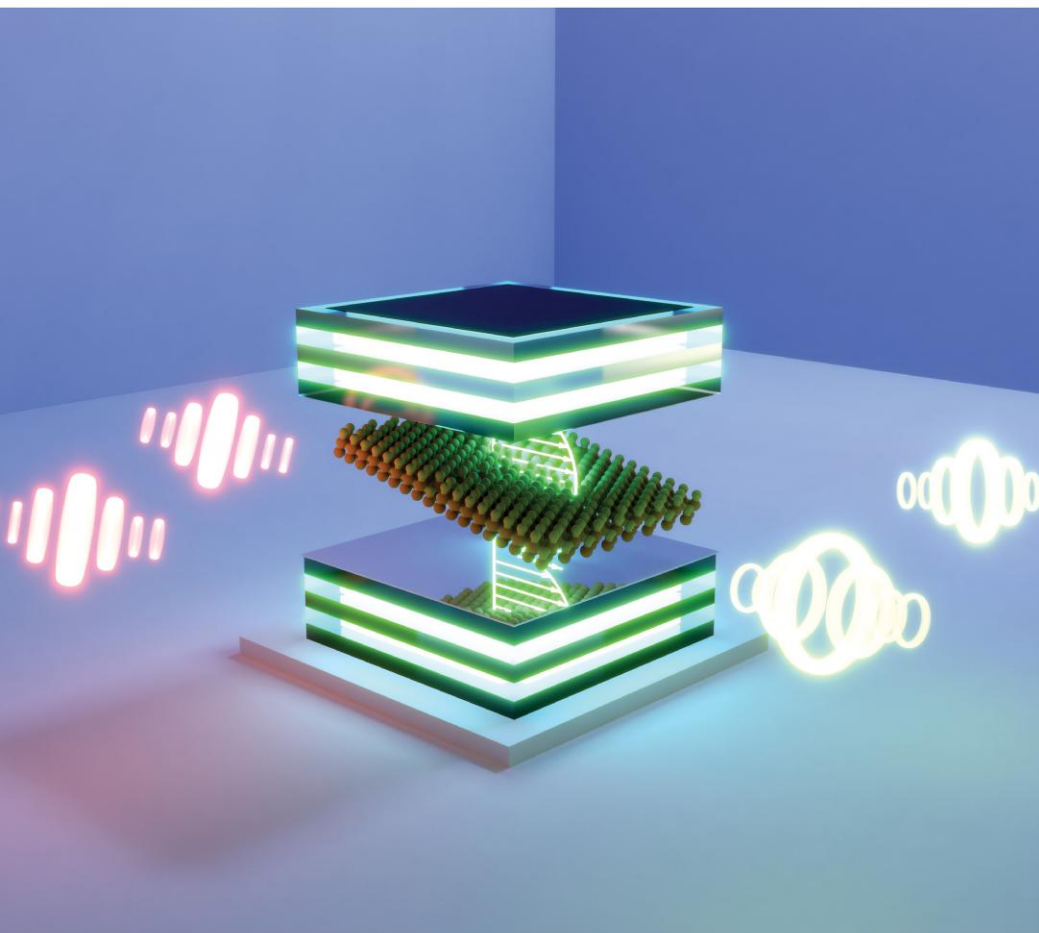




Tuning Quantum Dynamics of Materials Between two Mirrors

Arshath Manjalingal, Mandal Group, Texas A&M

Manjalingal[†], Rahmanian[†], Blackham, Mandal, *ACS Photonics* (2025)

Blackham[†], Manjalingal[†], Rahmanian, Mandal, *Nano Letters* (2025)

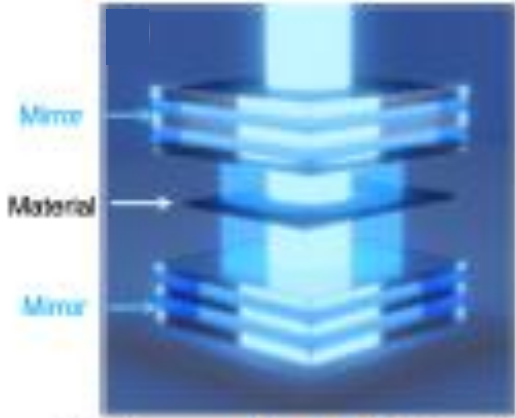
Ghosh, Manjalingal, Wickramasinghe, Rahmanian, Mandal, *Physical Review B* (2025)

Haines[†], Manjalingal[†], Blackham, Rahmanian, Mandal, *arXiv* (2026)

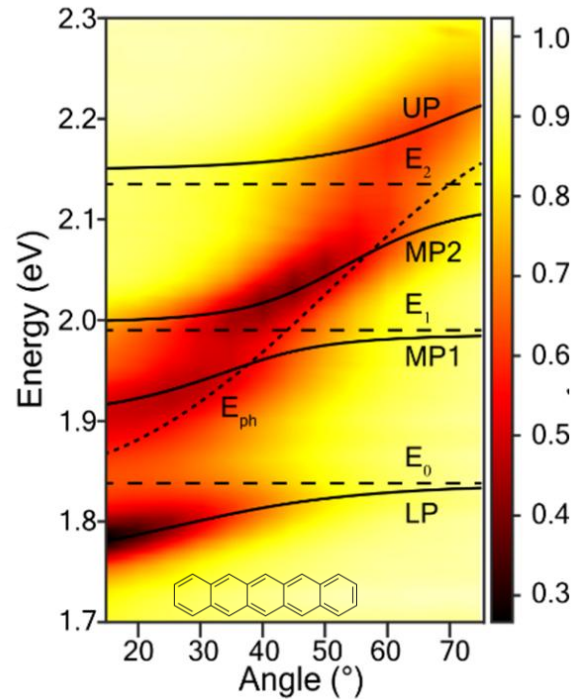
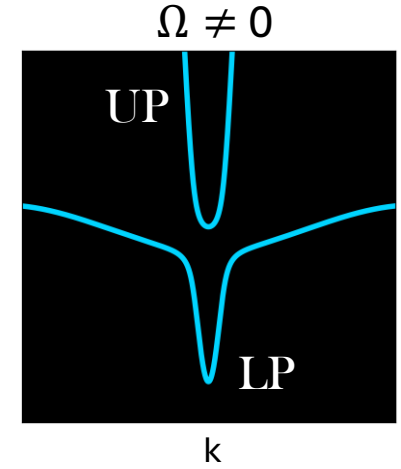
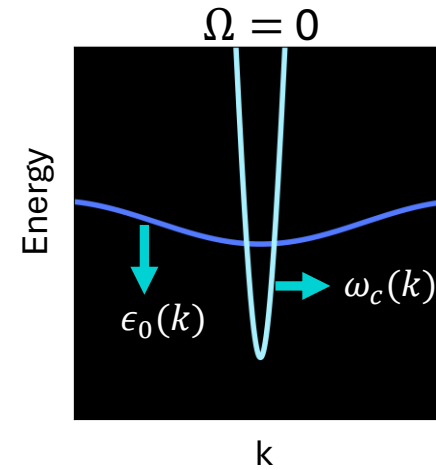
Rahmanian, Manjalingal, Blackham, Mandal, *arXiv* (2025)

[†]equal contribution

Polaron-Polariton Dispersion



$$\hat{H}_k = \begin{bmatrix} \epsilon_0(k) & \Omega \\ \Omega & \omega_c(k) \end{bmatrix}$$

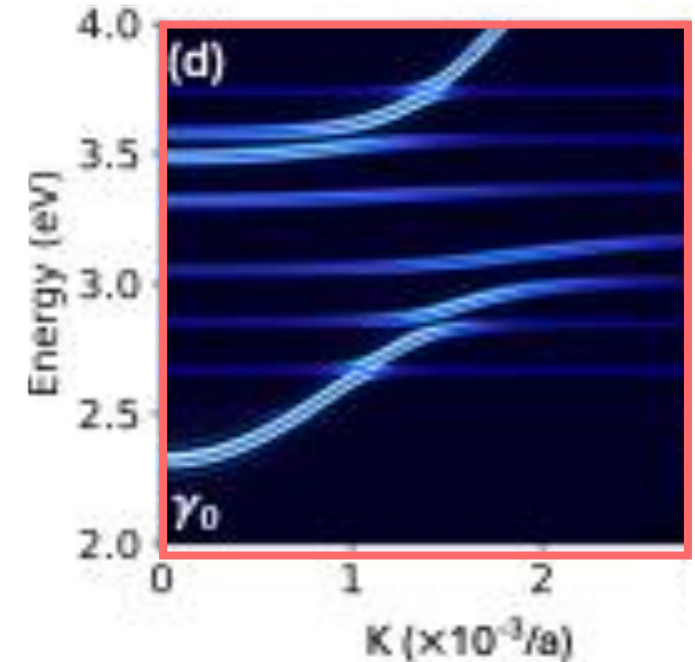


Alam,... , Frontiera, arXiv. (2025)

