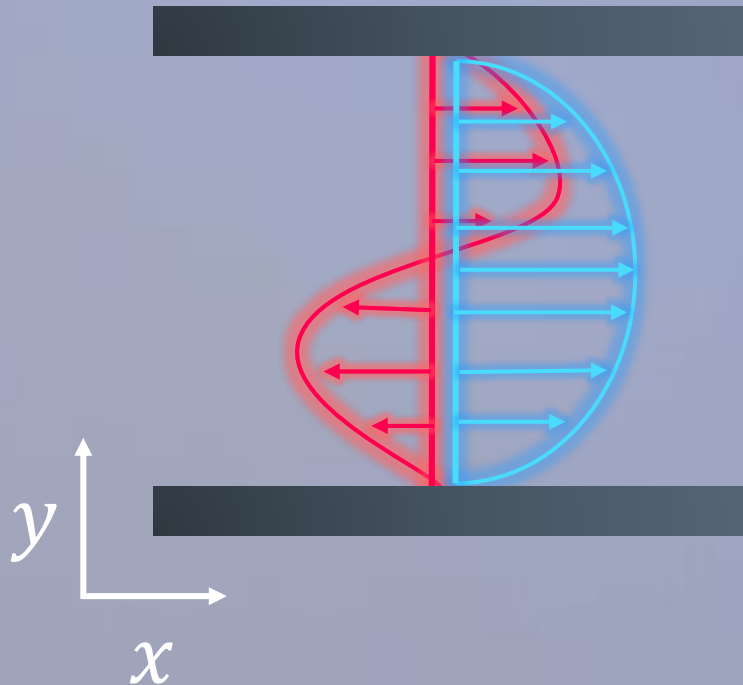
Balasubrahmaniyam et. al. Nat. Matter (2023)

Xu[†], Mandal[†], ..., Milan, Reichman (arXiv: 2205.01176) 2022

$$\hat{H}_{\text{LM}} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1}) + \gamma \sum_n Q_n \hat{c}_n^\dagger \hat{c}_n + \frac{1}{2} \sum_n (P_n^2 + \omega_p^2 Q_n^2)$$

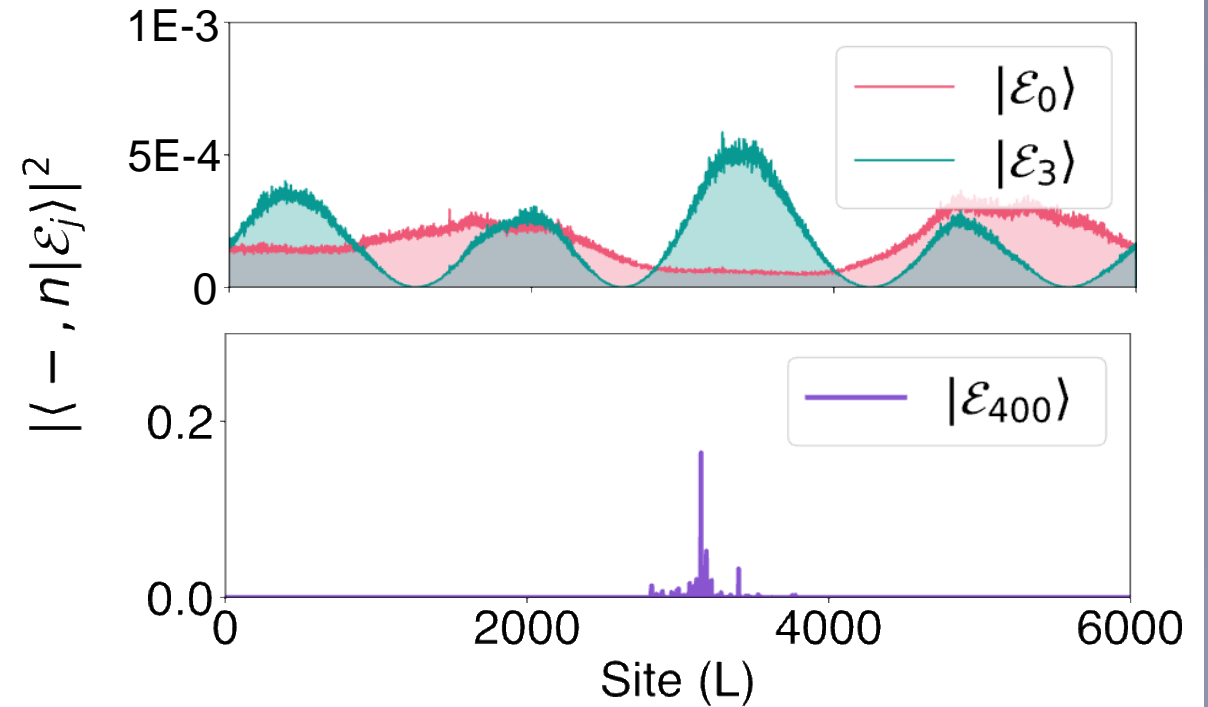
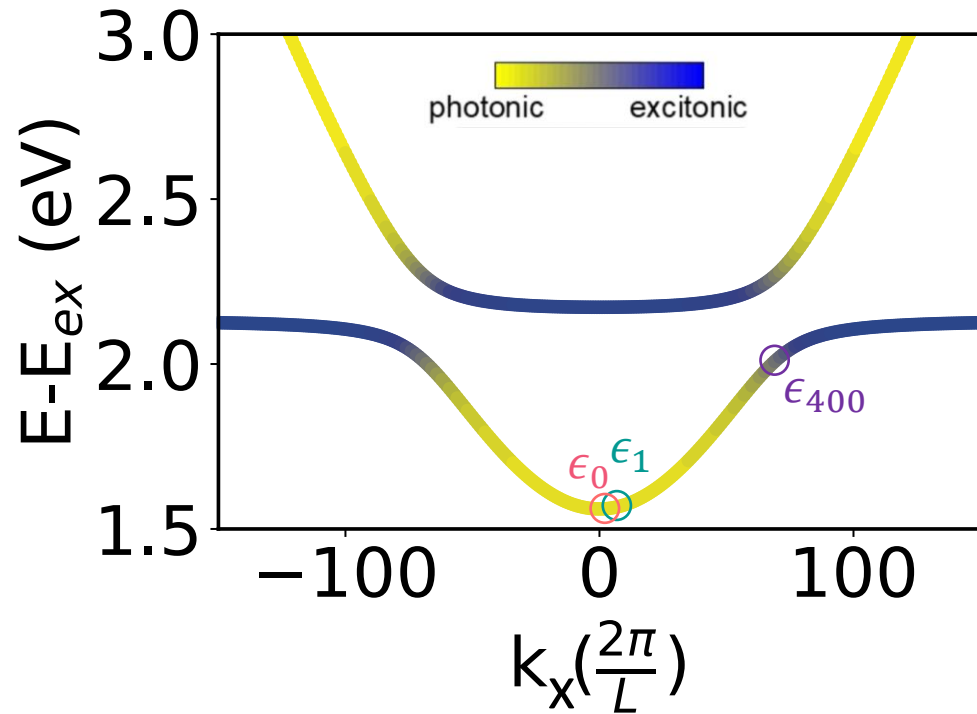
$$+ \sum_{\mathbf{k}} \hat{a}_{\mathbf{k}}^\dagger \hat{a}_{\mathbf{k}} \omega_{\mathbf{k}} + g_c \sum_{n,\mathbf{k}} (\hat{c}_n^\dagger \hat{a}_{\mathbf{k}} e^{ik_x \cdot \mathbf{R}_n} + \hat{a}_{\mathbf{k}}^\dagger \hat{c}_n e^{-ik_x \cdot \mathbf{R}_n}) \sin(k_y \cdot \mathbf{R}_n)$$