Our Analytical Theory

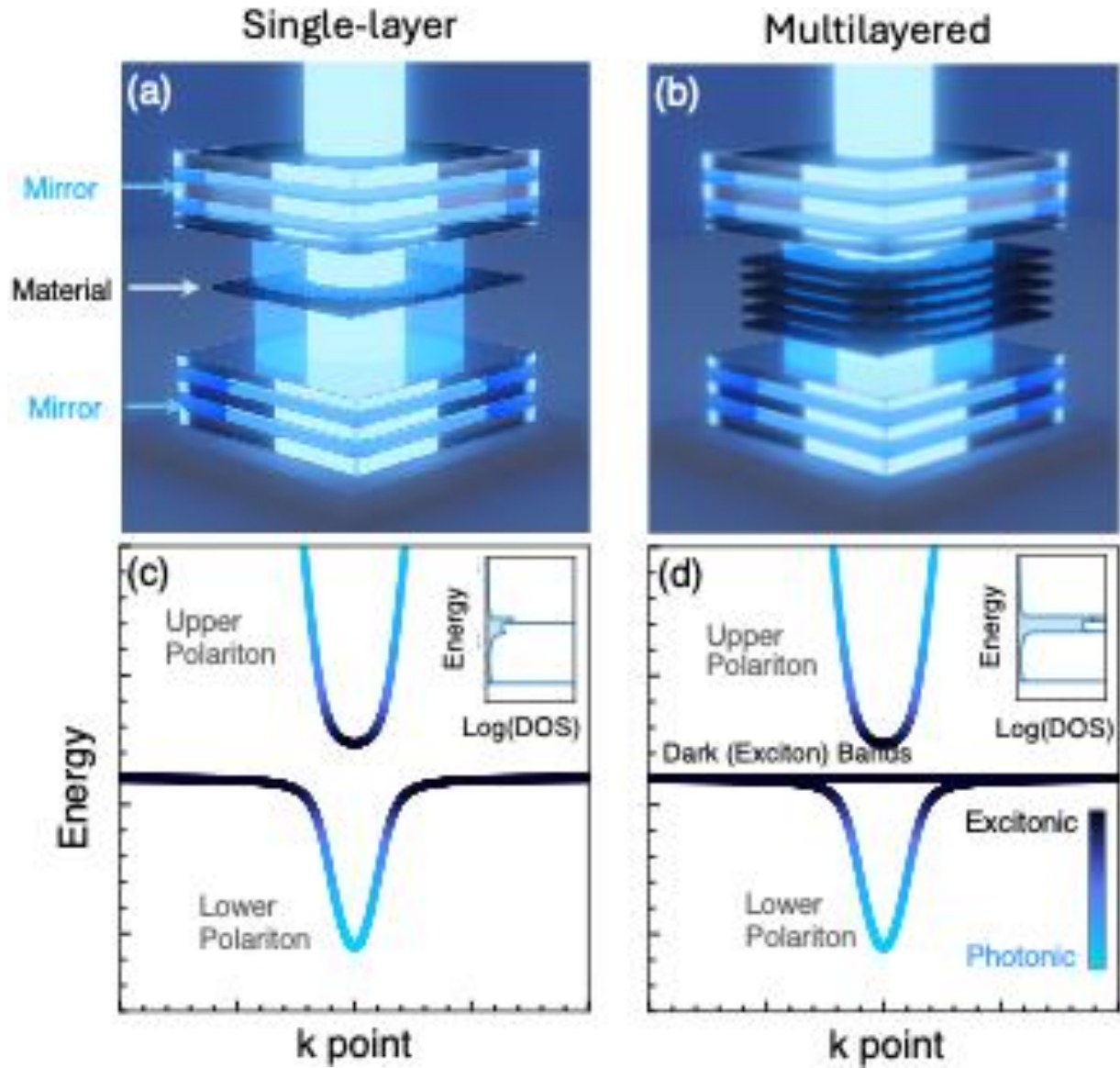
$$\hat{H}_k = \begin{bmatrix} \ddots & \vdots & \vdots & \vdots & \vdots \\ \dots & \tilde{\epsilon} - \omega_0 & 0 & 0 & \dots \\ \dots & 0 & \tilde{\epsilon} & 0 & \dots \\ \dots & 0 & 0 & \tilde{\epsilon} + \omega_0 & \dots \\ \dots & \sqrt{\frac{S^{[0]}}{N}} \Omega_k & \sqrt{\frac{S^{[0]}}{N}} \Omega_k & \sqrt{\frac{S^{[0]}}{N}} \Omega_k & \ddots \\ \dots & \sqrt{\frac{S^{[0]}}{N}} \Omega_k & \sqrt{\frac{S^{[0]}}{N}} \Omega_k & \sqrt{\frac{S^{[0]}}{N}} \Omega_k & \dots \end{bmatrix}$$

$$S_{m_j}^{[l]} = \lim_{M \rightarrow \infty} 2 \tanh\left(\frac{\beta \omega_j}{2}\right) \int_{-\infty}^{\infty} dz \frac{M!}{(M + m_j)!} \left(\frac{\gamma_j^2 z^2}{\omega_j^2 M}\right)^{m_j} \times \exp\left[-\left(4\omega_j \tanh\left(\frac{\beta \omega_j}{2}\right) + \frac{\pi^2 \gamma_j^4}{4\omega_j^4 M^2}\right) z^2\right] \left[L_M^{(m_j)}\left(\frac{\gamma_j^2 z^2}{\omega_j^2 M}\right)\right]^2 \quad (14)$$

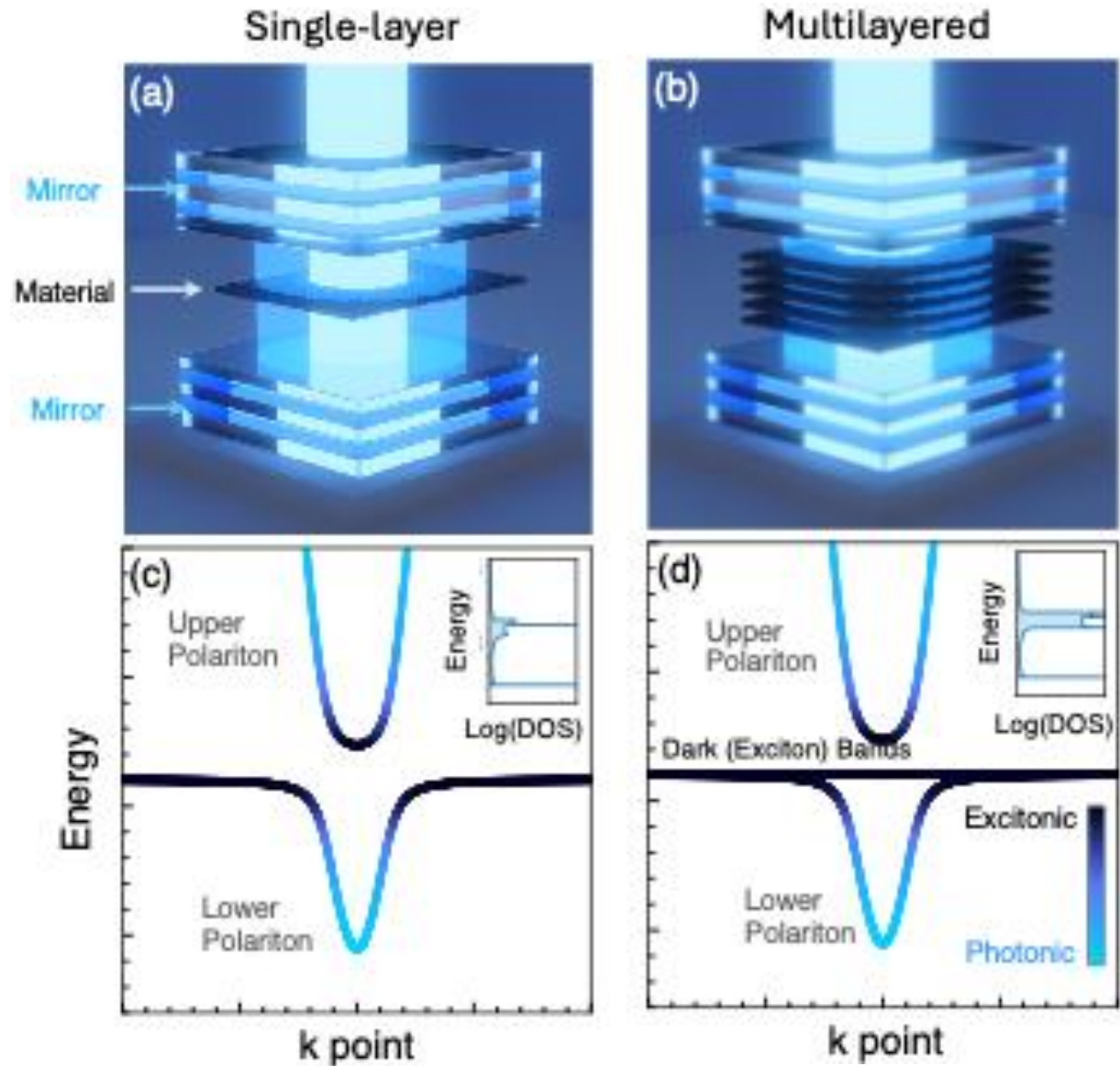


Blackham [†], Manjalingal [†], Rahmanian, Mandal, *Nano Letters* (2025)