Photon Modes



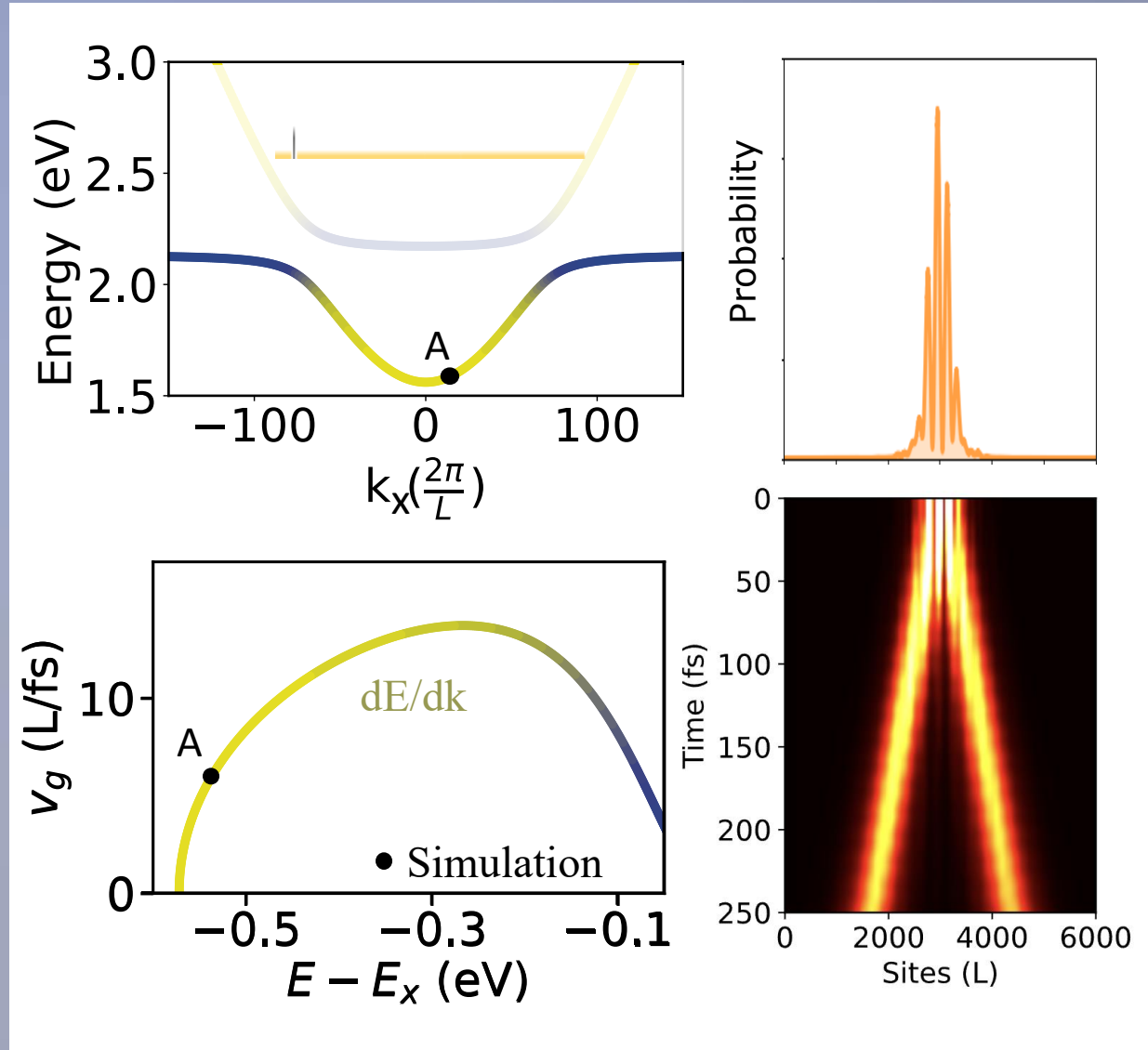
Cavity operators do not couple to phonons. Photon frequency is off-resonant to phonon frequency.

Polaritons, which are **partially** excitonic, have **effectively smaller** coupling to phonons.



Higher Exciton character \rightarrow Higher Phonon Coupling \rightarrow Higher Localization

Group Velocity



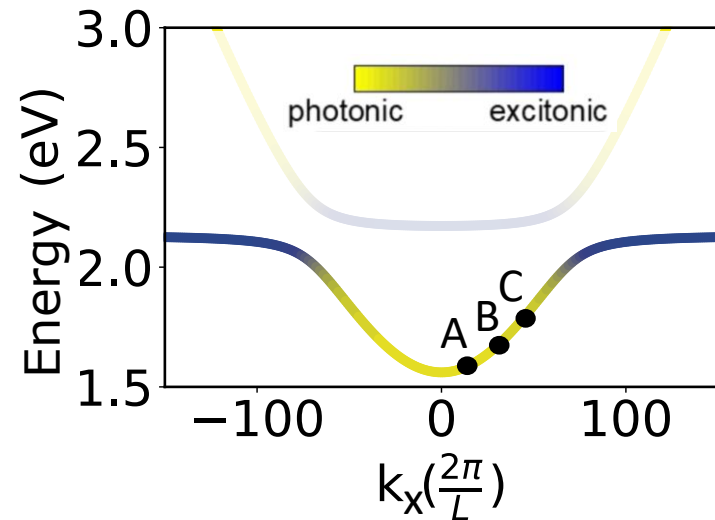
At low exciton character (at large detuning) the exciton-polariton wavepacket **propagates ballistically.**

The wavefront velocity matches the expected group velocity.

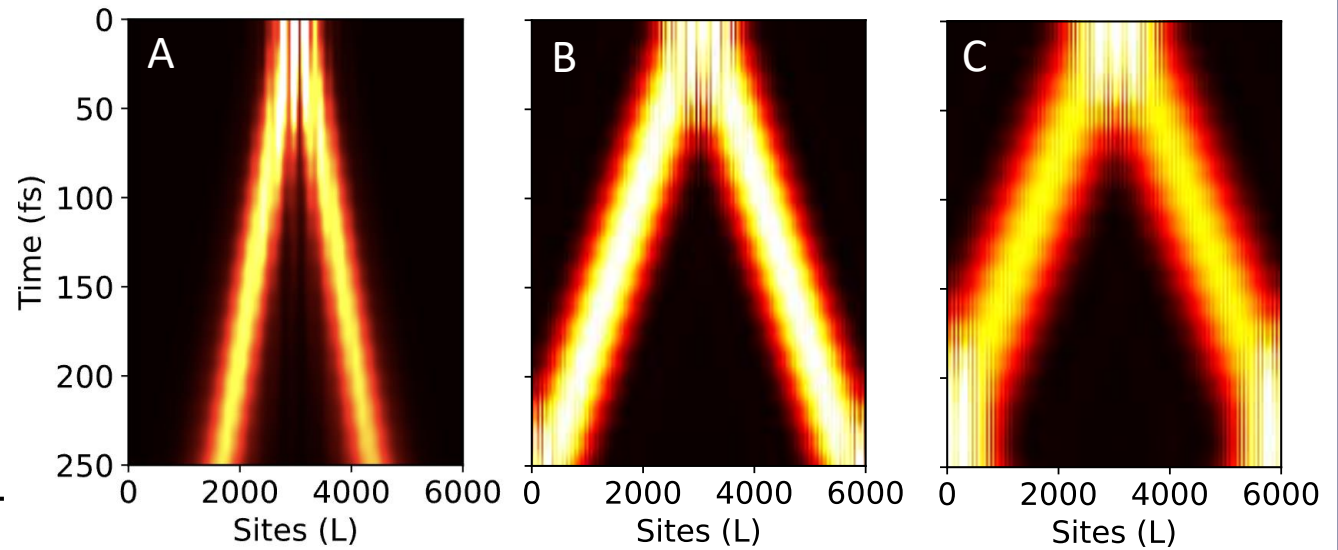
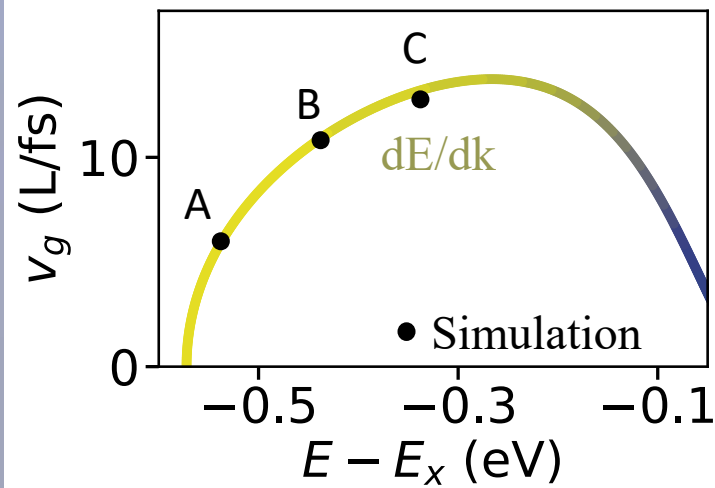
Also see: Berghuis et. Al. ACS photonics 9 (7), 2263-2272

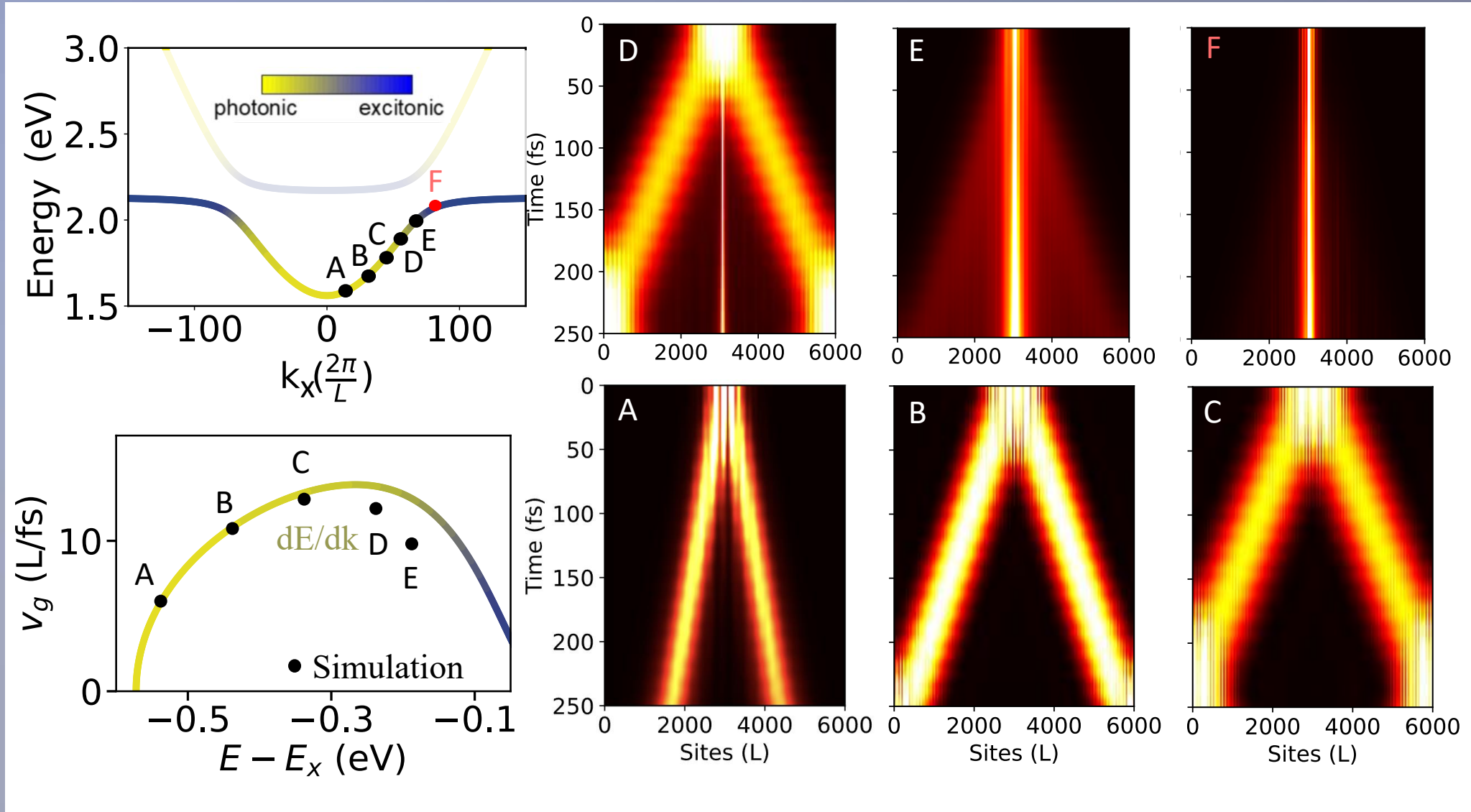
Sokolovskii et. Al. arXiv:2209.07309

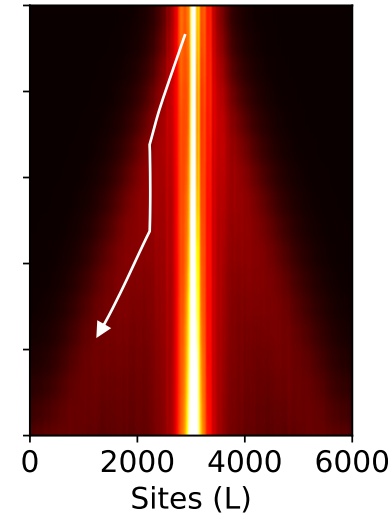
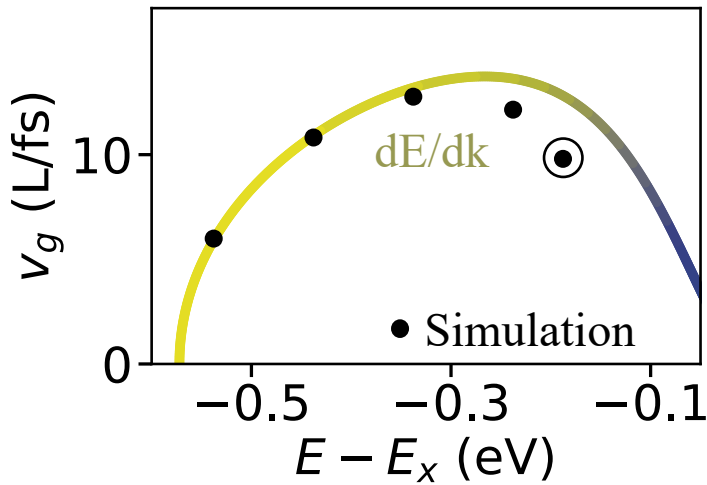
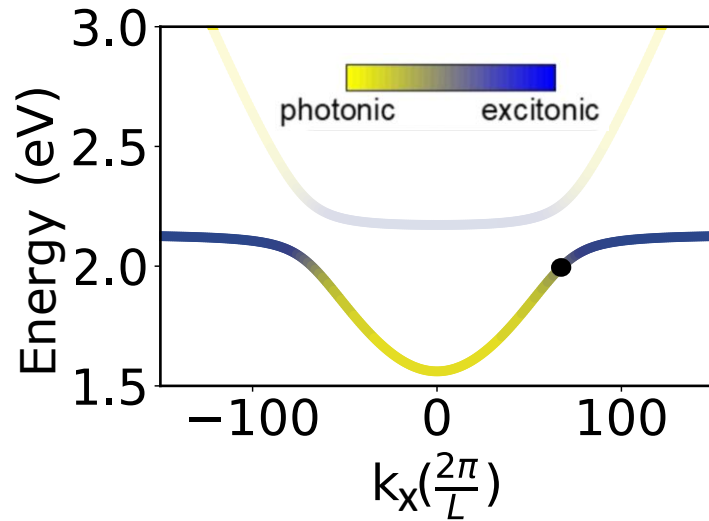
Xu[†], Mandal[†], Milan, Reichman (arXiv: 2205.01176) 2022



The wavefront velocity matches the expected group velocity for exciton character $< 15\%$.

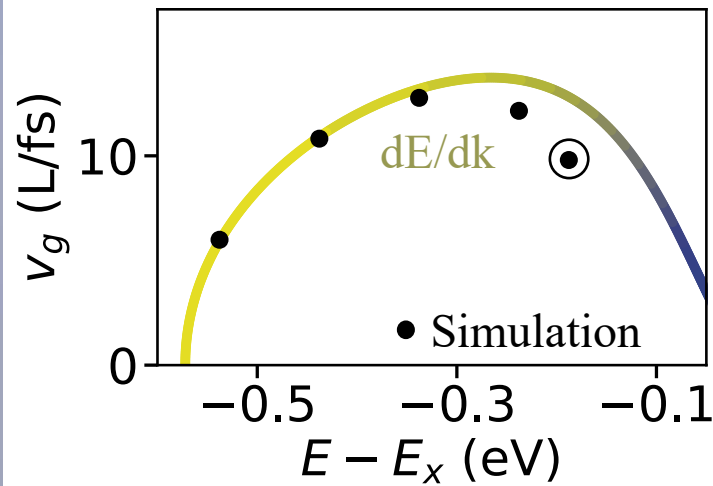
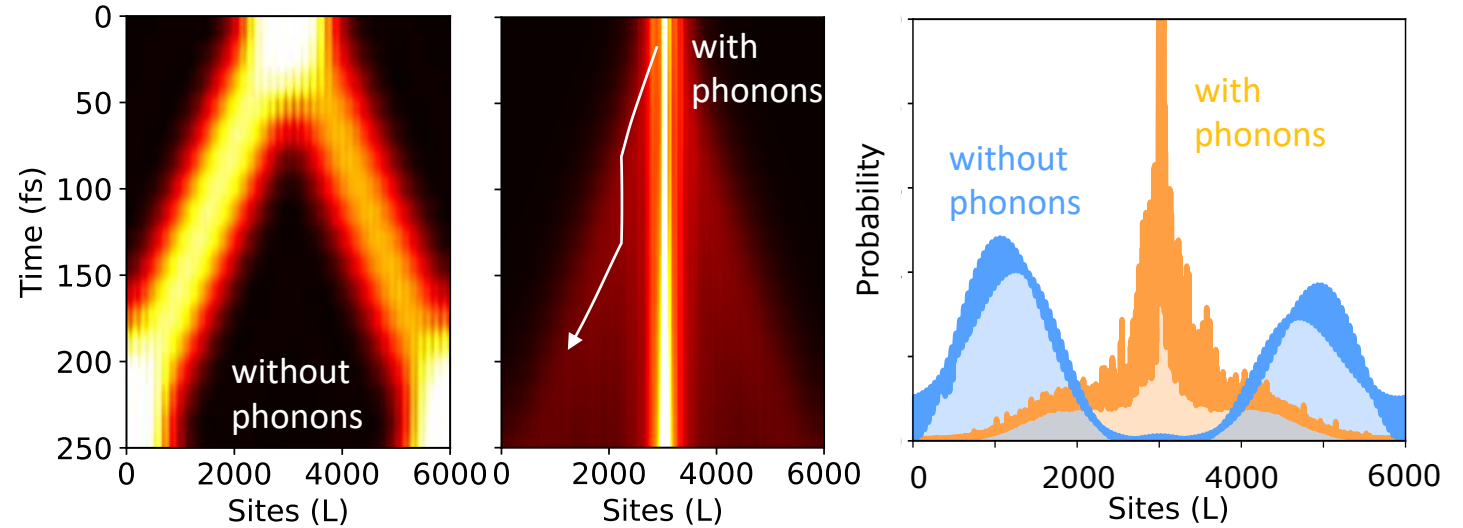
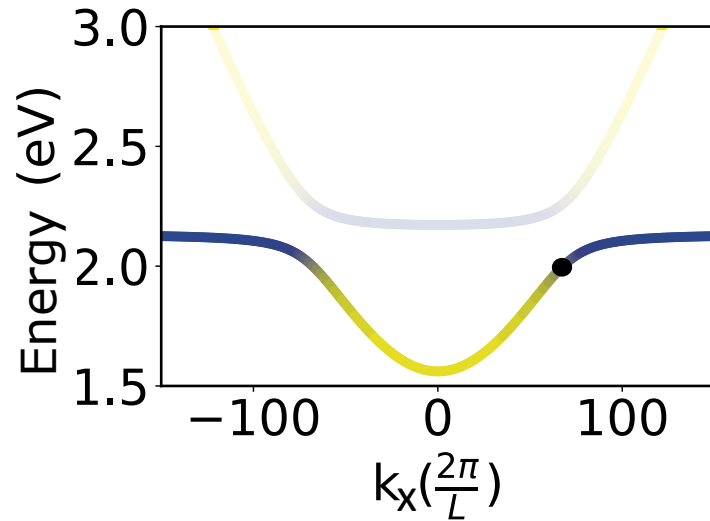