Single vs Multilayer Materials in Cavities

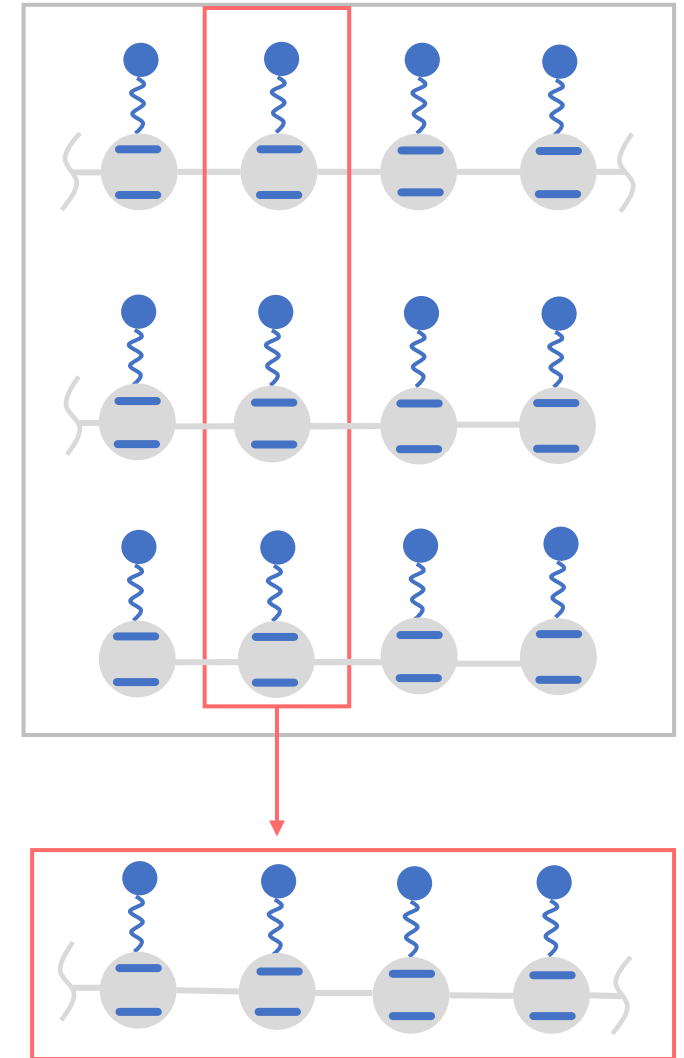


Single vs Multilayer Materials in Cavities

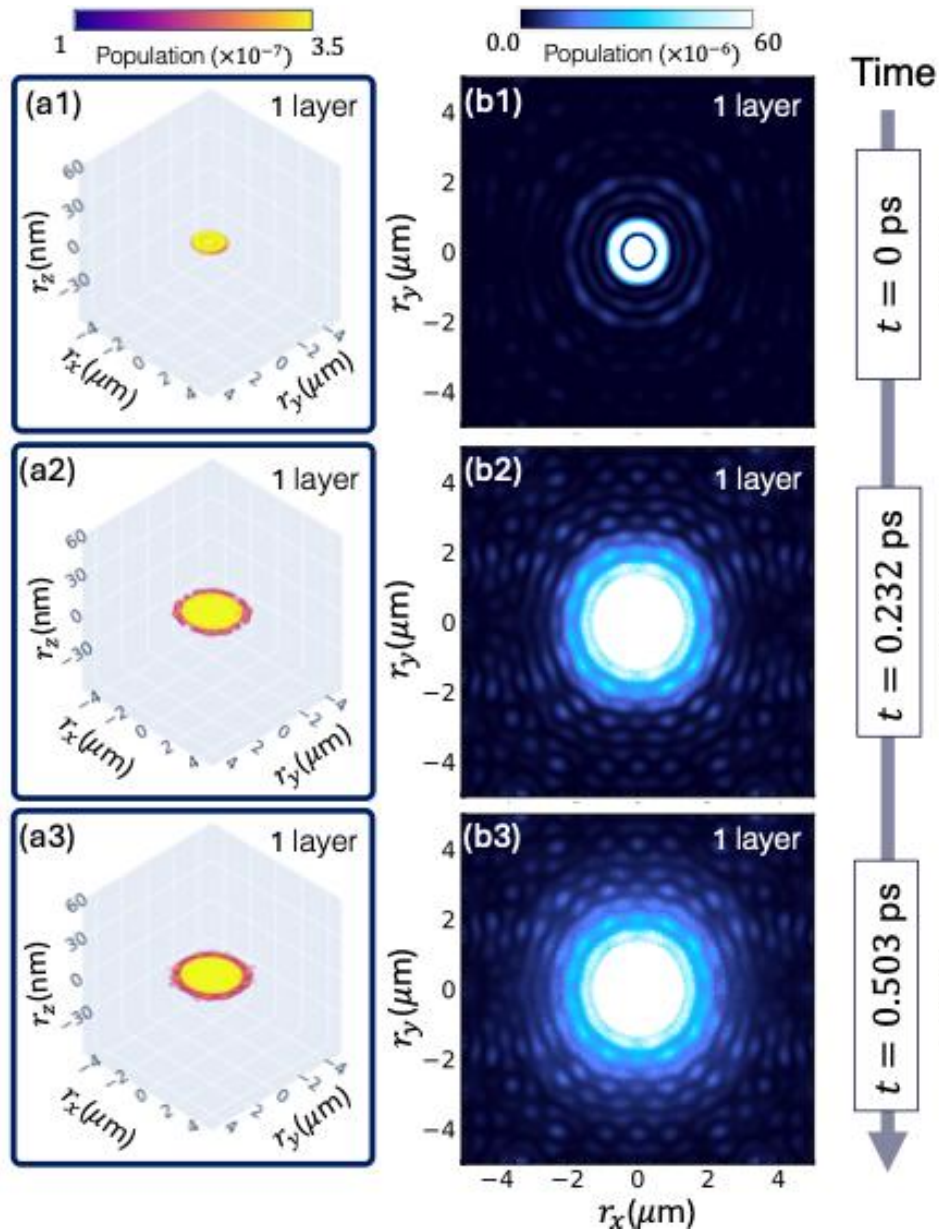


Phonon Fluctuation Synchronization Effect

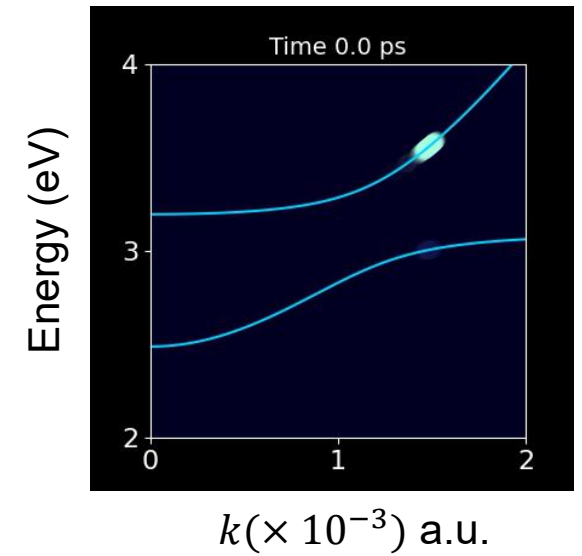
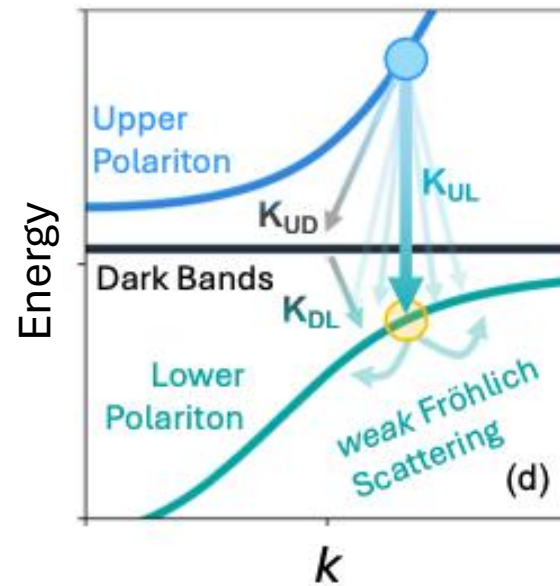
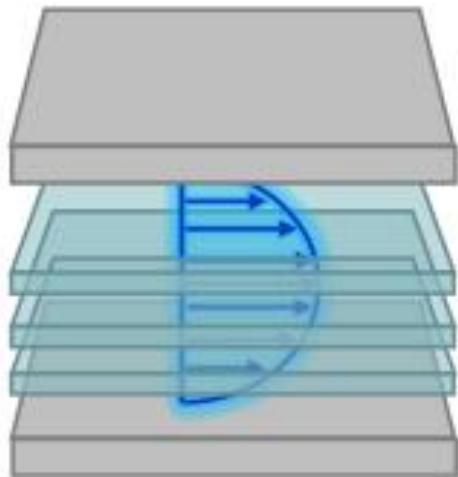
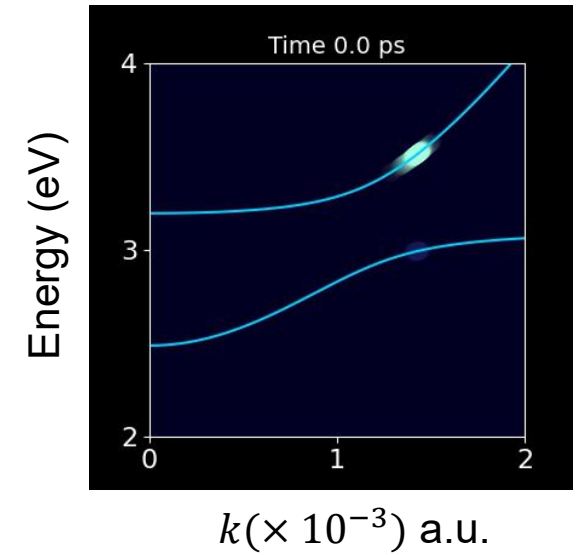
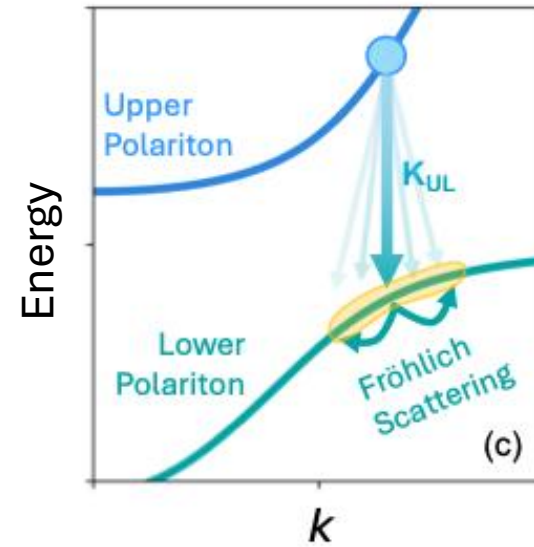
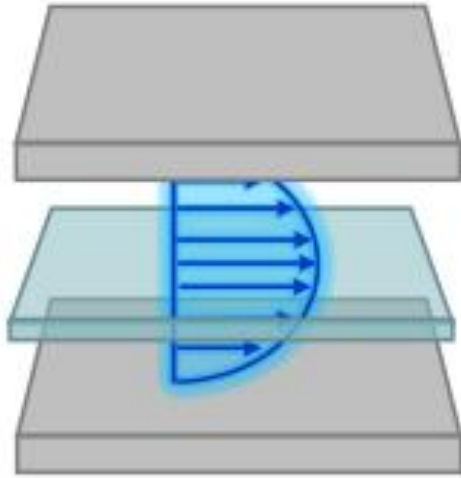
Bright layer