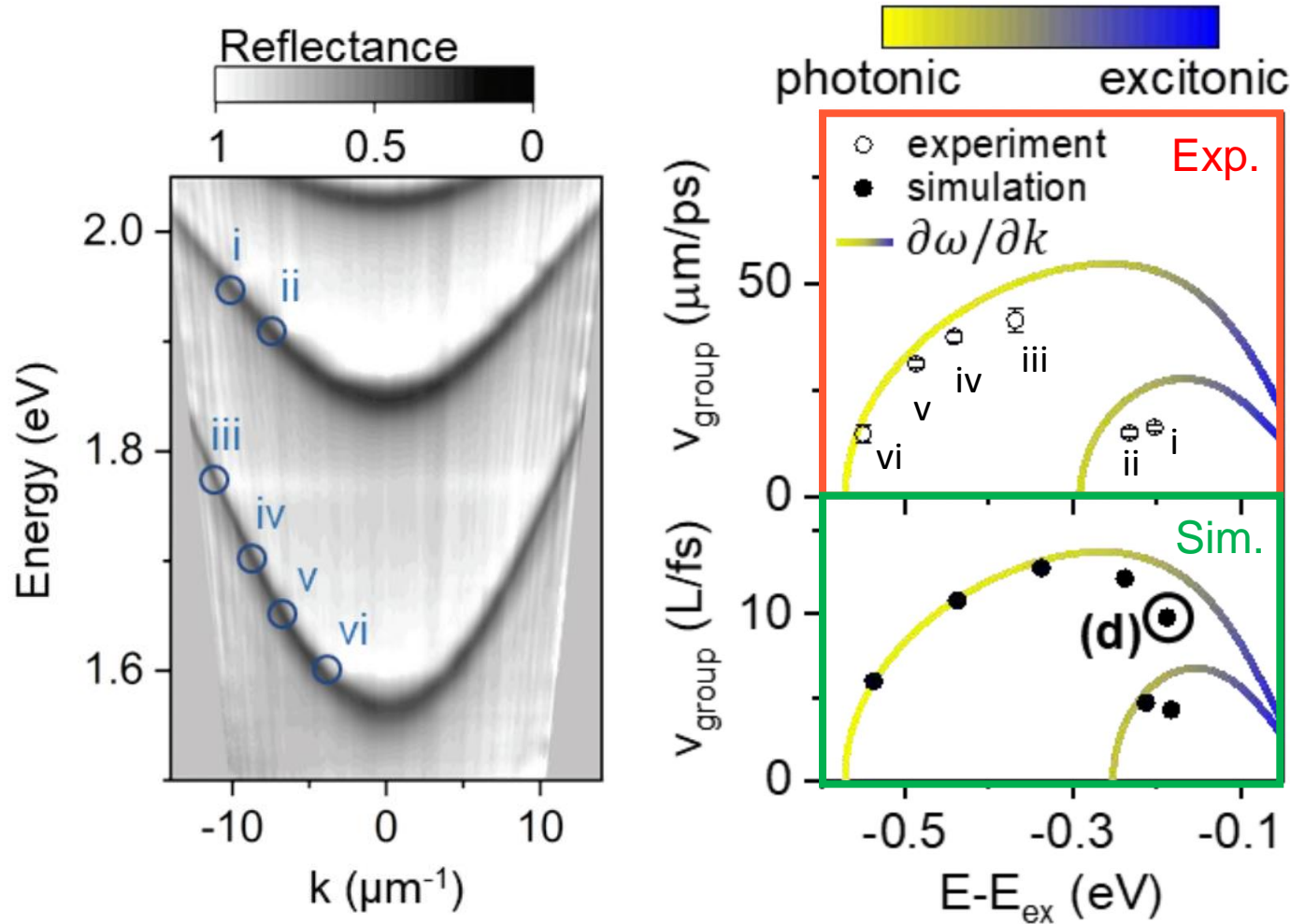


At exciton character 25-40% → Phonons **renormalizes** polariton group velocity

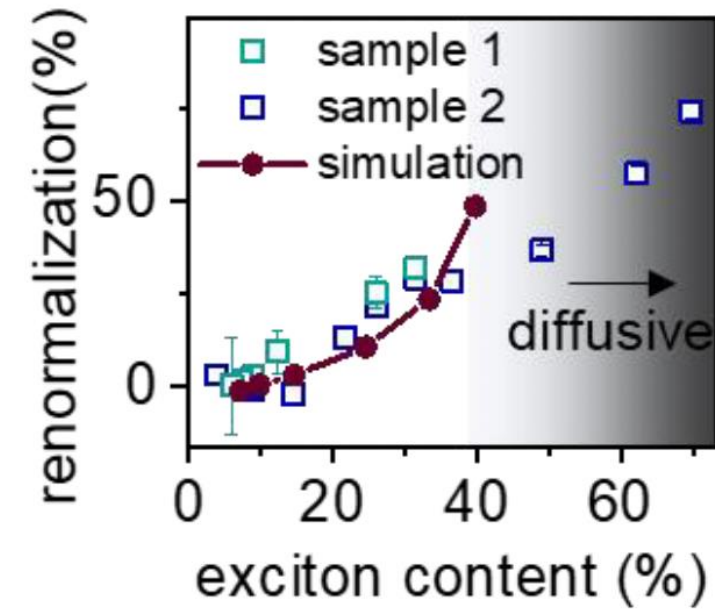
Phonon induced transient localization leads to reduced velocity



We can confirm the renormalization by comparing with a case without phonons.



We experimentally observe the same phenomena.

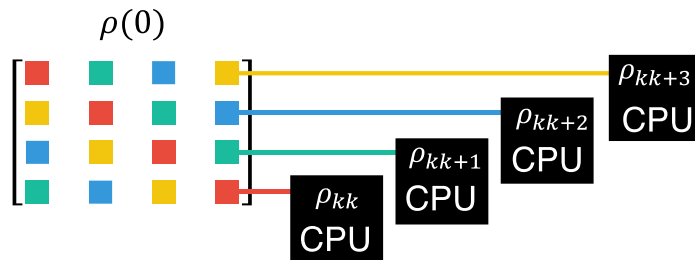


Aim: Simulate a matter system with $\sim 10^4$ sites and 10^2 cavity modes (~ 10000 states)

N^5
↓
 N^4
↓
 N^3
↓
 N^2

$$\dot{\rho}_{k,k+\delta k}(t) = \int_0^t d\tau K_{k,k+\delta k,p,p+\delta k}(t-\tau)\rho_{p,p+\delta k}(t)$$

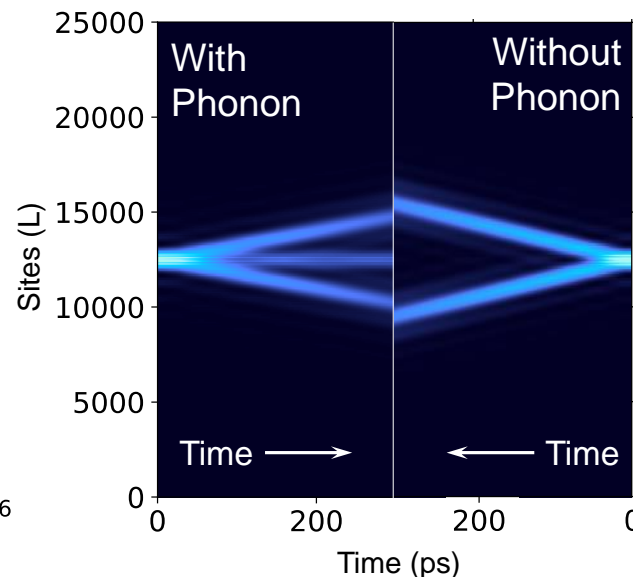
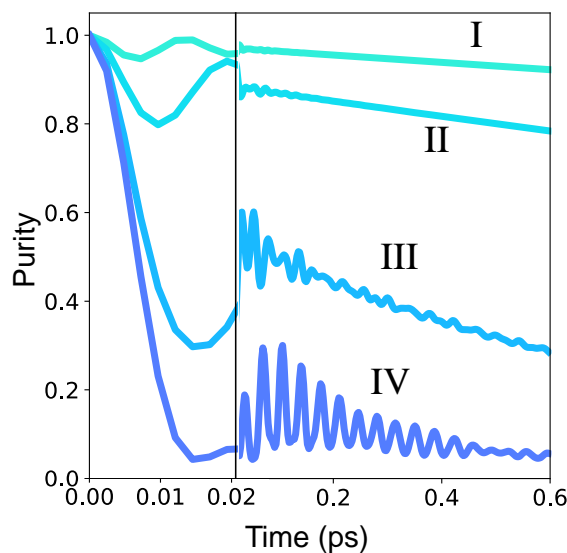
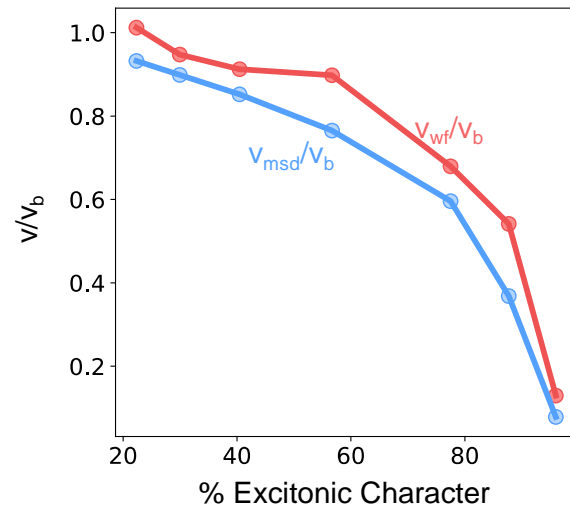
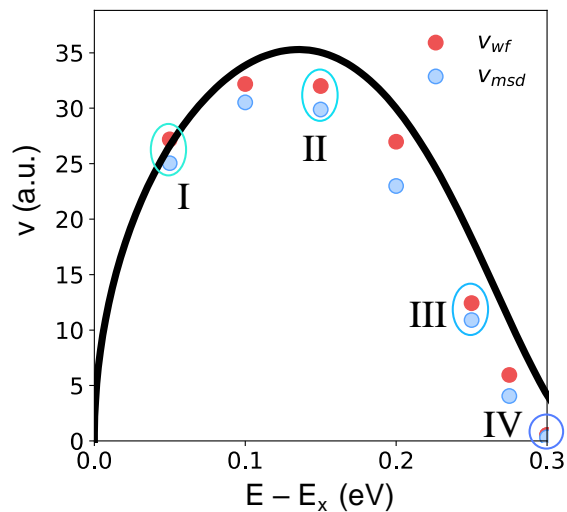
$$K_{k,k',p,p'} = K_{k,k',p,p+(k'-k)}$$



Momentum Conservation makes K a 3-dimensional tensor instead of 4-dimensional

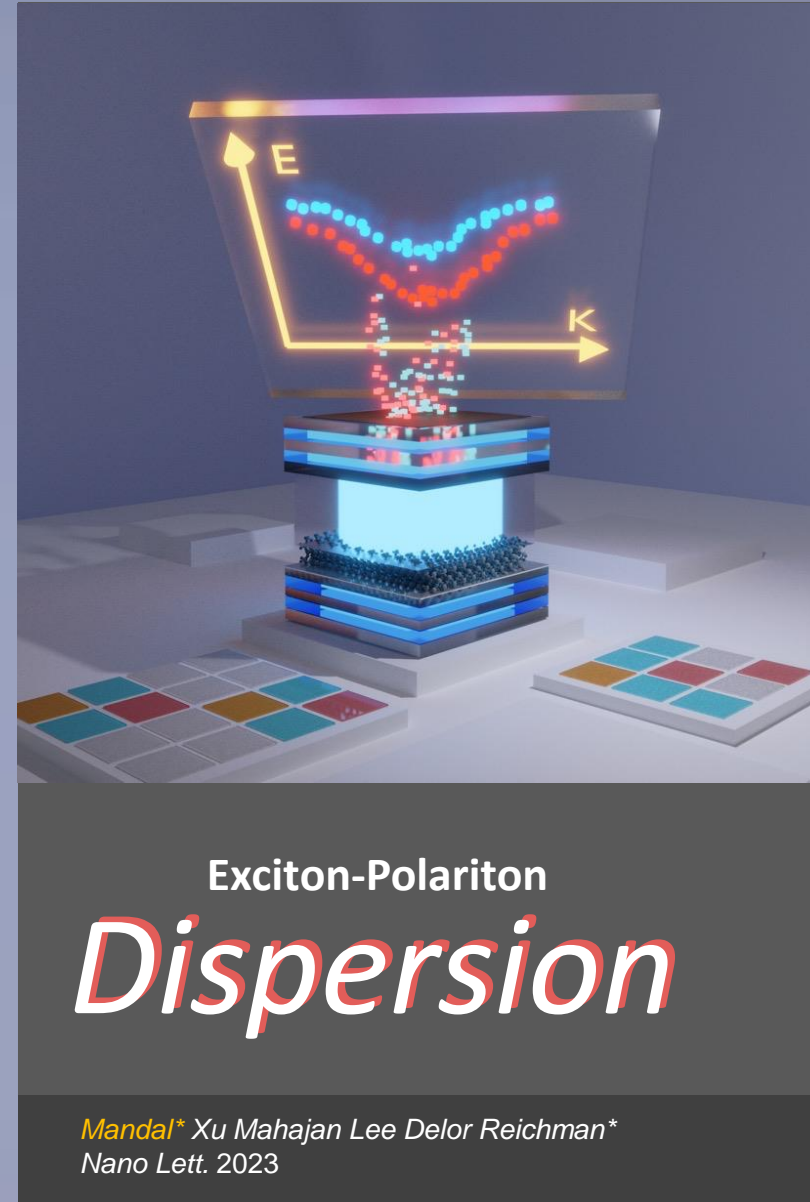
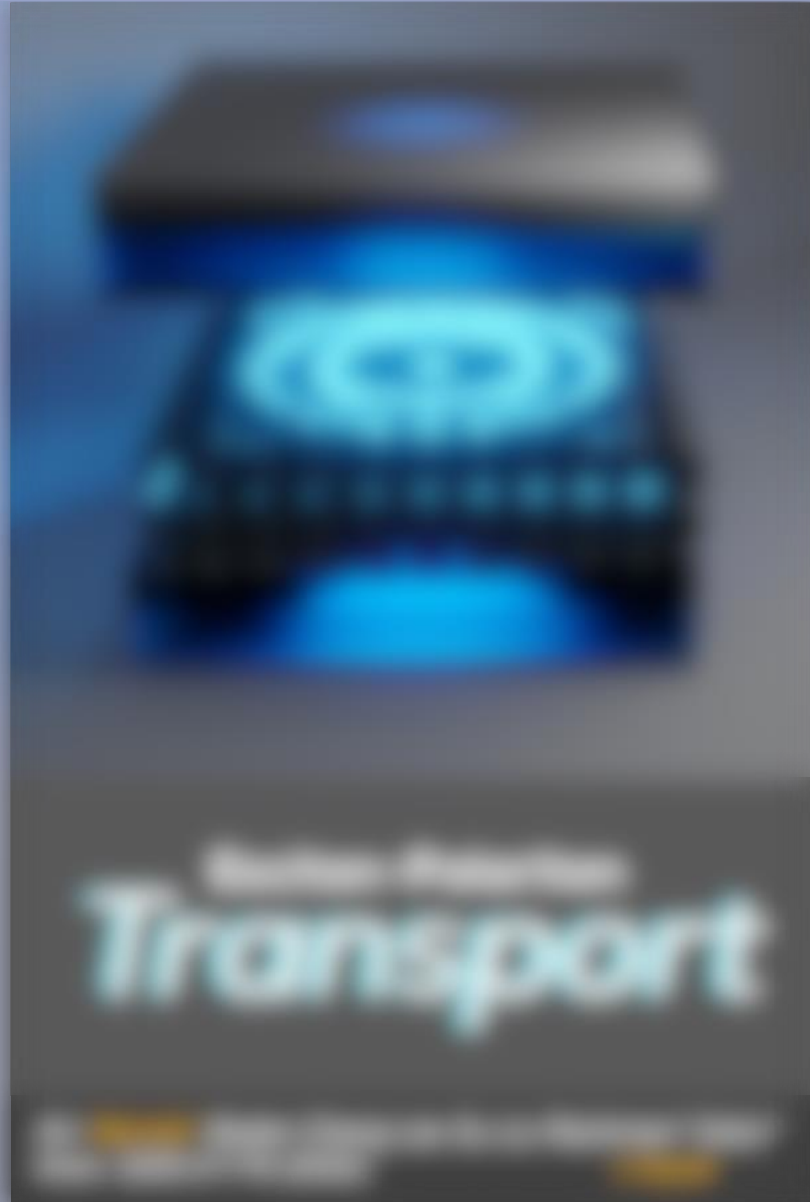
decoupled diagonals of density matrix in the reciprocal space – parallelized simulation