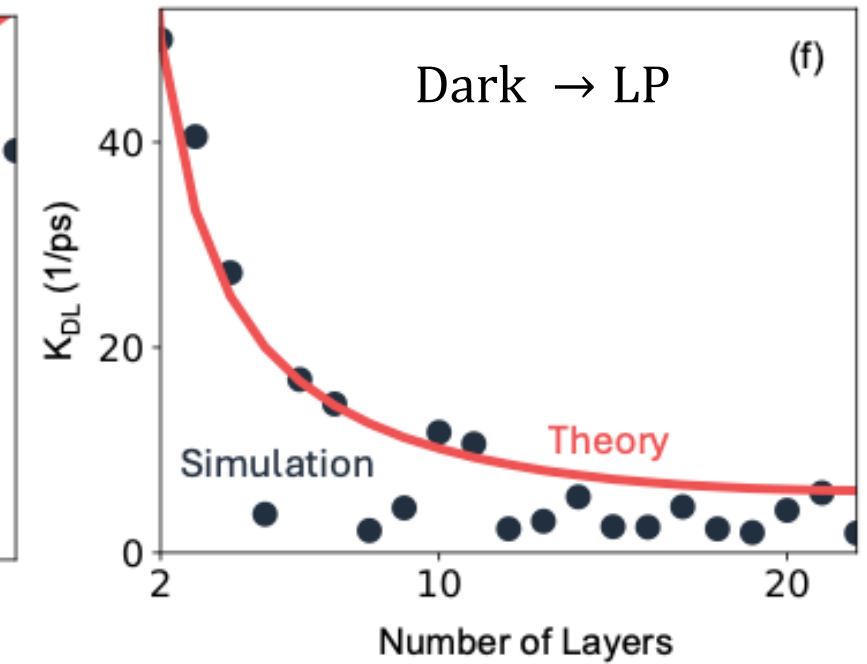
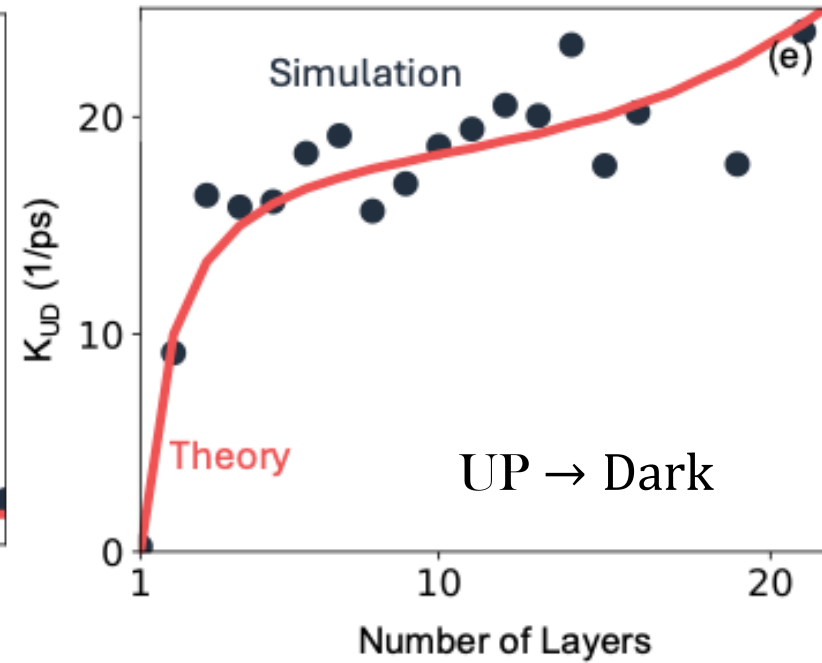
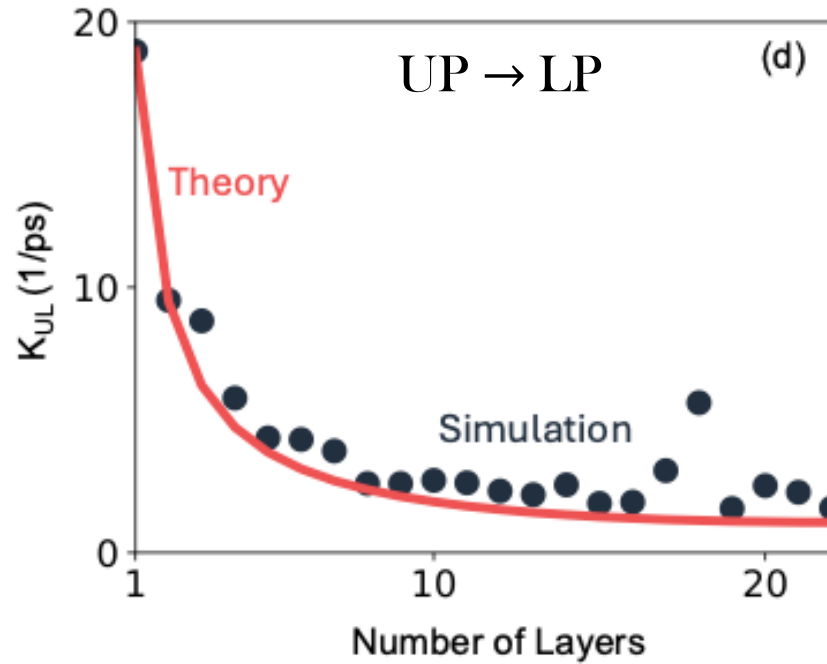
Single Layer Vs Multi-Layer with 3D Cavity-Material Architecture



Mechanistic Principles of Exciton-Polariton Relaxation



Mechanistic Principles of Exciton-Polariton Relaxation



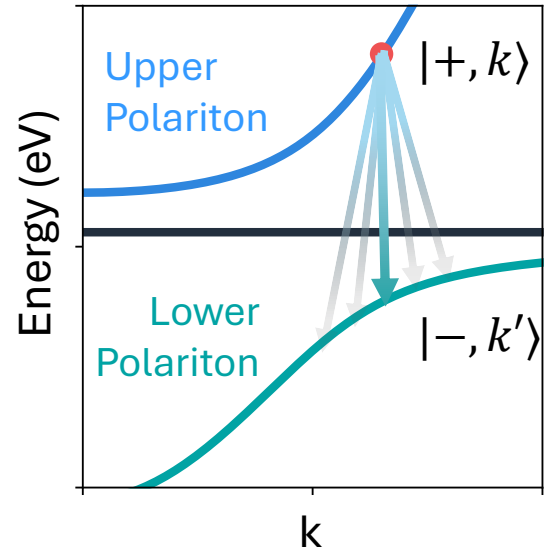
$$K_{UL}(N_L) \propto f(N_L)$$

$$K_{UD}(N_L) \propto (N_L - 1)f(N_L)$$

$$K_{DL}(N_L) \propto f(N_L)$$

$$f(N_L) = \frac{1}{S^2} \sum_m^{N_L} \sin^4(k_0 \cdot y_m)$$

Direct Transition from Upper to Lower Polariton



$$\langle -, k' | e^{-i\Delta t \hat{H}_{bX}} | +, k \rangle$$

$$\mathbb{P}_- \hat{H}_{bX} \mathbb{P}_+ = \gamma \sum_{k,k'} \hat{P}_{k,-}^\dagger \hat{P}_{k',+} \left[\cos(\theta_k) \sin(\theta_{k'}) \mathcal{Q}(t) \right].$$

Exciton-Phonon coupling

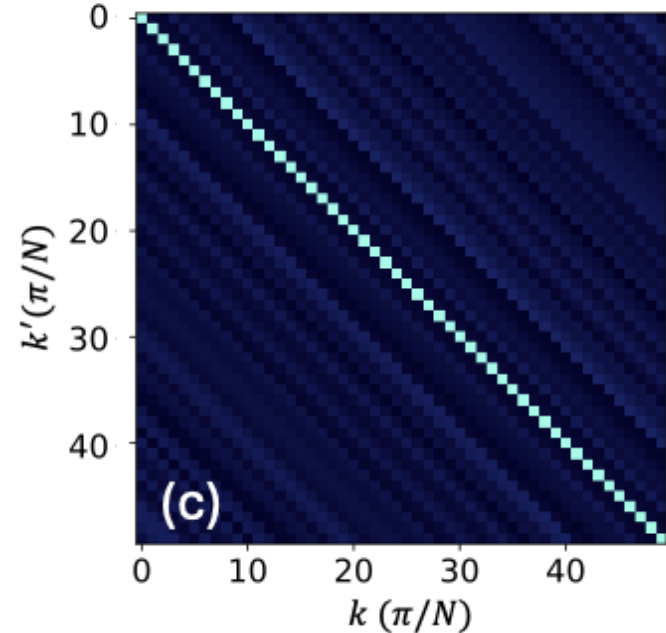
$$\langle -, k' | e^{-i\hat{H}_{bX}\Delta t} | +, k \rangle$$

$$= C_{kk'} \sum_n \frac{e^{i(k'-k) \cdot x_n}}{N} (1 - e^{-i\gamma q_{n,m} \Delta t})$$

$$\approx C_{kk'} \langle 1 - e^{-i\gamma q \Delta t} \rangle \sum_n \frac{e^{i(k'-k) \cdot x_n}}{N}$$

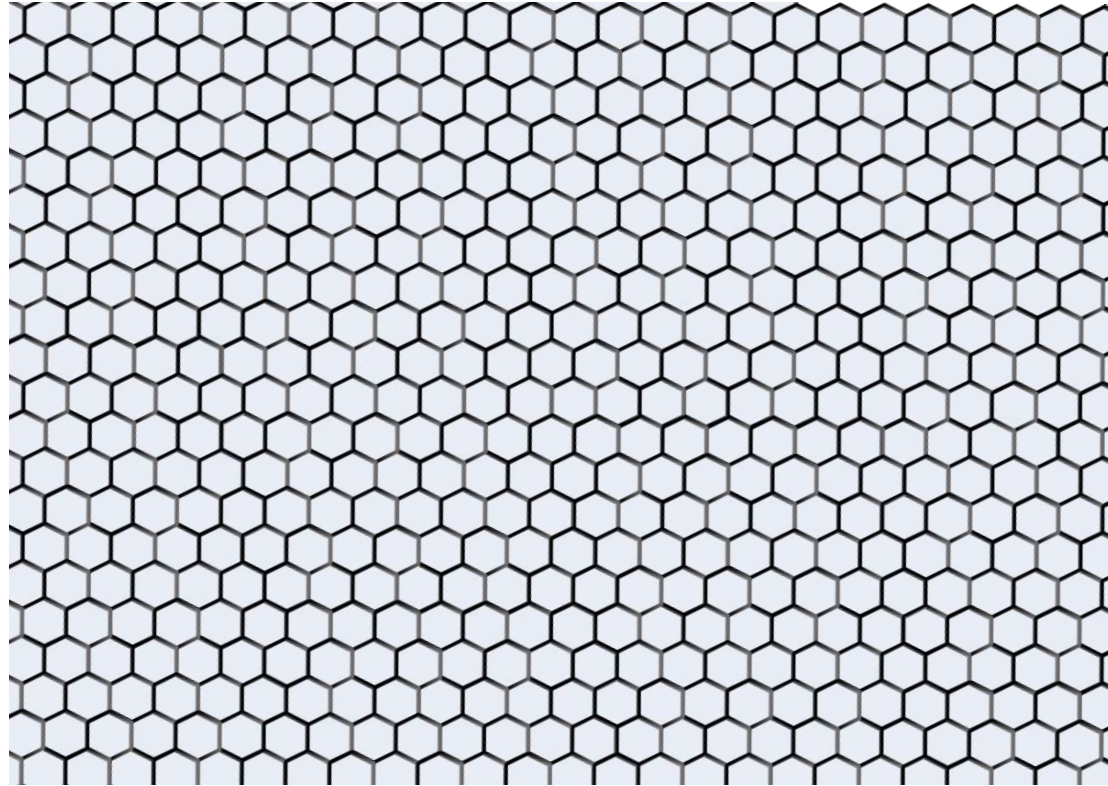
Using separation of length-scales

$$= C_{kk'} \langle 1 - e^{-i\gamma q \Delta t} \rangle \cdot \delta_{kk'}$$

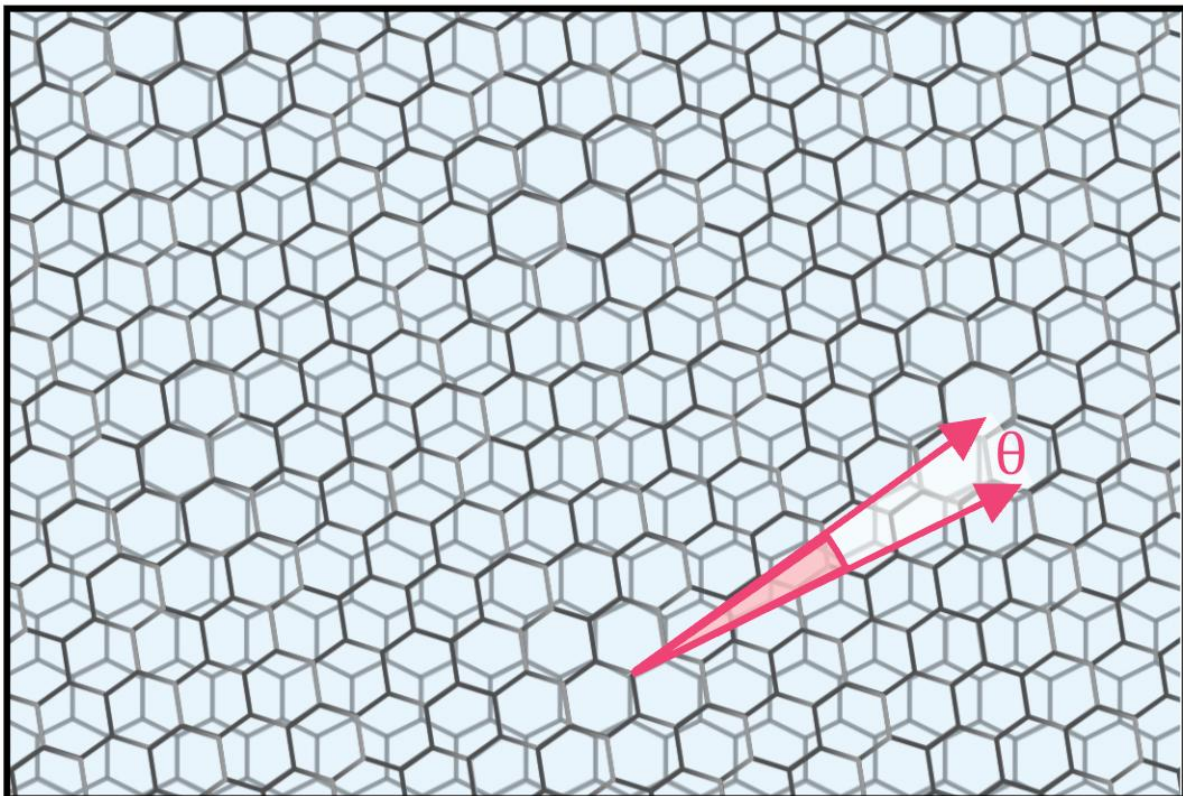


Moiré Pattern

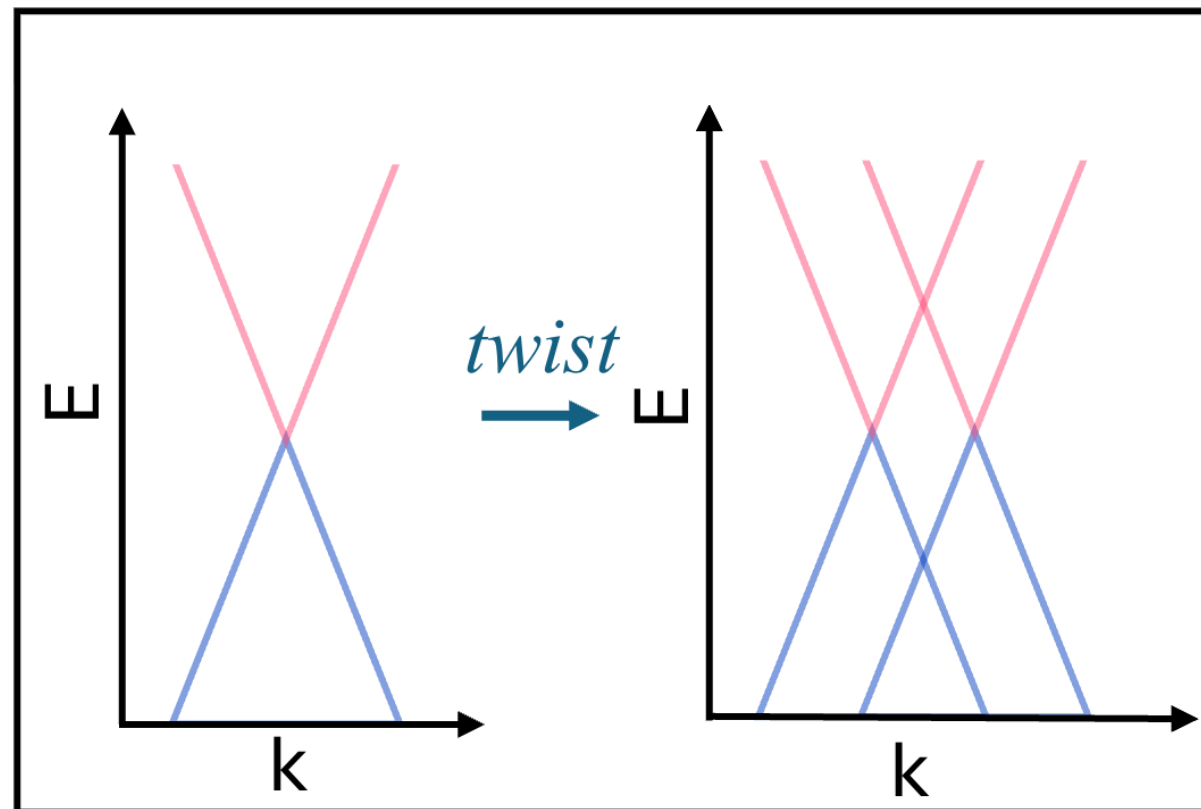
Graphene Bilayer



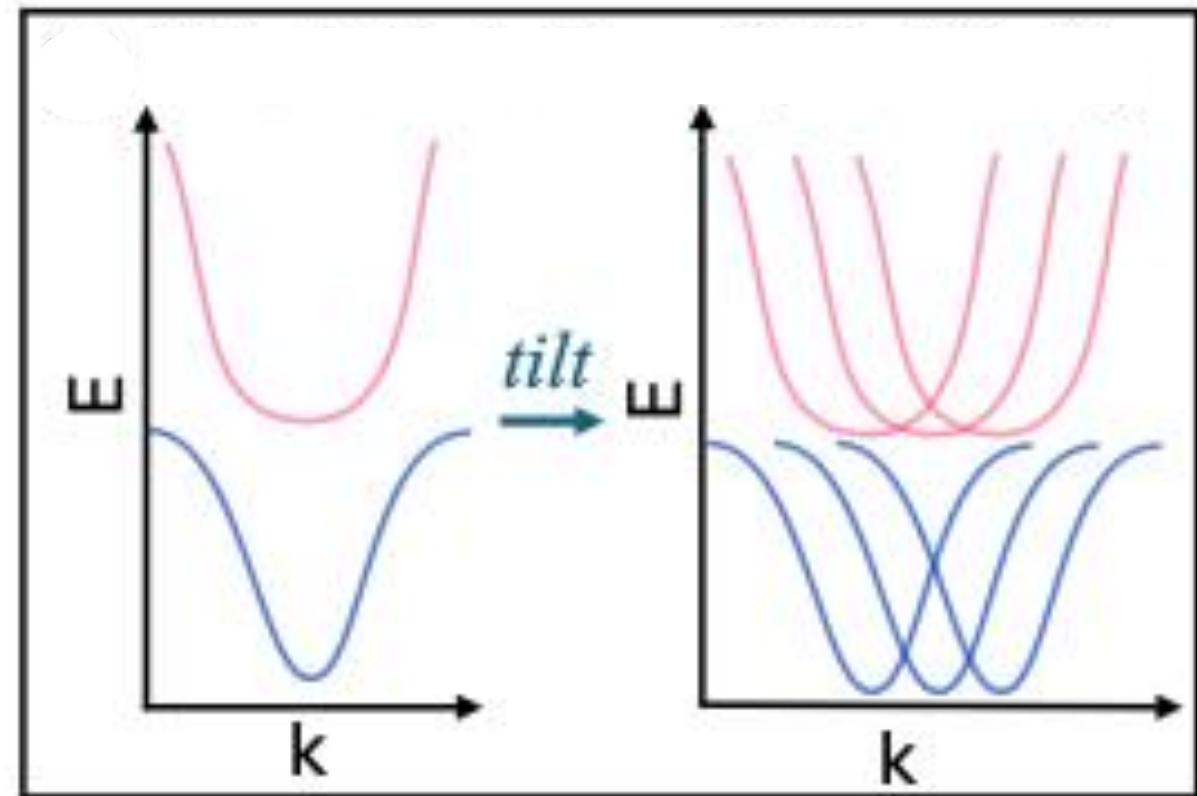
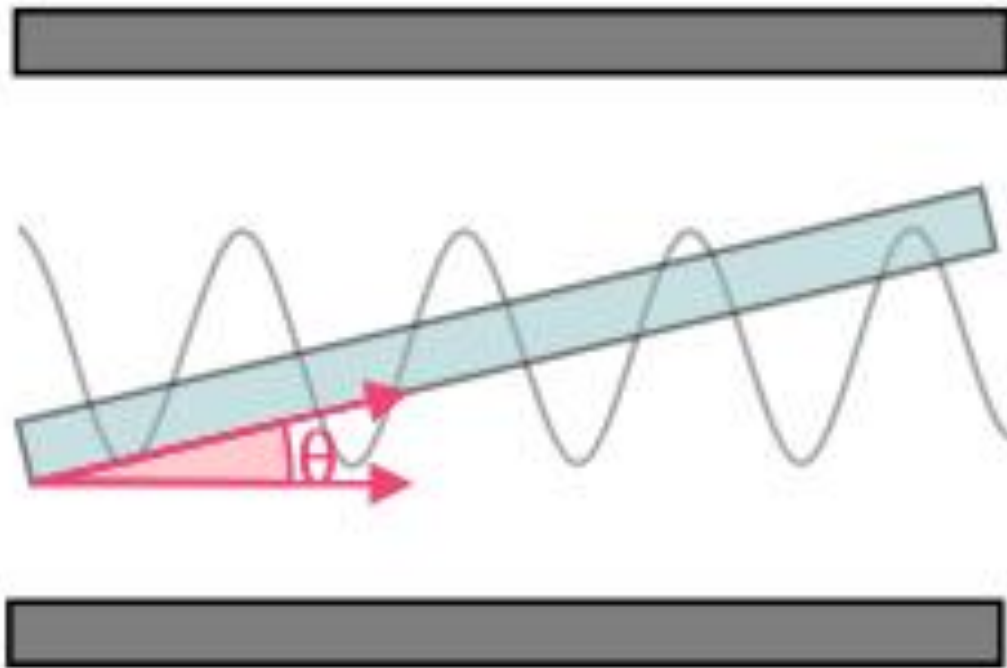
Twisted Bilayer