Prony decomposition of memory kernel + Coarse Graining Density Matrix.



Higher purity ==
Coherent.

We perform
Non-Markovian
Master Equation
simulation with
25000 states!

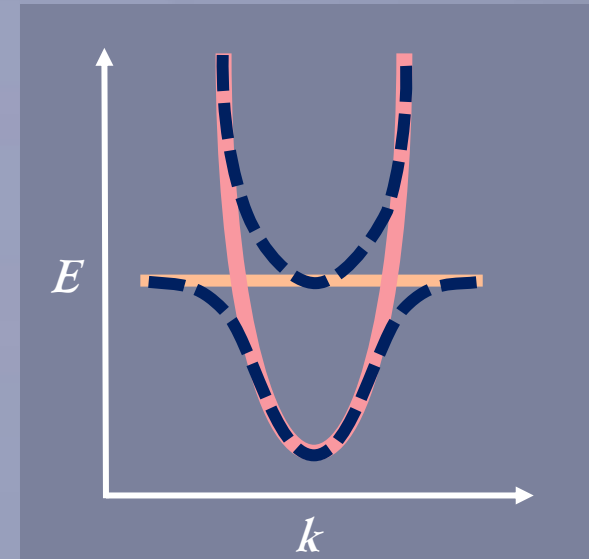


$$\hat{H}_{\text{LM}} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1}) + \sum_{\mathbf{k}} \hat{a}_{\mathbf{k}}^\dagger \hat{a}_{\mathbf{k}} \omega_{\mathbf{k}} + g_c \sum_{n, \mathbf{k}} (\hat{c}_n^\dagger \hat{a}_{\mathbf{k}} e^{i\mathbf{k}_{\parallel} \cdot \mathbf{R}_n} + \hat{a}_{\mathbf{k}}^\dagger \hat{c}_n e^{-i\mathbf{k}_{\parallel} \cdot \mathbf{R}_n}) \sin(\mathbf{k}_{\perp} \cdot \mathbf{R}_n)$$

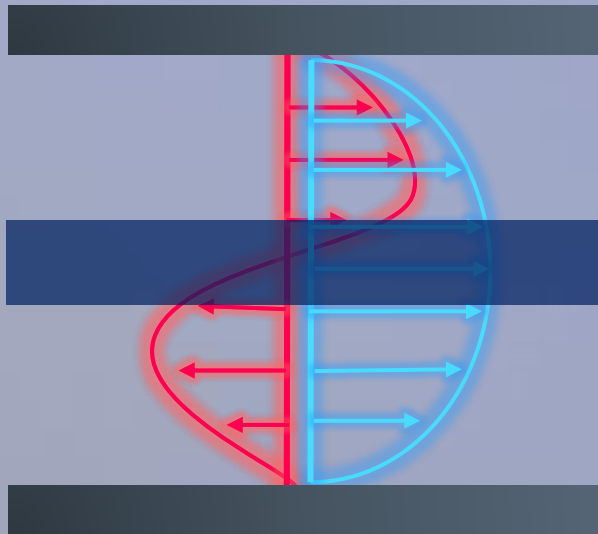


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ϵ	Ω_1
Ω_1	ω_{C_1}



Expectation: Exciton-Polariton Band Structure is obtained by a (N+1)x(N+1) Matrix.
N = number of cavity mode branches.



$$\hat{H}_{LM} = \sum_k \hat{c}_k^\dagger \hat{c}_k \epsilon_k + \hat{a}_k^\dagger \hat{a}_k \omega_k - g(\hat{a}_k^\dagger \hat{c}_k + \hat{c}_k^\dagger \hat{a}_k) = \sum H_k$$

	Ω_1	Ω_2	Ω_3
Ω_1	c_1	0	0
Ω_2	0	c_2	0
Ω_3	0	0	c_3

Problem with N+1 Hamiltonian

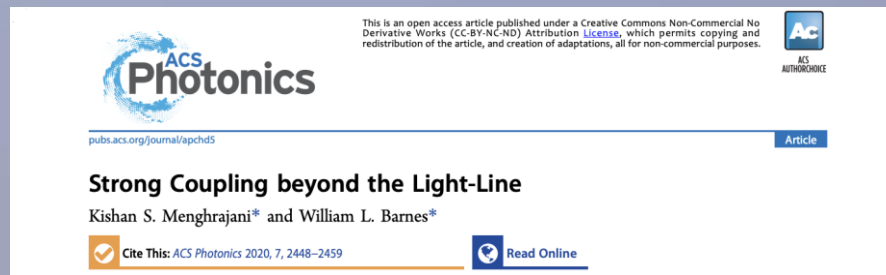
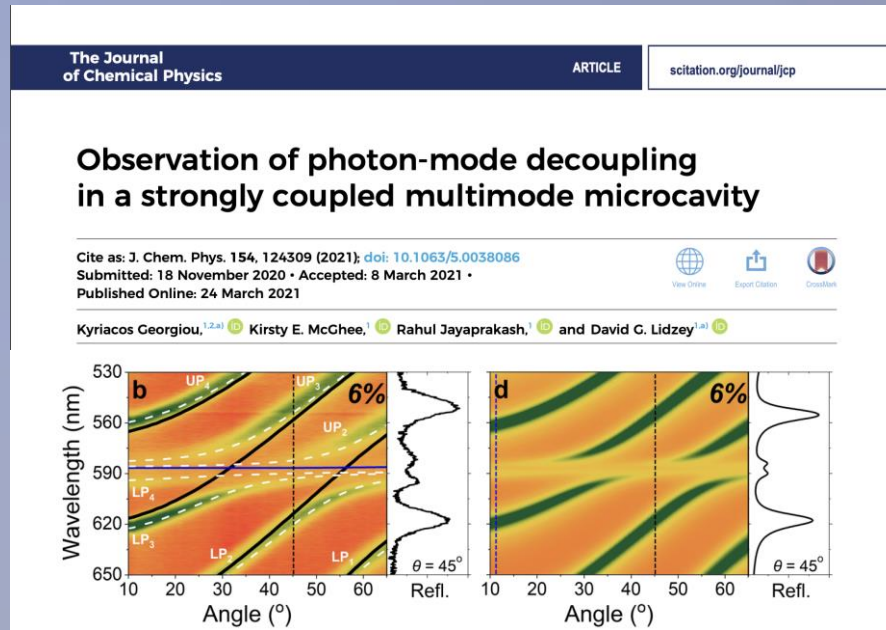
(N+1)x(N+1) model do not reproduce exciton polariton dispersion
2N x 2N model reproduce exciton polariton dispersion

**N+1 Hamiltonian
(cannot be used)**

	Ω_1	Ω_2	Ω_3
Ω_1	c_1	0	0
Ω_2	0	c_2	0
Ω_3	0	0	c_3

2N Hamiltonian

	Ω_1	0	0	0	0
Ω_1	c_1	0	0	0	0
0	0	Ω_2	0	0	0
0	0	Ω_2	c_2	0	0
0	0	0	0	Ω_3	0
0	0	0	0	Ω_3	c_3