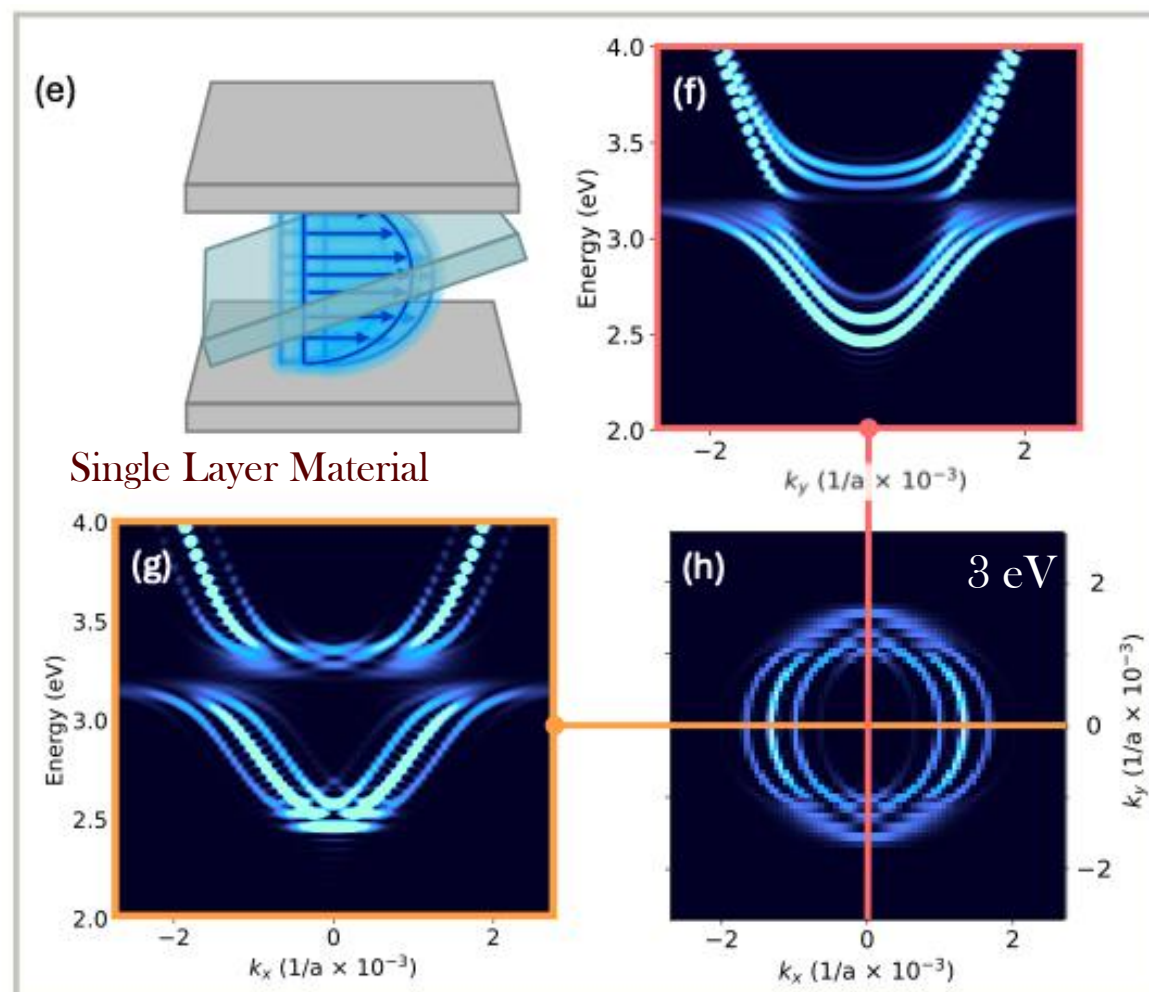
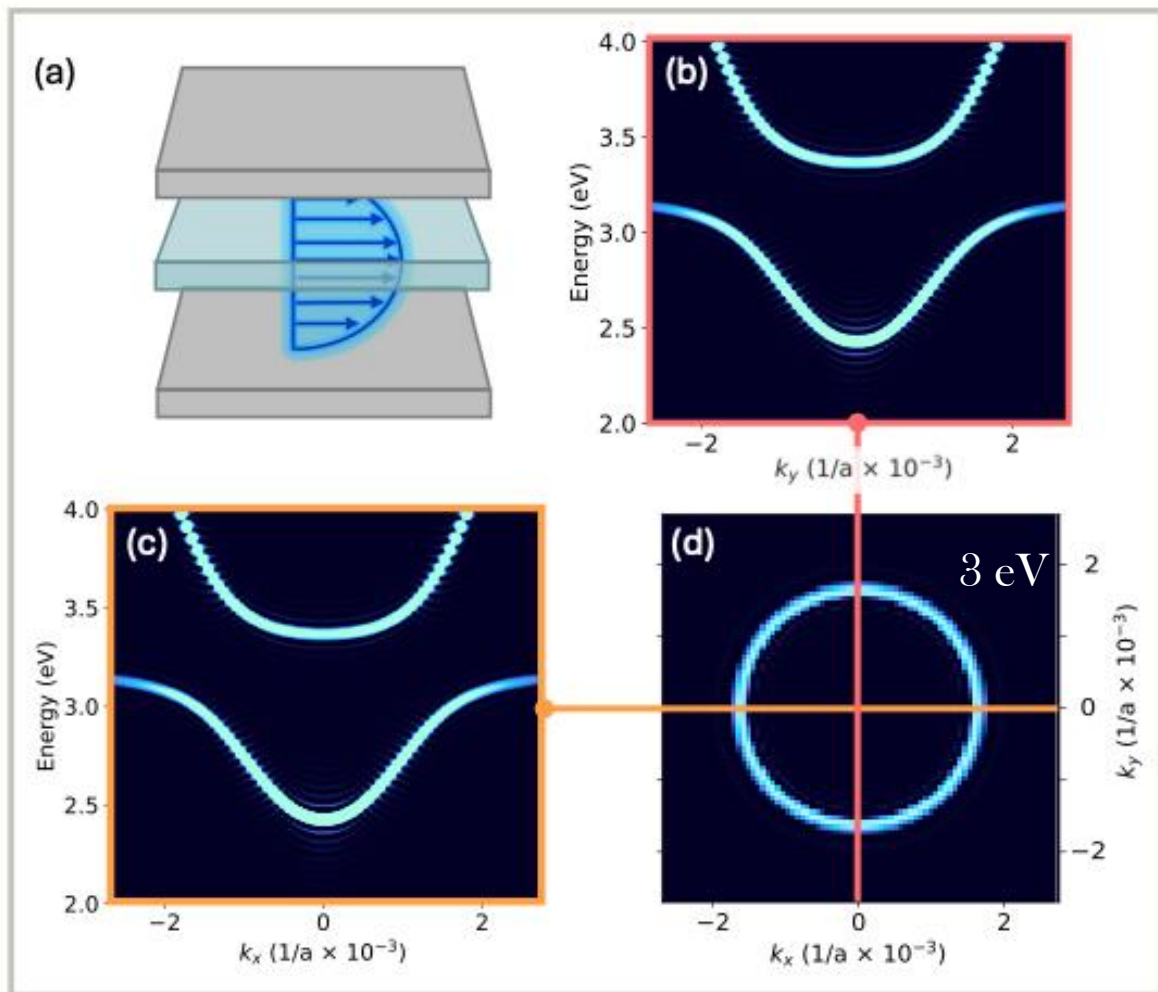
Band structure modification