GDCh

Forschungsartikel

Angewandte Chemie

Polaritons

Zitierweise: *Angew. Chem. Int. Ed.* 2021, 60, 16661–16667
Internationale Ausgabe: doi.org/10.1002/anie.202105442
Deutsche Ausgabe: doi.org/10.1002/ange.202105442

Ultralong-Range Polariton-Assisted Energy Transfer in Organic Microcavities

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Theory

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Maxwell consideration of polaritonic quasi-particle Hamiltonians in multi-level systems

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Letter

Coupling and decoupling of polaritonic states in multimode cavities

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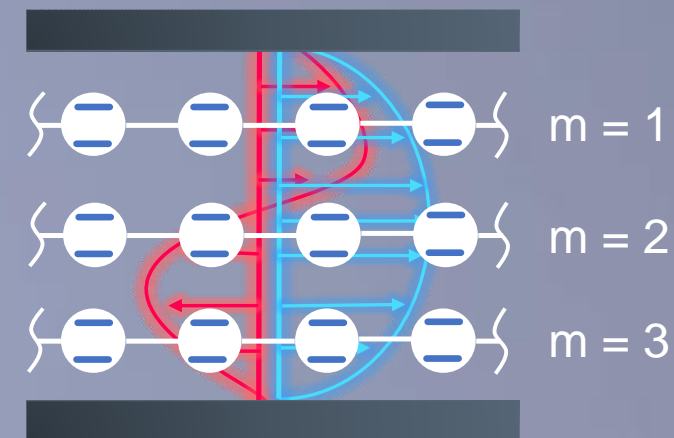
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We have a simple microscopic understanding of this phenomena

$$\hat{H}_{\text{LM}} = \sum_k \hat{c}_{k_x, m}^\dagger \hat{c}_{k_x, m} \epsilon_k + \hat{a}_{k_x k_y}^\dagger \hat{a}_{k_x k_y} \omega_k + g \left(\hat{a}_{k_x k_y}^\dagger \hat{c}_{k_x, m} + \hat{c}_{k_x, m}^\dagger \hat{a}_{k_x k_y} \right) \sin k_y Y_m$$

$$= \sum_k \hat{H}_{k_x}$$


$$\begin{bmatrix} \hat{c}_{k_x, 1}^\dagger & \dots & \hat{c}_{k_x, m}^\dagger \end{bmatrix} Q \times R \begin{bmatrix} \hat{a}_{k_x, 1} \\ \vdots \\ \hat{a}_{k_x, m} \end{bmatrix}$$



$$\hat{H}_{\text{LM}} = \sum_k \hat{c}_{k_x, m}^\dagger \hat{c}_{k_x, m} \epsilon_k + \hat{a}_{k_x k_y}^\dagger \hat{a}_{k_x k_y} \omega_k + g \left(\hat{a}_{k_x k_y}^\dagger \hat{c}_{k_x, m} + \hat{c}_{k_x, m}^\dagger \hat{a}_{k_x k_y} \right) \sin k_y Y_m$$

$$= \sum_k \hat{H}_{k_x}$$

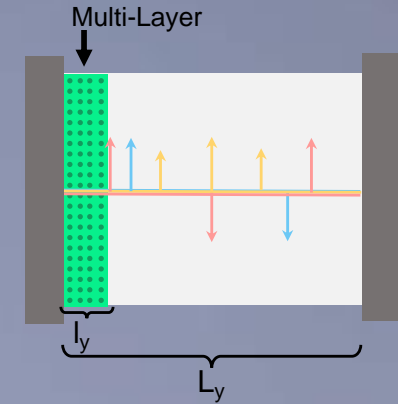
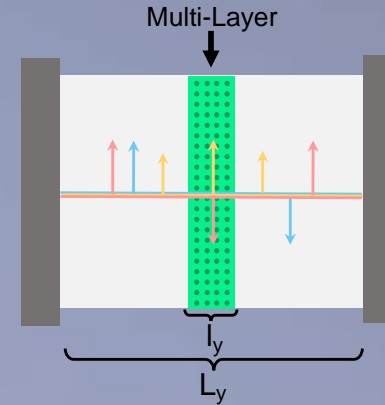
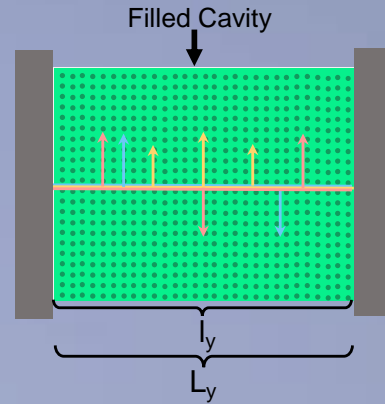
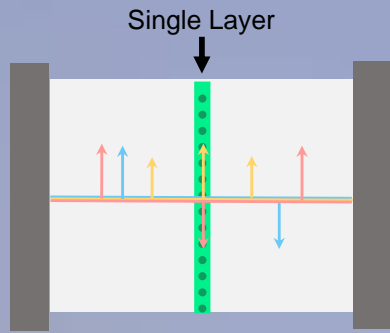
$$\begin{bmatrix} \hat{c}_{k_x, 1}^\dagger & \dots & \hat{c}_{k_x, m}^\dagger \end{bmatrix} Q \times R \begin{bmatrix} \hat{a}_{k_x, 1} \\ \vdots \\ \hat{a}_{k_x, m} \end{bmatrix}$$



$$\begin{bmatrix} \hat{c}_{k_x, \kappa_1}^\dagger & \dots & \hat{c}_{k_x, \kappa_{N_e}}^\dagger \end{bmatrix}$$

For filled cavities $\hat{c}_{k_x, k_y}^\dagger$ operator only couple to $\hat{a}_{k_x k_y}$

Simple Matrix Models



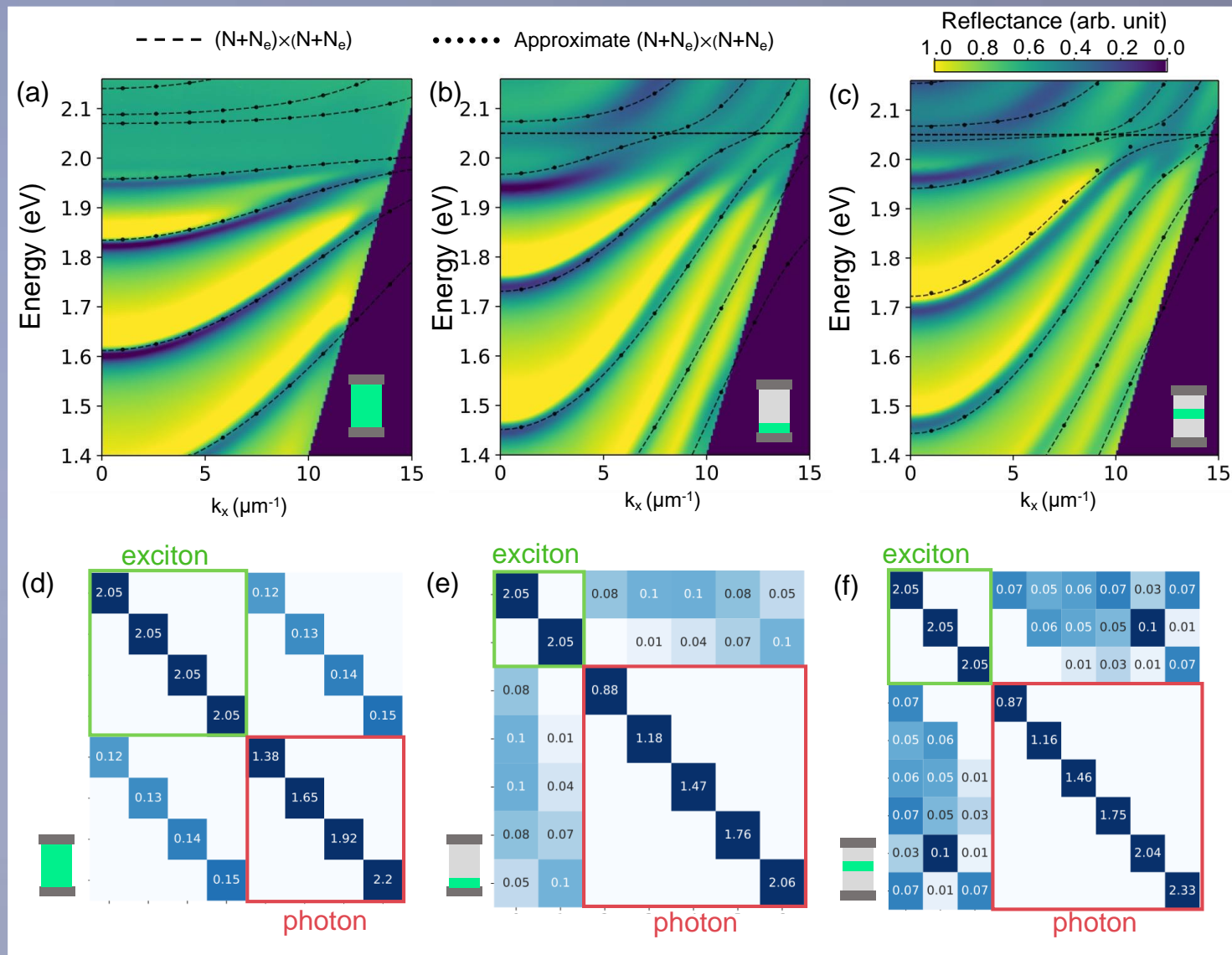
ϵ	Ω_1	Ω_2	Ω_3	Ω_4	Ω_5
Ω_1	ω_{C1}	0	0	0	0
Ω_2	0	ω_{C2}	0	0	0
Ω_3	0	0	ω_{C3}	0	0
Ω_4	0	0	0	ω_{C4}	0
Ω_5	0	0	0	0	ω_{C5}