Tilted Material in an Optical Cavity

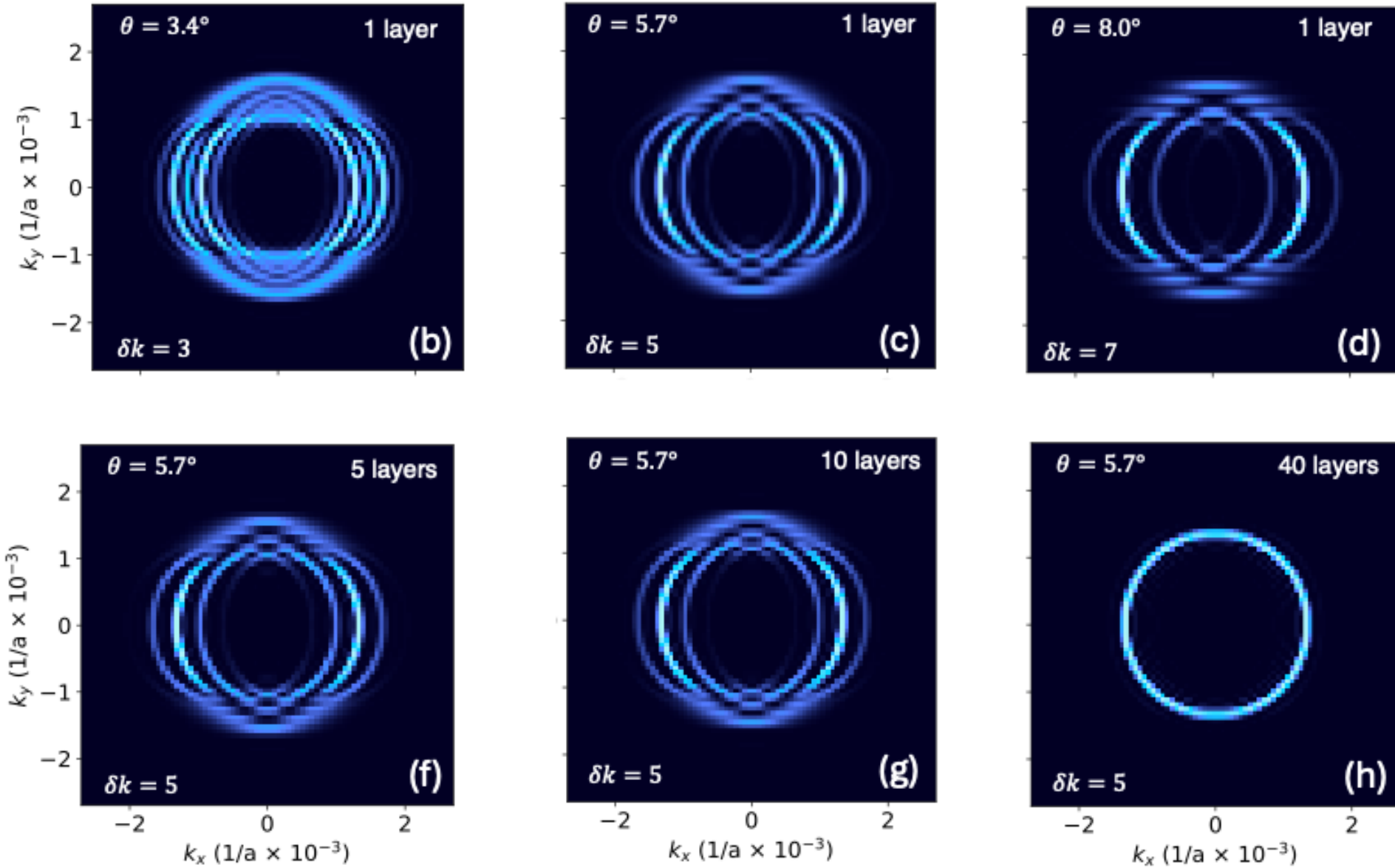


Light-Matter Moiré Effect

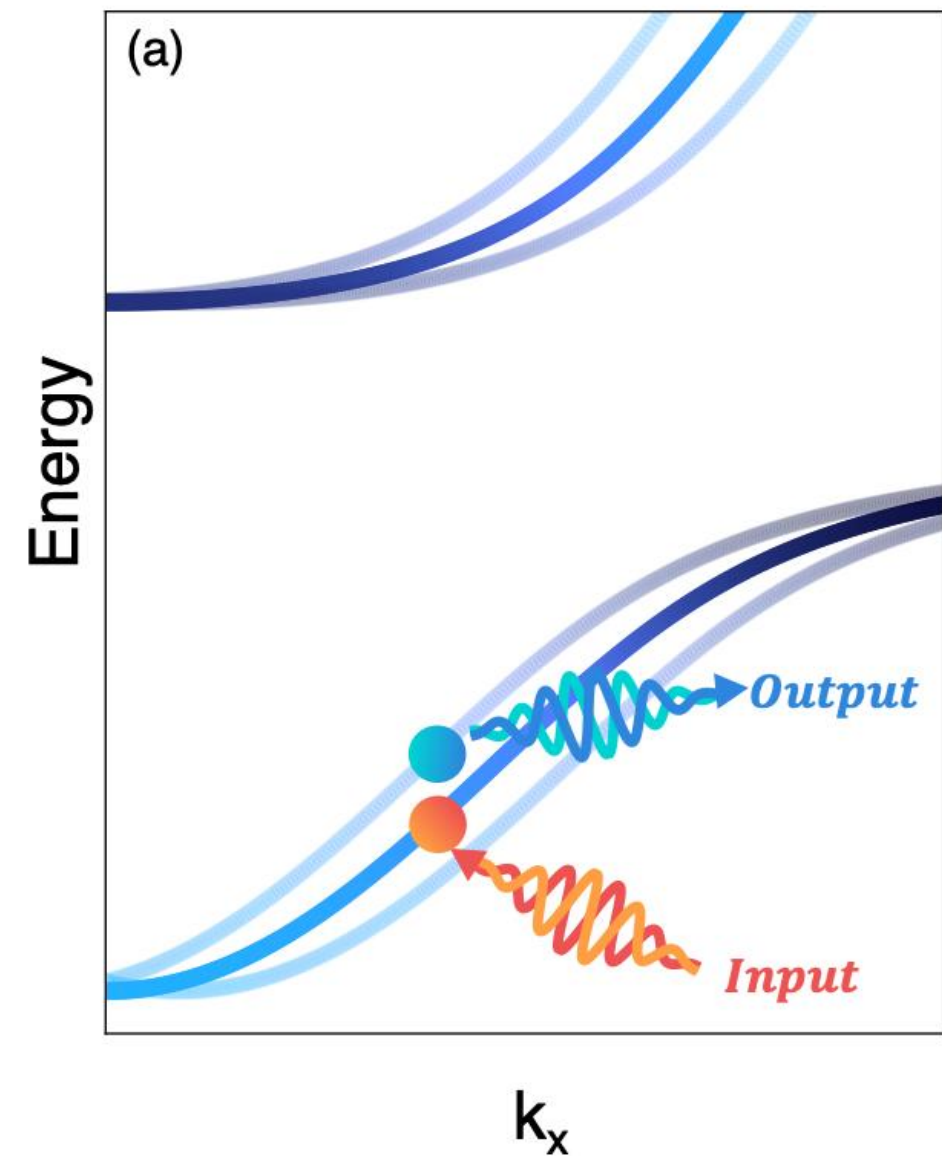


Manjalingal[†], Rahmanian[†], Blackham, Mandal, *ACS Photonics* (2025)

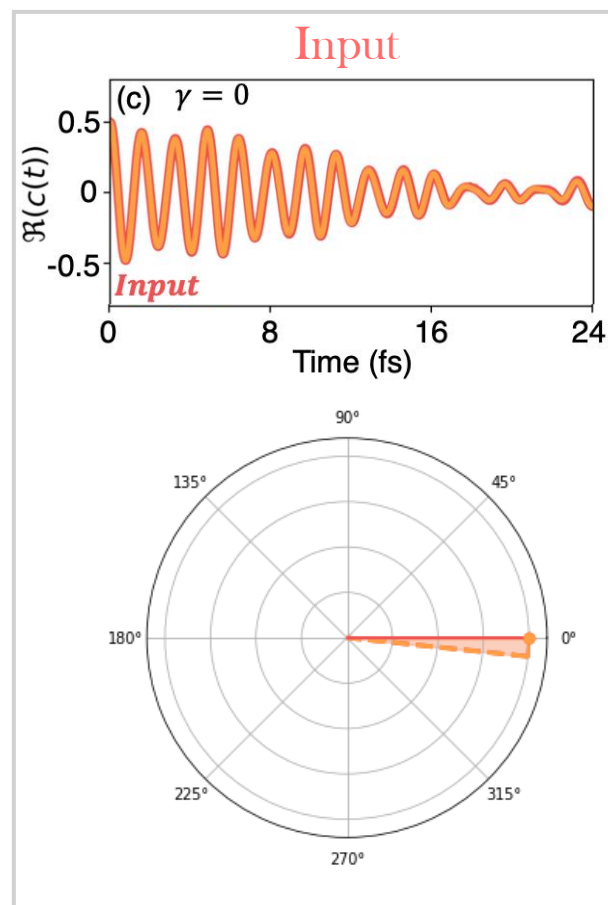
$$\Delta K = \sin(\theta) \frac{m_z}{2L_z}$$