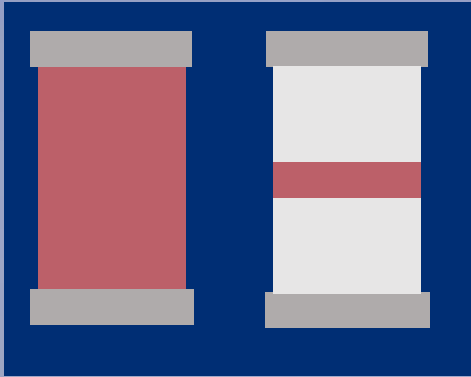
ϵ	Ω_1	0	0	0	0
Ω_1	ω_{C1}	0	0	0	0
0	0	ϵ	Ω_2	0	0
0	0	Ω_2	ω_{C2}	0	0
0	0	0	0	ϵ	Ω_3
0	0	0	0	Ω_3	ω_{C3}

ϵ	Ω_1	Ω_3	0	0	0
Ω_1	ω_{C1}	0	0	0	0
Ω_3	0	ω_{C3}	0	0	0
0	0	0	ϵ	Ω_2	Ω_4
0	0	0	Ω_2	ω_{C2}	0
0	0	0	Ω_4	0	ω_{C4}

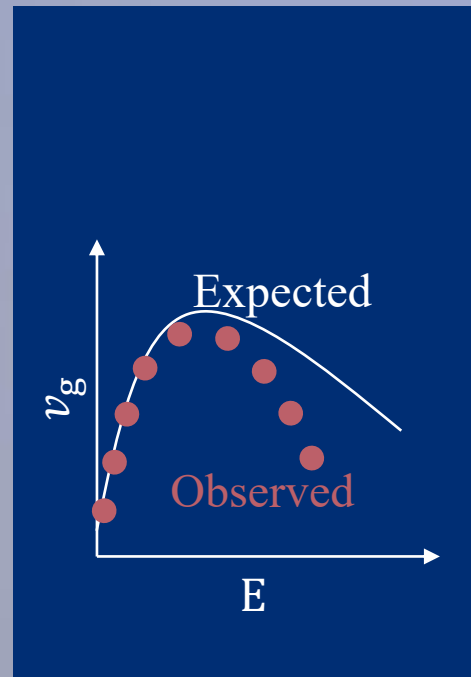
ϵ	Ω_1	Ω_2	Ω_3	Ω_4	Ω_5
Ω_1	ω_{C1}	0	0	0	0
Ω_2	0	ω_{C2}	0	0	0
Ω_3	0	0	ω_{C3}	0	0
Ω_4	0	0	0	ω_{C4}	0
Ω_5	0	0	0	0	ω_{C5}

The theoretical models predicts the experiment



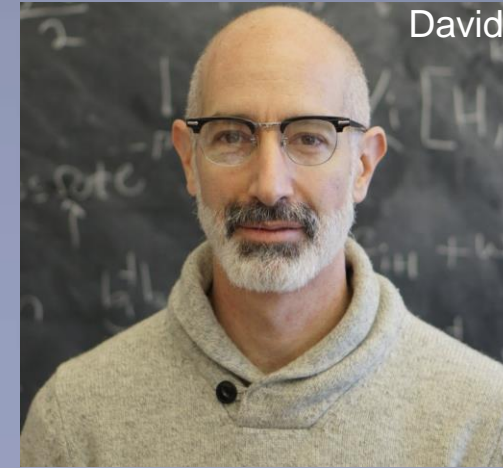
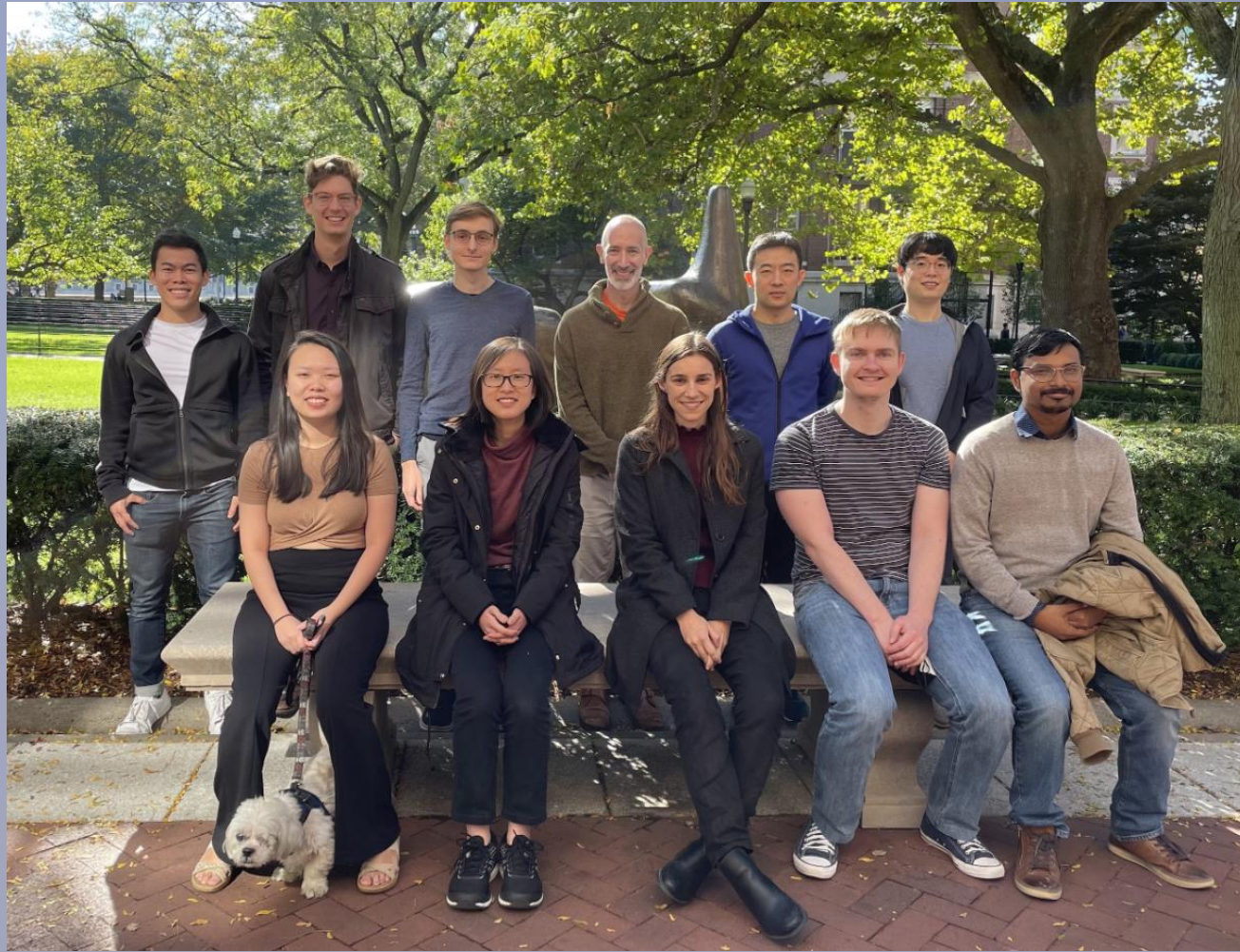


- For extended materials: $2N$ Hamiltonian (N = number of cavity mode branch) should be used.
- For arbitrary setup : $N+N_e$ Hamiltonian (N = number of cavity mode branch, $N_e < N$) should be used.



- We simulated exciton-polariton transport with Semi-classical approach.
- We find ballistic (Coherent) motion when exciton character is low. ($< 40\%$)
- We find phonons can **rescale** group velocity through a transient localization mechanism.
- Coherence is long-lived (\sim ps) for low exciton character.

Acknowledgements



David



Milan



Ding