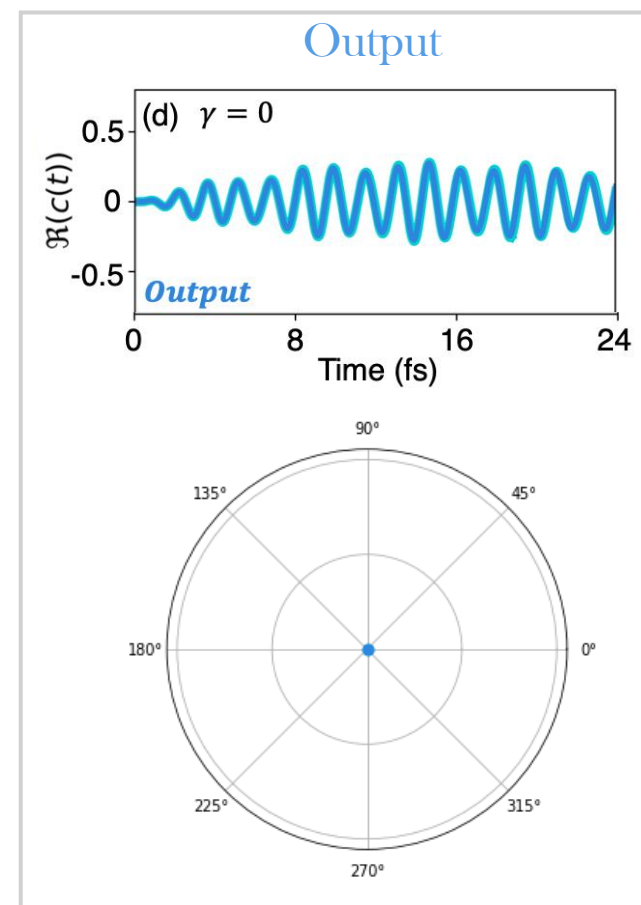
Coherent Frequency Conversion



$$\frac{1}{\sqrt{2}} \left(A_{k_1}^\dagger + A_{k_2}^\dagger \right) |0\rangle$$

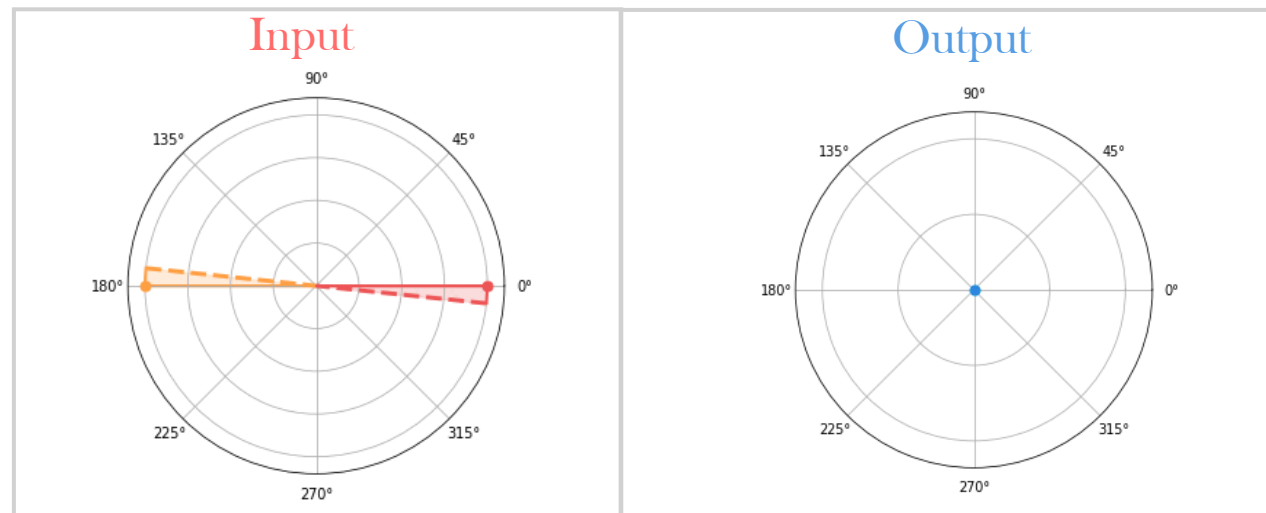
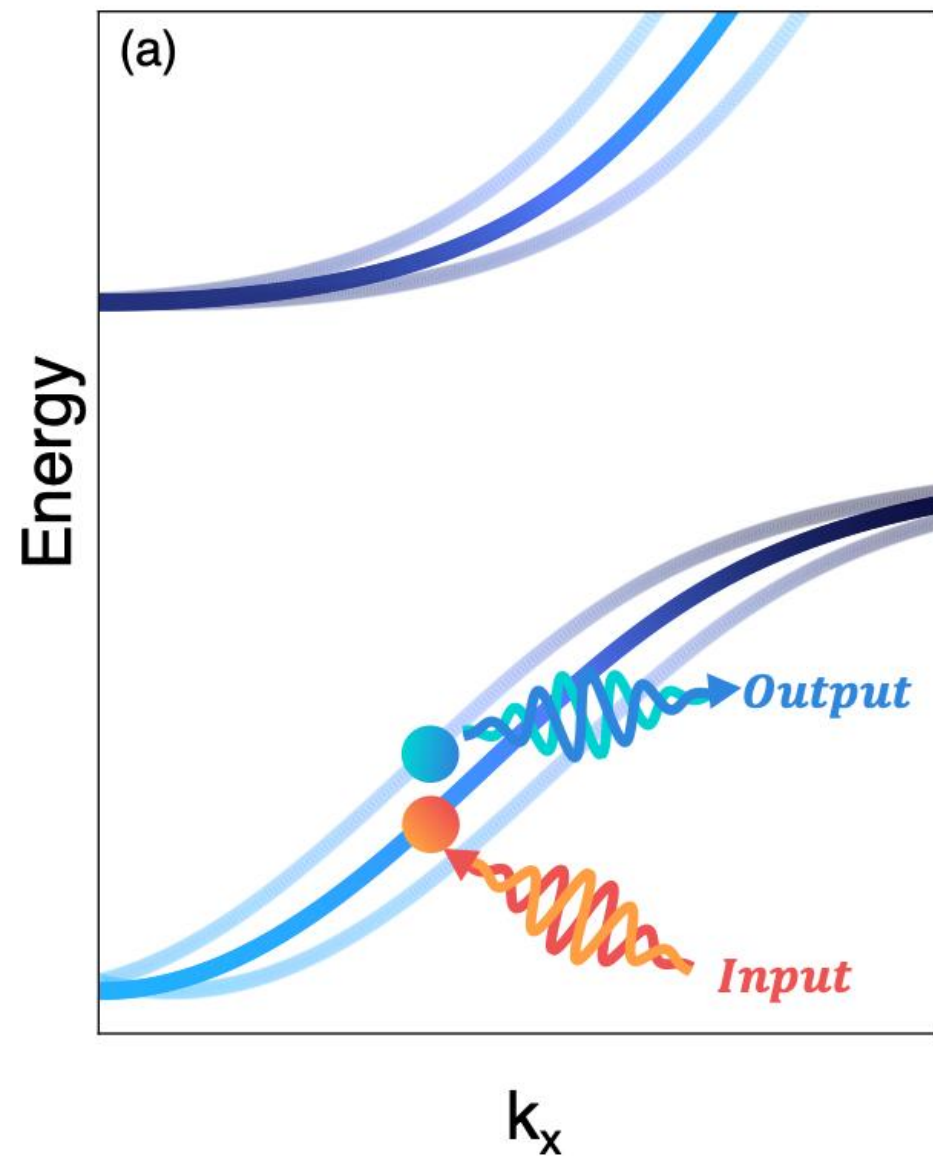


$$\langle 0 | \left(A_{k_1+2\Delta k}^\dagger + A_{k_2+2\Delta k}^\dagger \right) | \psi(t) \rangle$$

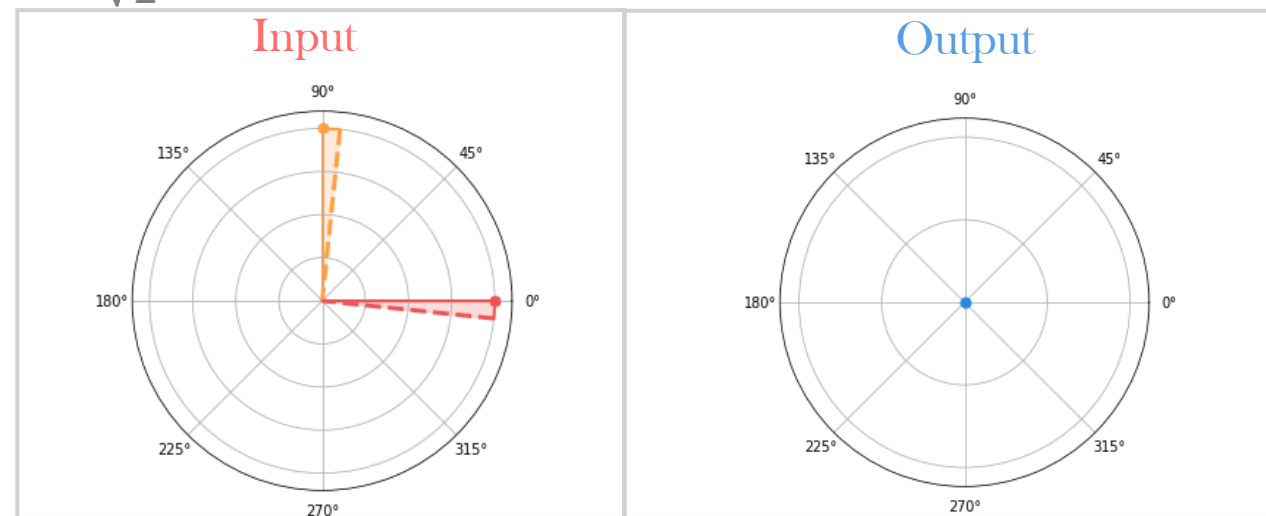


Coherent Frequency Conversion

$$\frac{1}{\sqrt{2}} \left(a_{k_1}^\dagger + e^{i\pi} a_{k_2}^\dagger \right) |0\rangle$$



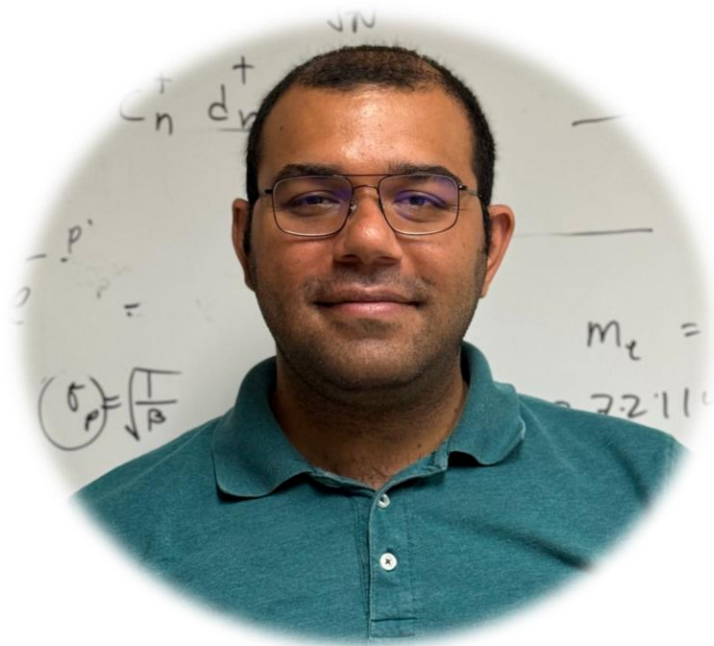
$$\frac{1}{\sqrt{2}} \left(a_{k_1}^\dagger + e^{i\frac{\pi}{2}} a_{k_2}^\dagger \right) |0\rangle$$



Summary

- ❑ Multilayer material-cavity configurations give rise to a **phonon-fluctuation synchronization effect**
- ❑ This synchronization leads to **enhanced quantum coherence**, accompanied by **more robust polaritonic transport properties**.
- ❑ The relaxation pathway from the upper to the lower polariton is strongly modified by the presence of **dark layers**, resulting in a **two-step relaxation mechanism**:
 - ❑ Step I: A momentum-conserving direct transition
 - ❑ Step II: Phonon-induced Fröhlich-type intraband scattering
- ❑ When the material is tilted inside the cavity, a **light-matter moiré effect** emerges. However, increasing the material thickness causes this effect to fade away.
- ❑ Finally, we derive simple analytical expressions that directly relate a material's finite thickness to its relaxation dynamics and coherence properties.

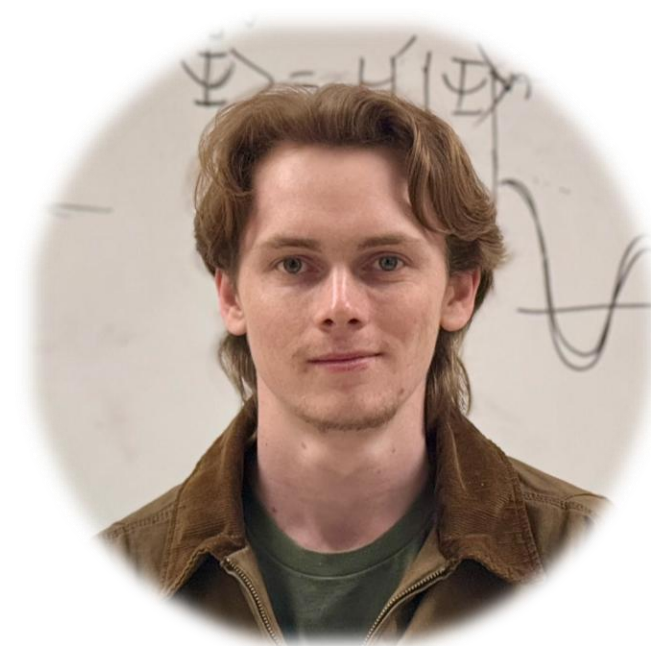
Acknowledgements



Saeed Rahmanian Koshkaki



Logan Blackham



Ian Haines





Light & Matter Research Group
at Texas A&M



TEXAS A&M
UNIVERSITY®

